

## RESEARCH

# In-flight Scalar Calibration and Characterisation of the Swarm Magnetometry Package

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## Abstract

We present the in-flight scalar calibration and characterisation of the *Swarm* magnetometry package consisting of the absolute scalar magnetometer (ASM), the vector magnetometer (VFM), and the spacecraft structure supporting the instruments. A significant improvement in the scalar residuals between the pairs of magnetometers is demonstrated, confirming the high performance of these instruments. The results presented here, including the characterization of a Sun-driven disturbance field, form the basis of the correction of the magnetic vector measurements from *Swarm* which is applied to the *Swarm* Level 1b magnetic data.

**Keywords:** Geomagnetism; Magnetometer; Instrument Calibration; Satellite; *Swarm*

1

2

## 1 Introduction

In November 2013 the European Space Agency (ESA) launched the three *Swarm* satellites named *Alpha*, *Bravo*, and *Charlie* with the objective to provide the best ever survey of the geomagnetic field and its temporal evolution ([Friis-Christensen et al., 2006](#)). Each spacecraft carries an Absolute Scalar Magnetometer (ASM) for measuring Earth's magnetic field intensity, a Vector Fluxgate Magnetometer (VFM) measuring the direction and strength of the magnetic field, and a three-head Star TRacker (STR) mounted close to the VFM to obtain the attitude needed to transform the vector readings to an Earth fixed coordinate frame. Time and position are provided by an on-board GPS receiver. The payload also includes instruments to measure plasma and electric field parameters as well as non-gravitational acceleration. More information on the mission status after two years in orbit can be found in [Floborghagen et al. \(2016\)](#).

16

One of the purposes of the scalar magnetometer (ASM) is to provide the necessary absolute magnetic data to calibrate the vector magnetometer (VFM). For this an approach similar to that adopted for the previous satellite missions Ørsted and CHAMP was foreseen (c.f. [Olsen et al., 2003](#); [Yin and Lühr, 2011](#)) since those missions carried equivalent instrumentation. However, soon after launch of *Swarm* it became clear that the magnetic field vector measurements on all three spacecraft were contaminated by unforeseen disturbances which could not be captured by the traditional in-flight calibration methods referred to above. Furthermore, the disturbances show systematic variation which could impact or map into scientific investigations based on *Swarm* magnetic data, The light blue symbols in Fig. 1 show

26

time series of the *scalar residuals*, which are the difference,  $\Delta F = |\vec{B}_{\text{VFM}}| - F_{\text{ASM}}$ , between the modulus of the VFM data,  $|\vec{B}_{\text{VFM}}|$ , and the magnetic intensity measurements,  $F_{\text{ASM}}$ , taken by the ASM instrument. Based on experience with Ørsted and CHAMP scalar residuals with sub-nanotesla level were expected (rms value well below 0.5 nT), while for *Swarm* the scatter of the residuals was observed to reach several nT, resulting in an rms value approaching 1 nT, but crucially showing a very clear Local Time dependence. A task force was therefore established to investigate and mitigate the effect.

Detailed investigations of the scalar residuals  $\Delta F$  and of the ASM and VFM measurements separately indicated that :

- the vector readings of the VFM are affected by a disturbance vector field;
- the scalar readings of the ASM are much less, if at all, affected.

Consequently the Task Force concluded to pursue models which assume the magnetic disturbance to be affecting the VFM measurements only. Plotting  $\Delta F$  as a function of the Sun incidence angles with respect to the spacecraft, reveals systematic features of the disturbance, as shown in Fig. 3. At the start of section 2 we provide detailed definitions of the two Sun incidence angles  $\alpha$  and  $\beta$ . This supports the hypothesis that a magnetic source in the vicinity of the VFM magnetometer, with strength and direction depending on the direction to the Sun (as seen from the spacecraft), is responsible. We refer to such a disturbance field vector, that depends on the direction to the Sun, as  $\delta\vec{B}_{\text{Sun}}$ .

The purpose of this article is to document the details of in-flight calibration of the *Swarm* magnetometer package, including an empirical determination and removal of the Sun driven vector disturbance field  $\delta\vec{B}_{\text{Sun}}$ , based on a mitigation approach proposed by Vincent Lesur ([Lesur et al., 2015](#)).

Section 2 describes the parameterisation of the model of the Sun-driven disturbance – in following referred to as the *characterisation* of the disturbance field – and of the *calibration* of the VFM instrument, by which means determination of its intrinsic scale factors and their dependence on time and temperature, and determination of the sensor-axis non-orthogonalities. We document the adopted Iteratively Reweighted Least Squared (IRLS) estimation approach, that includes a truncated singular value decomposition (SVD) approach to solving the inverse problem. The results obtained for *Swarm Alpha*, based on data covering the period from launch (22. November 2013) until end of June 2015 (i.e. 19 months), are presented in Section 3. Application of the scheme to data from the satellites *Bravo* and *Charlie* resulted in similar levels of residual improvement and statistics, and the estimates of the Sun driven disturbance  $\delta\vec{B}_{\text{Sun}}$  show generally similar behaviour and structural features as found for *Swarm Alpha*, although there are also some differences. Finally, Section 4 summarizes the findings and provides perspectives regarding further improvements of the method.

## 71 2 Characterisation and Calibration with Scalar Residuals

72 The Sun incidence angles  $\alpha$  and  $\beta$  are crucial in our approach to *characterise* the  
 73 scalar residual. To clarify, in Fig. 2 we illustrate the definition of these angles with  
 74 respect to the spacecraft and the Sun position.  $\alpha$  is the azimuth in the spacecraft  
 75 x-z plane (nominally the orbit plane) and  $\beta$  is the “elevation” out of the x-z plane  
 76 positive towards *left* (looking in the nominal flight direction; i.e. positive *opposite*  
 77 the spacecraft  $y$  axis). Considering how these angles vary over orbits of the *Swarm*  
 78 spacecraft, we find the angle  $\alpha$  varies rapidly: from  $0^\circ$  to  $360^\circ$  within one orbit (i.e.  
 79 within  $\approx 90$  minutes) while the other angle,  $\beta$ , varies more slowly (by  $\approx 1.5^\circ$  in one  
 80 day).

- 81 •  $\beta = +90^\circ$ : Sun directly from  $-y$  (i.e. from the left during nominal flight)
- 82 •  $\beta = -90^\circ$ : Sun directly from  $+y$  (i.e. from the right)
- 83 •  $\beta = 0^\circ, \alpha = 0^\circ$  : Sun directly from  $+x$  (i.e. from the front)
- 84 •  $\beta = 0^\circ, \alpha = +90^\circ$  : Sun directly from  $-z$  (above)
- 85 •  $\beta = 0^\circ, \alpha = +180^\circ$  : Sun directly from  $-x$  (i.e. from the back – slightly above  
 86 the boom)

87 Considering how these angles vary over orbits of the *Swarm* spacecraft during nom-  
 88 inal flight, we find that  $\alpha$  varies rapidly: from  $360^\circ$  down to  $0^\circ$  within one orbit (i.e.  
 89 within  $\approx 90$  minutes) while  $\beta$ , varies slowly up and down typically by  $\approx 1.25^\circ$  in  
 90 one day (for *Alpha* and *Charlie*,  $1.20^\circ$  for *Bravo*).

91  
 92 Although the observed scalar residuals clearly vary with the Sun incidence angles  
 93  $\alpha$  and  $\beta$  (see Fig. 3) there is no direct mapping of  $\Delta F$  in terms of these parameters.  
 94 This is a consequence of the scalar residuals  $\Delta F \approx \delta \vec{B}_{\text{Sun}} \cdot \vec{b}_0$  being the projection  
 95 of the magnetic disturbance vector  $\delta \vec{B}_{\text{Sun}}$ , onto the unit vector  $\vec{b}_0$  of the ambient  
 96 magnetic field direction (Earth’s main field). The former is oriented relative to  
 97 the spacecraft while the latter is oriented relative to Earth, which results in the  
 98 variations with the spacecraft local time (captured by  $\beta$ ) as seen in Fig. 3. The  
 99 spacecraft local time changes by 12 hours (corresponding to a change in  $\beta$  by  $180^\circ$ )  
 100 within approximately  $4\frac{1}{2}$  months.

101  
 102 To account for the projection on to the ambient field, we consider a *vector* mag-  
 103 netic disturbance  $\delta \vec{B}_{\text{Sun}}(\alpha, \beta)$ , with each component depending individually on the  
 104 Sun incidence angles. Mathematically, we describe each component of the distur-  
 105 bance field vector by a spherical harmonic expansion in  $\alpha$  and  $\beta$  i.e. we consider  
 106 three independent spherical harmonic expansions in all.

107  
 108 This model *characterizing* the Sun-driven disturbance is co-estimated together  
 109 with a model of the temporal evolution of the VFM sensitivity and an adjustment  
 110 of the pre-flight estimated non-orthogonality angles of the VFM sensor. For this we  
 111 perform a *scalar calibration* via a least squares fit, minimizing the discrepancy ( $\Delta F$ )  
 112 between the measurements from ASM and the modulus of the vector measurements  
 113 from the VFM after our model has been applied. Huber weights are used iteratively  
 114 to eliminate the effect of anomalous measurements (“outliers”) on the estimated  
 115 models.

## 117 2.1 Model Parameterisation

118 As outlined above, our model characterizing the Sun-driven disturbance vector  
 119  $\delta\vec{B}_{\text{Sun}}$  consists of three spherical harmonic expansions up to degree and order 25,  
 120 one for each of the magnetic field components in the VFM magnetometer frame,  
 121 with the position of the Sun with respect to the spacecraft parameterised by the  
 122 Sun incidence angles  $\alpha$  and  $\beta$ . It takes the form

$$\delta\vec{B}_{\text{Sun}} = \sum_{n=0}^{25} \sum_{m=0}^n (\vec{u}_n^m \cos m\alpha + \vec{v}_n^m \sin m\alpha) P_n^m(\sin \beta)$$

123 where  $\vec{u}_n^m$  and  $\vec{v}_n^m$  are the spherical harmonic expansion coefficients, with one com-  
 124 ponent for each component of the disturbance field, and  $P_n^m$  are the Schmidt semi-  
 125 normalized Legendre functions. Note that  $\delta\vec{B}_{\text{Sun}}$  includes static terms ( $n = m = 0$ ),  
 126 that describe a static (i.e. independent of the Sun position) disturbance vector.  
 127 The disturbance field vector  $\delta\vec{B}_{\text{Sun}}$  is thus described by  $3 \times 26^2 = 2,028$  model  
 128 coefficients.

129  
 130 The model for re-scaling the vector measurements and taking into account any  
 131 small adjustment of the non-orthogonality of the VFM sensors, which is required in  
 132 order to obtain the fully calibrated and corrected vector field measurements  $\vec{B}_{\text{VFM}}$ ,  
 133 now takes the form

$$\vec{B}_{\text{VFM}} = \underline{\underline{P}}^{-1} \underline{\underline{S}}^{-1} \vec{B}_{\text{pre-flight}} - \delta\vec{B}_{\text{Sun}}$$

134 where  $\vec{B}_{\text{pre-flight}}$  are the VFM measurements calibrated using the pre-flight param-  
 135 eters and corrected for the pre-flight determined stray fields as described in [Tøffner-  
 136 Clausen \(2015\)](#).  $\underline{\underline{S}}$  is a  $3 \times 3$  diagonal scaling matrix with elements

$$s_j = s^{\text{B-spline}}(t) + s_{j, T_{\text{sensor}}} T_{\text{sensor}} + s_{j, \beta} \beta$$

137 where  $s^{\text{B-spline}}(t)$  is a quadratic B-spline in time with 3-month knot separation  
 138 (common for all three components of the magnetic field), and  $s_{j, T_{\text{sensor}}}$ ,  $j = 1 - 3$   
 139 is an adjustment of the pre-flight estimated dependency of the VFM sensitivity on  
 140 its sensor temperature,  $T_{\text{sensor}}$ , for each sensor axis  $j$ .  $s_{j, \beta}$  is an empirical scaling  
 141 parameter and  $\beta$  the Sun incidence angle, as defined above. The choice of quadratic  
 142 B-splines with 3-month knot separation is made to allow sufficient flexibility of the  
 143 model. The estimated B-splines exhibit very moderate accelerations (in the case of  
 144 the full model, see Fig. 6) and it may be possible to simplify the parameterisation  
 145 of the time-dependence in future models.

146  
 147  $\underline{\underline{P}}$  is the non-orthogonality matrix that makes small adjustments to the pre-flight  
 148 estimated non-orthogonalities of the VFM sensor (cf. [Olsen \*et al.\*, 2003](#))

$$\underline{\underline{P}} = \begin{pmatrix} 1 & 0 & 0 \\ -\sin u_1 & \cos u_1 & 0 \\ \sin u_2 & \sin u_3 & \sqrt{1 - \sin^2 u_2 - \sin^2 u_3} \end{pmatrix}$$

149 Our in-flight calibration model comprises 18 parameters in all; together with the  
 150 2,028 parameters describing  $\delta\vec{B}_{\text{Sun}}$  this results in 2,046 model parameters to be  
 151 estimated, as listed in Table 1.

## 152 2.2 Estimation of Model Parameters: Inversion and Regularisation

153 In order to estimate the 2,046 model parameters from the scalar residuals we need  
 154 to solve a nonlinear inverse problem. The nonlinearity arises from the the treatment  
 155 of non-orthogonalities (*Olsen et al., 2003*).

156  
 157 The forward relationship between the vector of the scalar residuals,  $\mathbf{d}$ , ( $d_i = \Delta F_i$ ,  
 158 the scalar residual of the  $i$ th data point) and the model parameter vector  $\mathbf{m}$ , may  
 159 therefore be written in the form

$$\mathbf{d} = \mathbf{g}(\mathbf{m}) + \mathbf{e}$$

160 where  $\mathbf{g}(\mathbf{m})$  is a nonlinear function of the models parameters and  $\mathbf{e}$  is a small re-  
 161 mainder, that cannot be explained by the model, which we seek to minimise.

162  
 163 Linearisation of this problem is straightforward. A *regularized, iteratively-*  
 164 *reweighted, least squares solution* to the inverse problem, is then obtained using  
 165 the algorithm

$$\mathbf{m}_{k+1} = \mathbf{m}_k + (\underline{\mathbf{G}}_k^T \underline{\mathbf{W}}_k \underline{\mathbf{G}}_k + \lambda \underline{\mathbf{R}})^{-1} \left( \underline{\mathbf{G}}_k^T \underline{\mathbf{W}}_k [\mathbf{d} - \mathbf{g}(\mathbf{m})] - \lambda \underline{\mathbf{R}} \mathbf{m}_k \right)$$

166 where at the  $k$ th iteration,  $\underline{\mathbf{G}}_k = \left. \frac{\partial \mathbf{g}(\mathbf{m})}{\partial \mathbf{m}} \right|_{\mathbf{m}=\mathbf{m}_k}$ , is the appropriate Jacobian ma-  
 167 trix,  $\underline{\mathbf{R}}$  is a regularization matrix discussed in detail below, and  $\underline{\mathbf{W}}_k$  is a (Huber)  
 168 weighting matrix.

169

$\underline{\mathbf{W}}_k$  are updated at each iteration, and consists of diagonal elements

$$w_i = \min \left( 1, \frac{c\sigma}{\Delta F_i} \right).$$

$\Delta F_i = \left| \vec{B}_{i,\text{VFM}} \right| - F_{i,\text{ASM}}$  is the scalar residual of the  $i$ th data point, with  $\vec{B}_{i,\text{VFM}}$   
 calculated using the model parameters from iteration  $k$ , and  $F_{\text{ASM}}$  being the fully  
 calibrated and corrected scalar field measurements from the ASM scalar magne-  
 tometer, and

$$\sigma = \sqrt{\frac{\sum_i (w_i \Delta F_i)^2}{\sum_i w_i^2}},$$

170 being a (robust) estimate of the standard deviation of the residuals at iteration  $k$ .  
 171 We set  $c = 2$ , slightly higher than the value of 1.5 usually chosen, in order to ensure  
 172 that the less numerous polar data are not overly downweighted in the determination  
 173 of the calibration parameters.

174

175 It turns out that the full set of 2,046 parameters is not needed to obtain good  
 176 results and low data misfit, which is confirmed by inspection of the eigenvalues of the  
 177 matrix  $(\underline{\mathbf{G}}_k^T \underline{\mathbf{W}}_k \underline{\mathbf{G}}_k + \lambda \underline{\mathbf{R}})$ , as presented in Fig. 4 for *Swarm Alpha*. The magnitudes  
 178 of the sorted eigenvalues (in order of decreasing magnitude) exhibit a distinct drop  
 179 around 750-800 degrees of freedom, indicating the smaller eigenvalues contribute  
 180 little to the solution. The inversion of this matrix was therefore finally performed  
 181 using a truncated singular value decomposition (TSVD) procedure, retaining only  
 182 750 degrees of freedom.

183

184 A regularization matrix  $\underline{\mathbf{R}}$  is also included to help to stable the inversion. This  
 185 is necessary because the *Swarm* satellites operates in a tightly controlled attitude  
 186 orientation which leads to a poor excitation of the VFM instrument along the axis  
 187 perpendicular to the orbit plane (the East-West direction corresponding to the  $y$ -  
 188 axis of the VFM sensor). Consequently, the parameters related to the  $y$ -axis are  
 189 poorly determined in a scalar calibration. The regularization matrix  $\underline{\mathbf{R}}$  is there-  
 190 fore defined so that it acts on the parameters  $s_{2,\text{Tsensor}}$ ,  $s_{2,\beta}$ ,  $u_1$ , and  $u_3$  to force  
 191  $s_{2,\text{Tsensor}} \simeq (s_{1,\text{Tsensor}} + s_{3,\text{Tsensor}}) / 2$  (to reflect the physical properties of the VFM  
 192 sensor) and also to minimize the norms  $s_{2,\beta}^2$  and  $u_1^2 + u_3^2$ .  $\lambda$  is chosen to be sufficiently  
 193 large to effectively impose the regularisation on the estimated model. Note that no  
 194 regularisation is directly imposed on  $\delta \vec{B}_{\text{Sun}}$  but use of truncated SVD during the  
 195 inversion automatically acts to suppresses structure in regions that are not well  
 196 constrained by the input data.

197

198 The starting model for the inversions is “unity”, i.e.  $\underline{P} = \underline{S} = \underline{I}$ , where  $\underline{I}$  is  
 199 the identity matrix, and  $\vec{u}_n^m = \vec{v}_n^m = \vec{0}$ . The inversions typically converge within  
 200 25 iterations.

### 201 3 Results of Model Estimation for Swarm Alpha

202 The model described above is estimated for *Swarm Alpha* using data from the begin-  
 203 ning of the mission (22 November 2013) until June 2015. Fig. 1 shows the final scalar  
 204 residuals, i.e. the residuals after application of the model (after “calibration and  
 205 correction”) of the VFM measurements, (in green) as a function of time. together  
 206 with the residuals of the un-corrected but re-scaled vector field measurements, i.e.  
 207  $\vec{B}_{\text{VFM}} + \delta \vec{B}_{\text{Sun}}$ , in light blue; these data illustrate what can be achieved with the  
 208 traditional scalar calibration methods. Note the excellent reduction of the scalar  
 209 residuals achieved by the model; the Huber weighted rms of the residuals drops  
 210 from 963 pT to 168 pT. Table 2 provides the corresponding numbers for *Bravo* and  
 211 *Charlie*.

212

213 Fig. 5 shows normal distribution plots for the scalar residuals. The top plot  
 214 shows the distributions of all data for un-corrected (red) and fully corrected data  
 215 (green) and demonstrates a transition from a non-Gaussian to Gaussian residual  
 216 distribution when applying the model. The bottom plots show the distributions  
 217 of the data split into 3-months periods, un-corrected to the left and corrected to  
 218 the right. These also demonstrate the elimination of systematic and non-Gaussian  
 219 effects.

220

221 Table 3 lists the estimated  $s_{\text{Tsensor}}$  and  $s_{\beta}$  parameters, and the non-orthogonality  
 222 values for all three *Swarm* satellites together with their estimated pre-flight values  
 223 for the VFM instrument itself for reference. I.e. the table shows the adjustments  
 224 applied in order to reduce the scalar residuals to the level indicated above.

225

226 Table 4 shows the increase in the weighted rms of the scalar residuals when omitting  
 227 individual parts of the model – a full re-estimation of the remaining model  
 228 parameters is carried out for each table entry. Particularly the omission of the  
 229 non-orthogonalities drastically increases the misfit – the power (the mean-square)  
 230 is more than doubled. Due to the stable attitude of the *Swarm* satellites, the  
 231 small  $x$ - $z$  non-orthogonality angle,  $u_2$ , is equivalent to a small, relative timeshift  
 232 between the ASM and VFM measurements – 1 arc-second corresponds roughly to  
 233 a 3 ms timeshift, and it has been discussed whether it would be more reasonable  
 234 to introduce such timeshifts rather than adjusting the pre-flight estimated non-  
 235 orthogonalities. However, the variations in the  $u_2$  angles estimated by this model  
 236 would imply time-shifts varying from  $-3$  ms to  $+13$  ms for the individual satel-  
 237 lites which seems quite unlikely.

238

239 The temporal evolution of the scaling of the vector field measurements,  $s^{B-spline}$ ,  
 240 is shown in Fig. 6 for the various test models listed in Table 4. The full model,  
 241 shown in green, shows a smooth behaviour in time, as expected from an instrument  
 242 design perspective. The blue curve shows the model without  $s_{\beta}$ ; this exhibits some  
 243 small oscillations, whereas the red (no  $s_{\text{Tsensor}}$ ) and magenta (no  $\delta\vec{B}_{\text{Sun}}$ ) curves  
 244 show much higher level of oscillations indicating they are inadequate to capture  
 245 the behaviour of the measurements. The cyan curve shows the model without non-  
 246 orthogonalities; this is rather close to the curve of the full model and indicates the  
 247 decoupling of the non-orthogonalities from any long-term temporal effect of the  
 248 measurement disturbances and instruments.

249

250 Maps of the three components of the estimated disturbance fields from the full  
 251 model as function of Sun incidence angles  $\alpha$  (abscissa) and  $\beta$  (ordinate) are given  
 252 in Figs. 7, 8, and 9 for *Swarm Alpha*, *Bravo*, and *Charlie* respectively. During nom-  
 253 inal flight, the Sun incidence angles traverse these plots horizontally from right  
 254 to left, and move up or down in  $\beta$  as the orbit plane moves through local time.  
 255 The Sun induced disturbance is observed to have temporal characteristics that are  
 256 observed in the plots as horizontally stretched features, these are attributed to  
 257 thermal capacitance: The Sun induced disturbance exhibits characteristic warm-up  
 258 and cool-down effects, i.e. the disturbance increases when the spacecraft is exposed  
 259 to the Sun, and decreases when the Sun exposure terminates. The time constants  
 260 for these effects are up to tens of minutes (corresponding to several tens of degrees  
 261 in the  $\alpha$  angle). This effect is captured by the spherical harmonic model expansion  
 262 of  $\delta\vec{B}_{\text{Sun}}$  and yields the horizontally stretched features in Figs. 7-9. Note also the  
 263 regions of nightside data (eclipse), the circled areas to the left of the figures, which  
 264 generally show less disturbance; this is not imposed by the model or any regulari-  
 265 sation, rather it is simply a result of the data itself, and thus another indicator of  
 266 the ability of the model to describe the observed disturbances. The plots also show

267 both the similarities and the differences in  $\delta\vec{B}_{\text{Sun}}$  between the three satellites.

268

## 269 4 Conclusions

270 We have established a predominantly empirical model for the calibration and cor-  
271 rection of the magnetic vector field measurements of the three *Swarm* spacecraft.  
272 The model is based on detailed studies of the observed scalar residuals between the  
273 measurements of the absolute scalar magnetometer, ASM, and the modulus of the  
274 measurements of the vector field magnetometer, VFM. The model has proven to be  
275 quite robust as more data are incorporated into the estimation of the model param-  
276 eters, although the ambiguity of determining vector disturbances from a pure scalar  
277 calibration affects the estimated correction vectors; these corrections do change  
278 non-negligibly (by a few tenths of a nT) as more data are added.

279

280 The estimated models reduce the scalar differences between the *Swarm* magne-  
281 tometers to generally below 0.5 nT with rms values well below 200 pT for all three  
282 satellites, and have been in operational use since April 2015 to produce corrected  
283 *Swarm* Level 1b magnetic field vector data (as of version 0401).

284

285 Future evolutions of the model presented here are foreseen to include changing  
286 the model of the temporal evolution of the VFM sensitivity from B-splines to an  
287 exponentially decaying function. Analysis of  $\delta\vec{B}_{\text{Sun}}$  also indicates that this vector is  
288 generally confined to a few, distinct directions which may be incorporated in future  
289 models. Finally, it may be possible to model the effect of the thermal capacitance  
290 using appropriate temporal filter functions which would lead to a significant reduc-  
291 tion of the number of parameters of the model.

292

### 293 *Data Availability*

294 The estimated disturbance vectors,  $\delta\vec{B}_{\text{Sun}}$ , are included in the operational Level 1b  
295 magnetic *Swarm* data products as `dB_Sun`.

296

297 Uncorrected data are available at <ftp://swarm-diss.eo.esa.int/Advanced/> (login  
298 required, access can be requested via <https://earth.esa.int/Swarm>).

299

### 300 **Author's contributions**

301 LTC carried out the in-flight scalar calibration and characterisation, analysed the results, and led the writing of this  
302 manuscript. VL proposed the model for the Sun induced vector disturbance,  $\delta\vec{B}_{\text{Sun}}$ , and made the first estimations  
303 using this model. NiO and CF supported the entire project with many discussions, suggestions, and source code.

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310 the VFM instruments.

311 This paper is the IGP contribution XXXX.

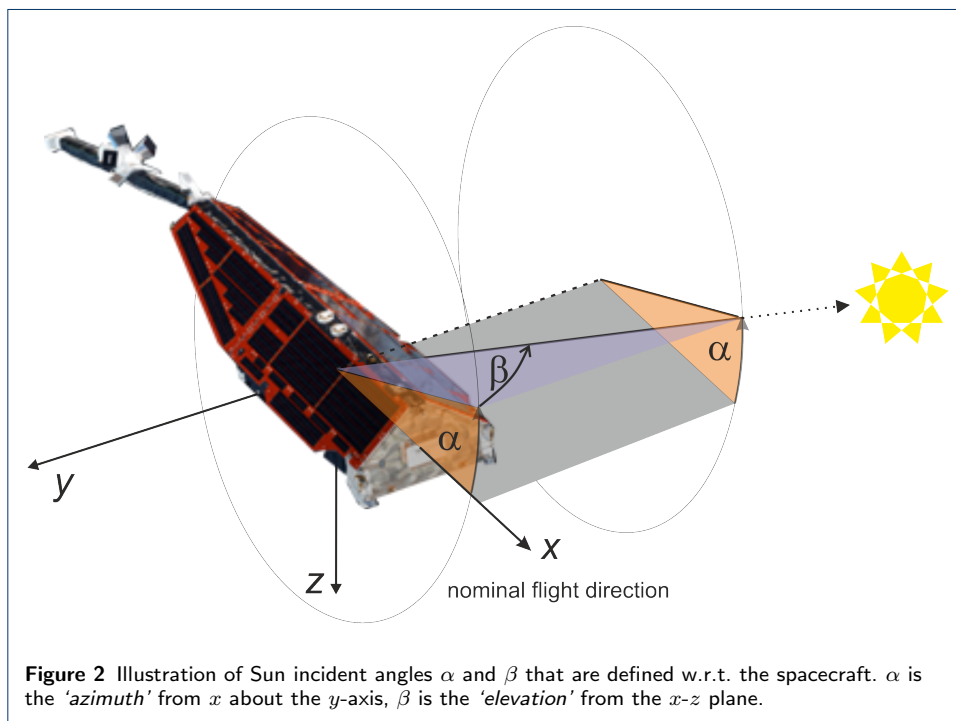
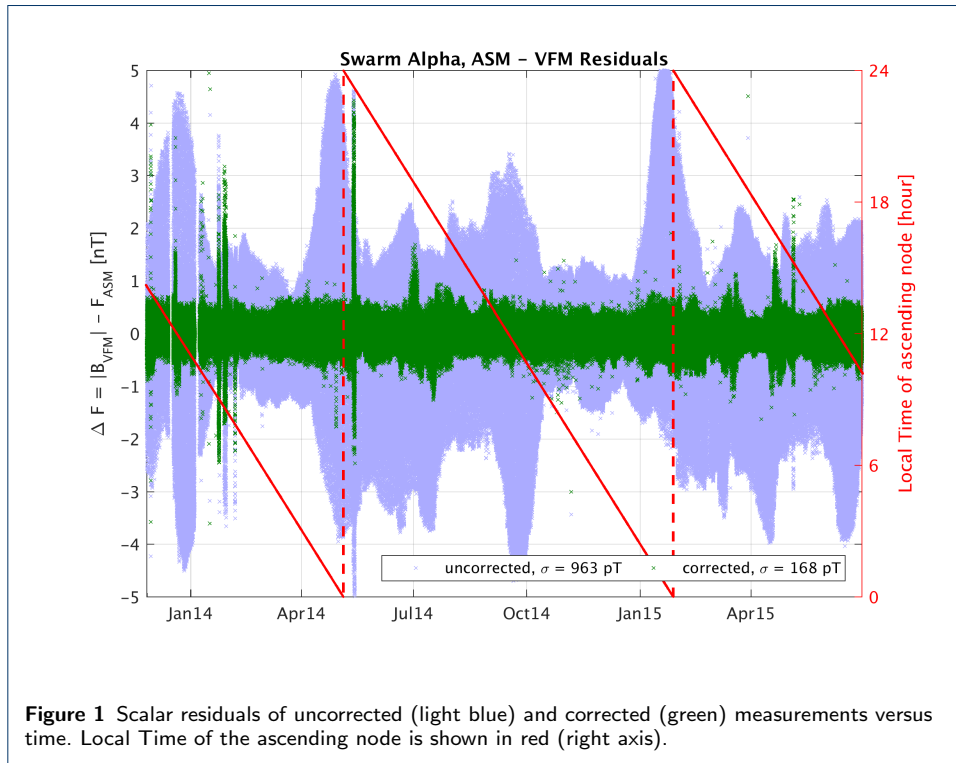


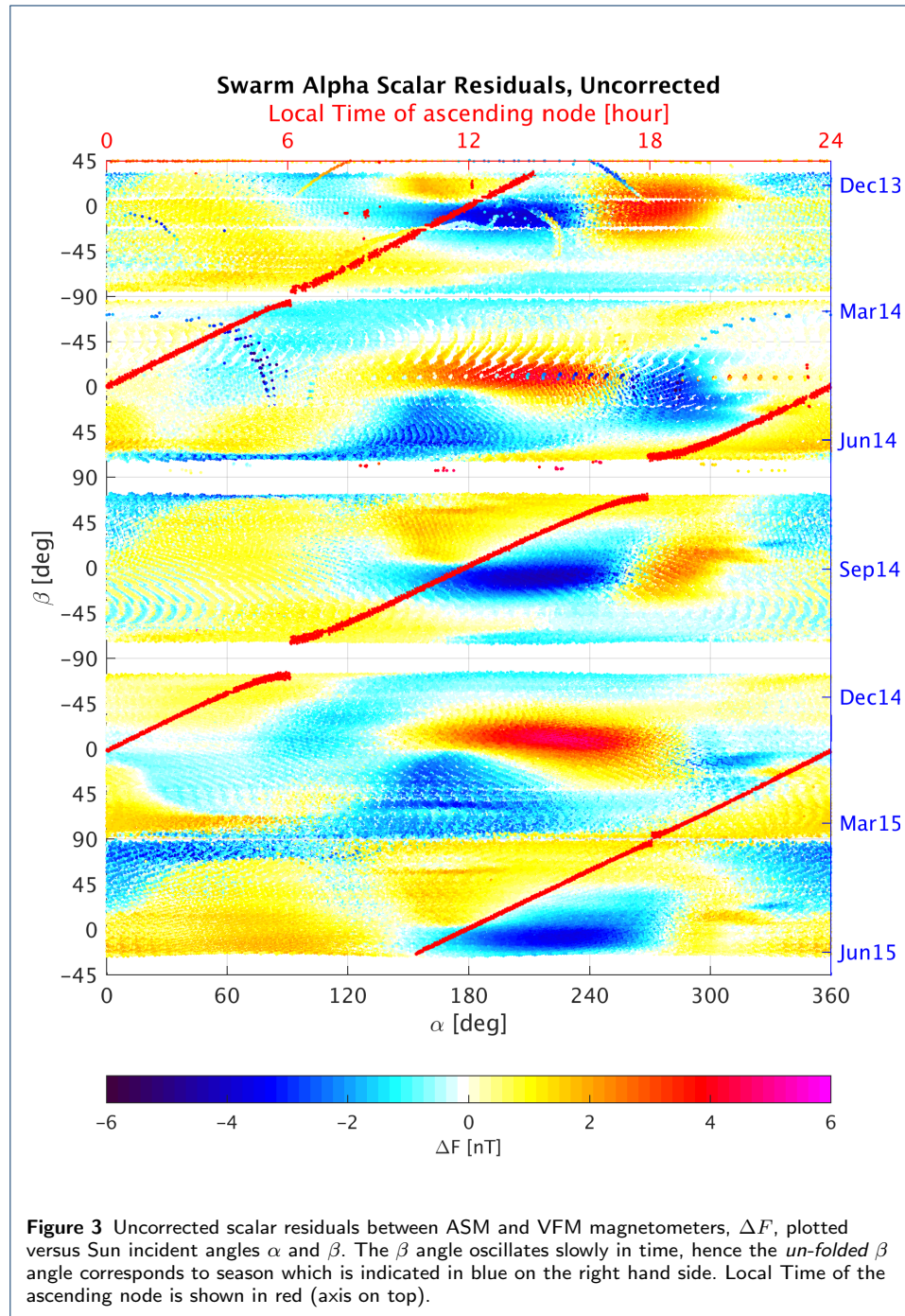
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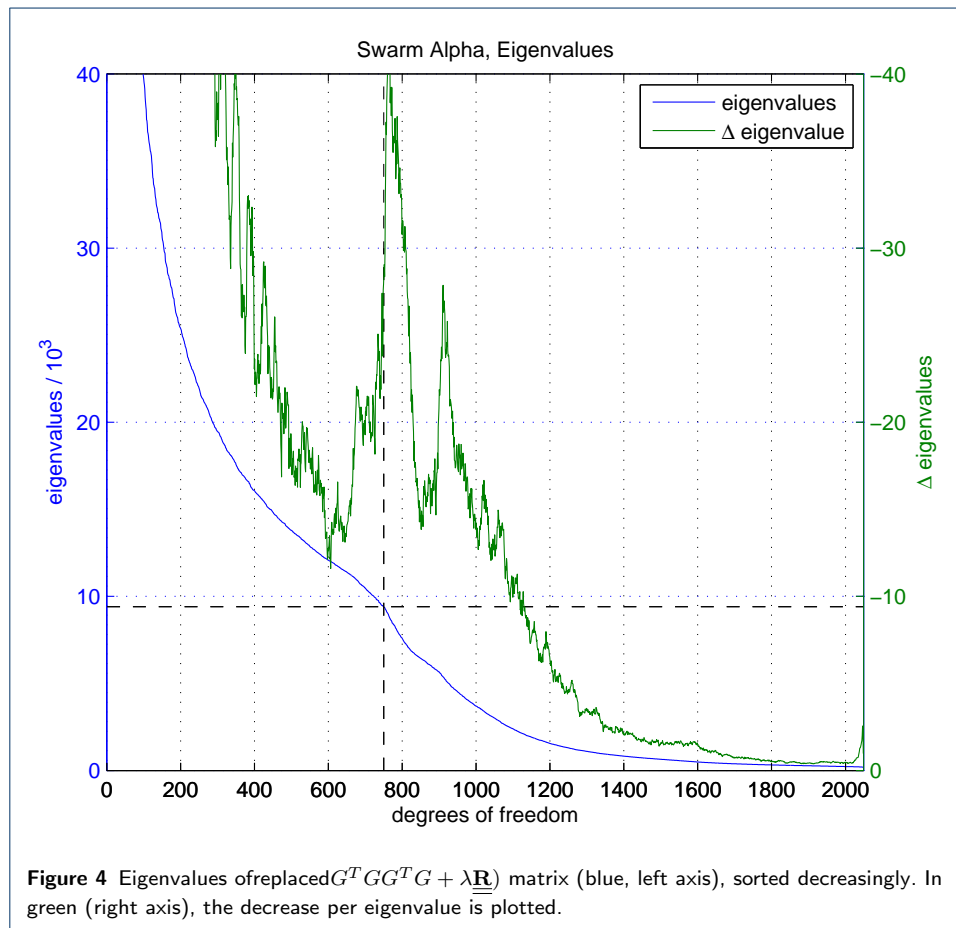
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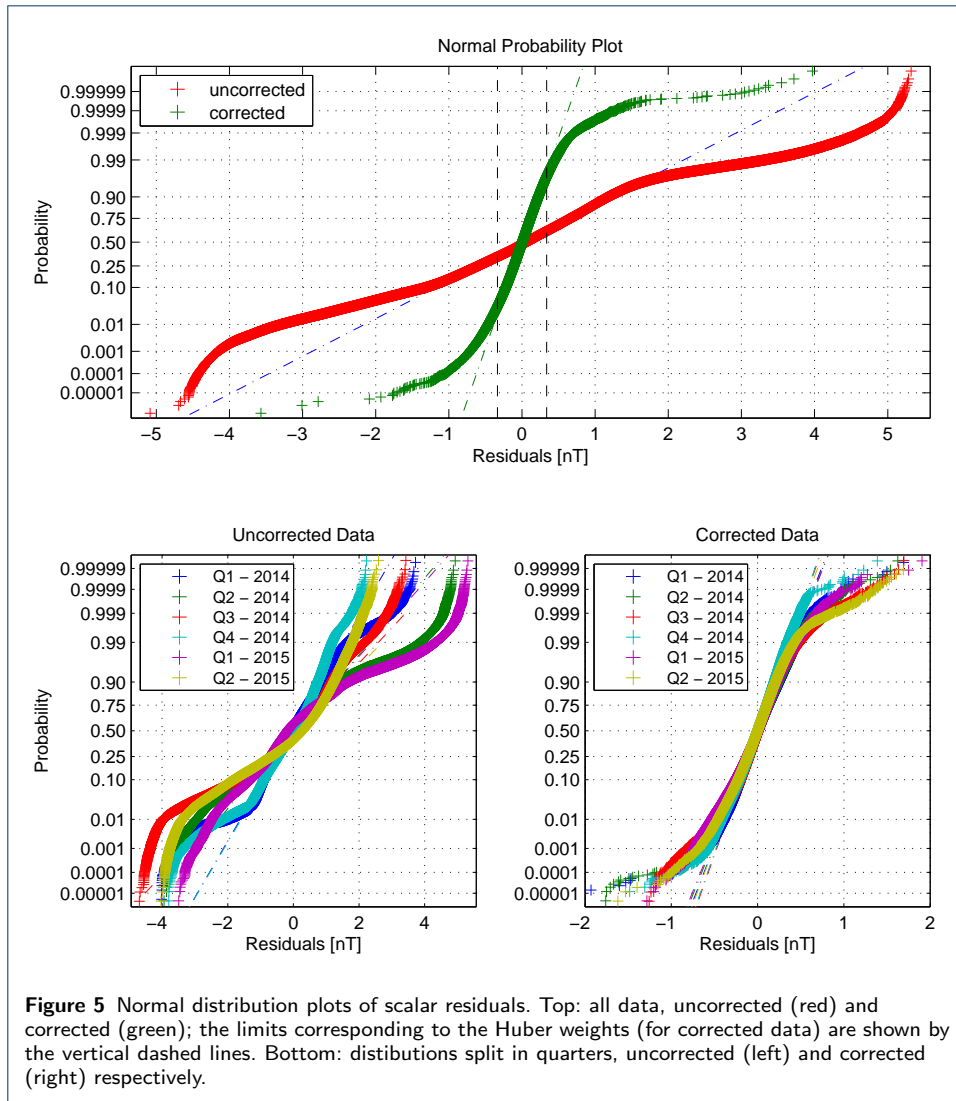
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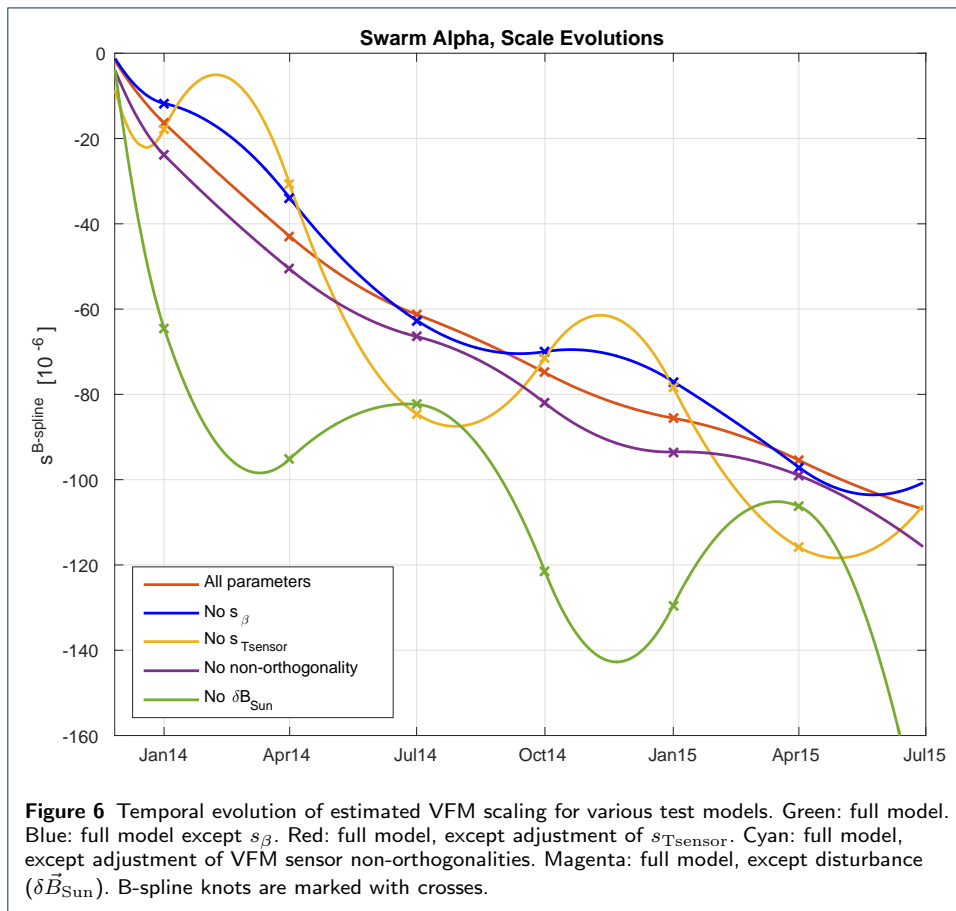
328 Figures



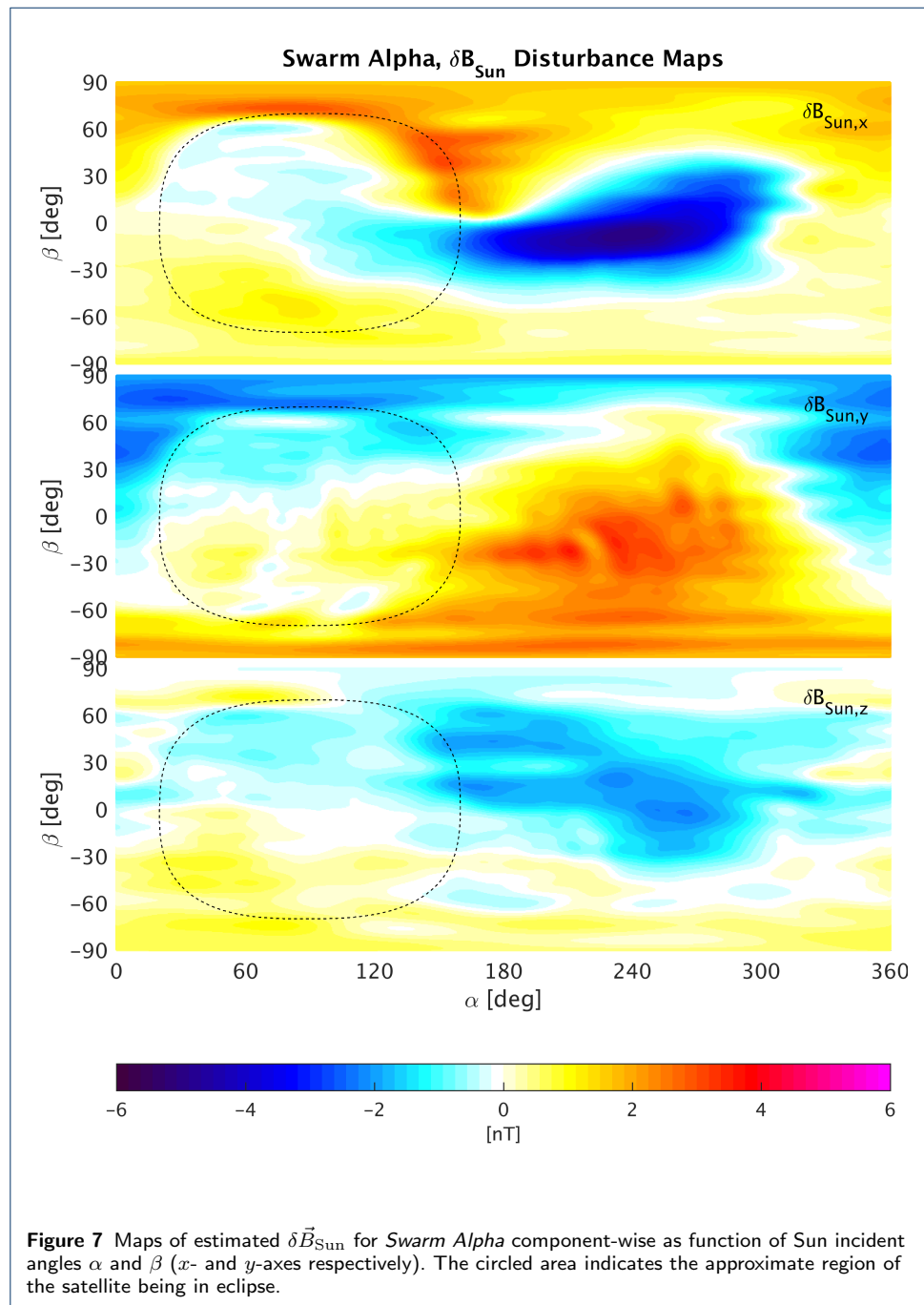


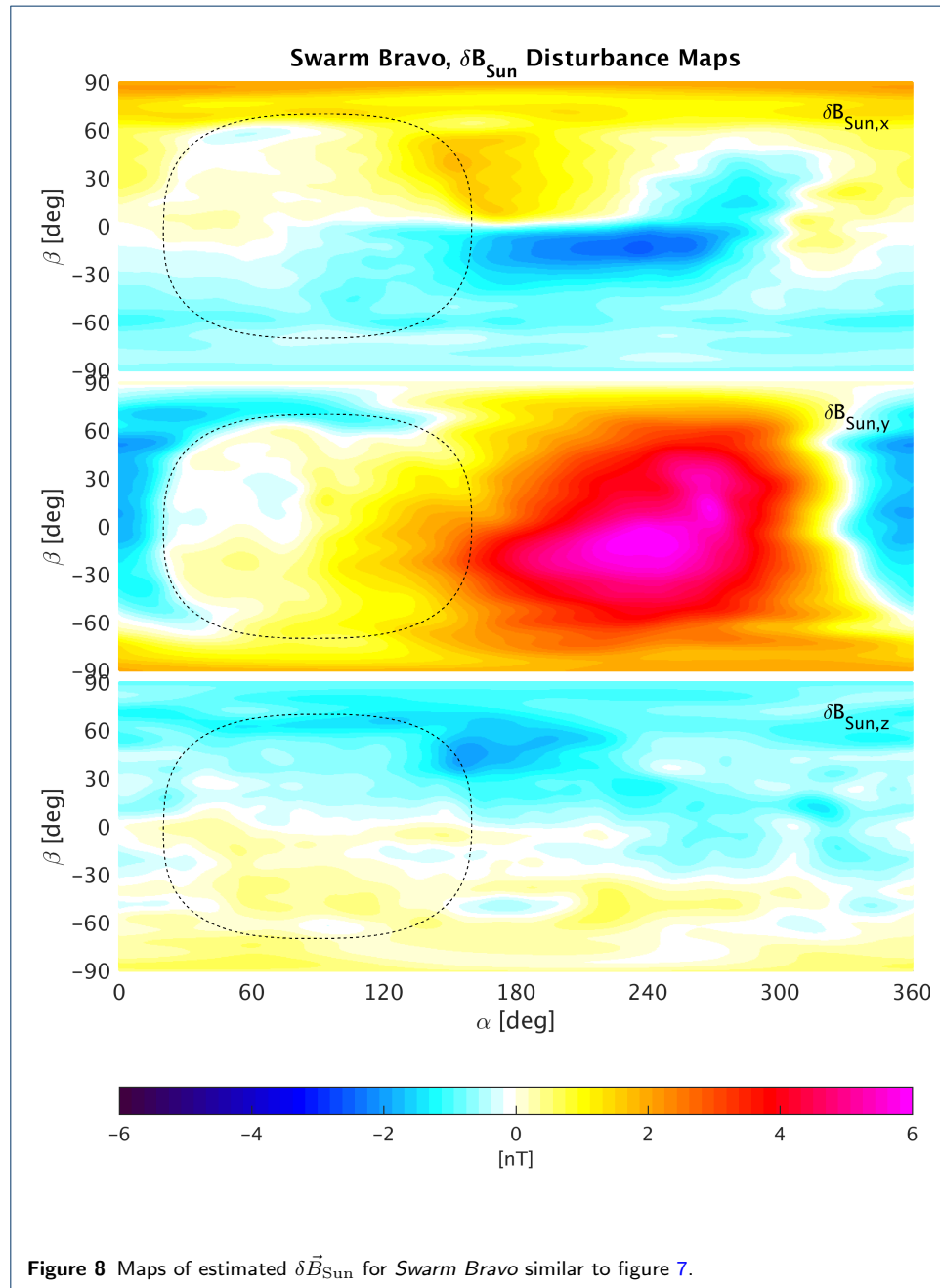




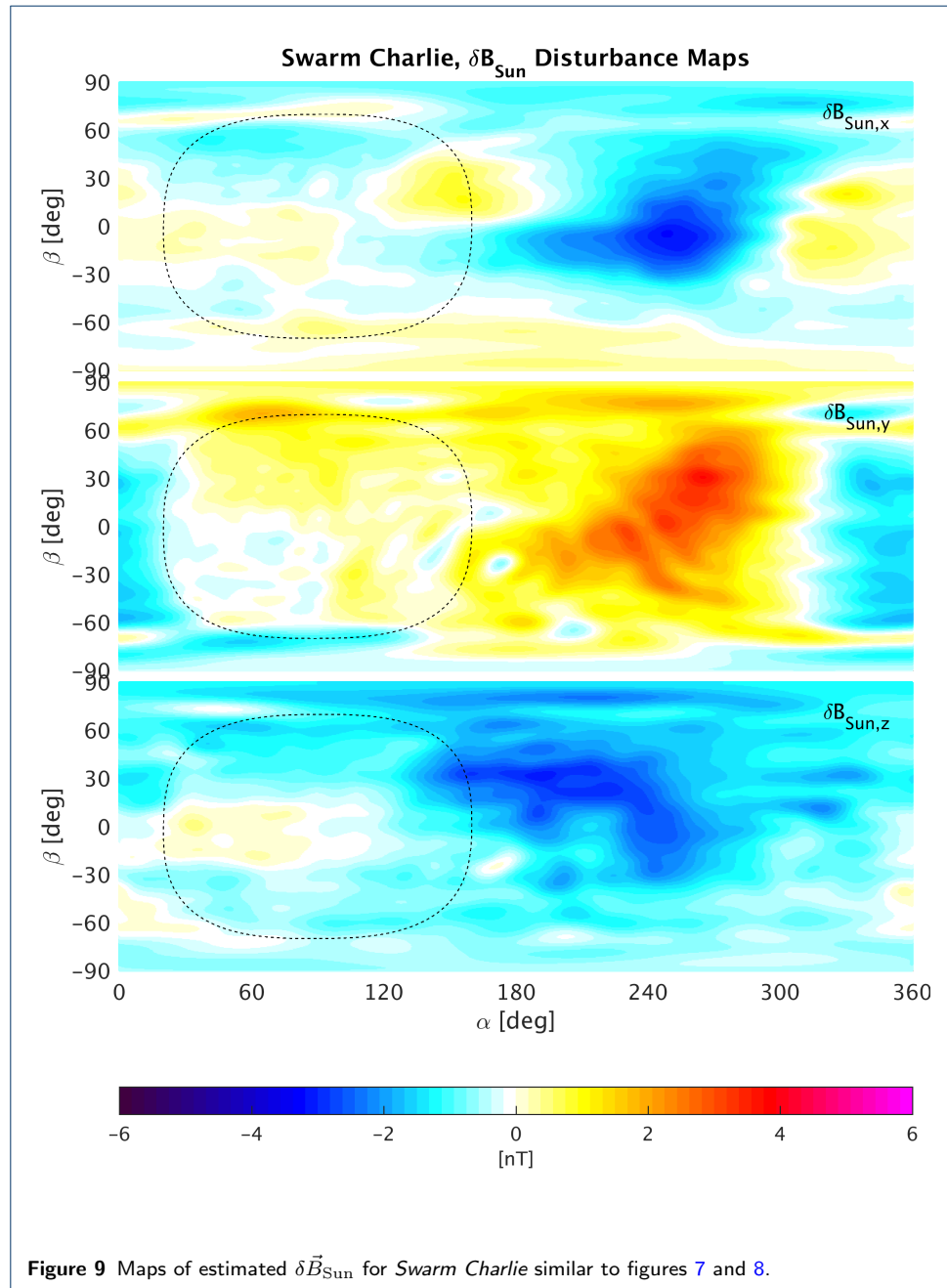


**Figure 6** Temporal evolution of estimated VFM scaling for various test models. Green: full model. Blue: full model except  $s_{\beta}$ . Red: full model, except adjustment of  $s_{T_{sensor}}$ . Cyan: full model, except adjustment of VFM sensor non-orthogonalities. Magenta: full model, except disturbance ( $\delta \vec{B}_{Sun}$ ). B-spline knots are marked with crosses.









## 329 Tables

**Table 1** Model parameters

Description	Parameters	Dimension
$\delta \vec{B}_{\text{Sun}}$	$\vec{u}, \vec{v}$	2,028
Sensitivity, time dependent	$s^{B\text{spline}}$	9
Sensitivity, $\beta$ dependency	$\vec{s}_{\beta}$	3
Sensitivity, sensor temperature dependency	$\vec{s}_{T\text{sensor}}$	3
Non-orthogonalities	$u_1, u_2, u_3$	3
Total		2,046

**Table 2** Scalar Residual Statistics, Uncorrected and Corrected Data.

For *Swarm Charlie* two sets of numbers are given; one set for which the ASM was still working ( $F_{\text{ASM}}$ , until 5. November 2014) and one set using the scalar data from *Swarm Alpha* mapped to the position of *Swarm Charlie* ( $F_{\text{AC,map}}$ ). For data from 1. May 2014 through 5. November 2014 the weighted rms of  $F_{\text{ASM}} - F_{\text{AC,map}}$  is 572.6 pT.

Satellite	Weighted rms [pT]	
	Uncorrected	Corrected
<i>Alpha</i>	962.6	168.3
<i>Bravo</i>	710.3	164.2
<i>Charlie</i> $F_{\text{ASM}}$	632.1	172.3
$F_{\text{AC,map}}$	862.1	527.7

**Table 3** Estimated values for selected model parameters for all three *Swarm* satellites. The  $nT$ -equivalents of the adjustments in a 50,000  $nT$  ambient field are:  $s_{T\text{sensor}} = 10^{-6}/^{\circ}\text{C} \sim 1.25 nT$  ( $25^{\circ}\text{C}$  temperature swing),  $s_{\beta} = 0.1 \times 10^{-6}/\text{deg} \sim \pm 0.45 nT$  ( $\pm 90$  deg),  $u = 1$  arc-second  $\sim 0.242 nT$ .

Sat	Sensitivity/sensor temperature, $s_{T\text{sensor}}$ , [ $10^{-6}/^{\circ}\text{C}$ ]		Sensitivity/ $\beta$ angle, $s_{\beta}$ , [ $10^{-6}/\text{deg}$ ]		Non-orthogonalities, $u_{1,2,3}$ , [arc-seconds]	
	Pre-flight	Adjustment	Pre-flight	Adjustment	Pre-flight	Adjustment
<i>Alpha</i>	28.5	0.616	–	-0.125	102.386	-0.601
	28.8	0.780	–	0	217.403	-3.960
	28.3	0.945	–	0.012	-179.318	0.149
<i>Bravo</i>	28.3	1.168	–	-0.132	350.880	-0.558
	29.0	1.385	–	-0.003	62.432	-2.453
	28.8	1.602	–	-0.198	-147.060	1.608
<i>Charlie</i>	27.7	1.521	–	-0.090	139.140	0.094
	29.1	1.300	–	-0.038	-248.890	1.042
	28.4	1.076	–	-0.167	-109.960	0.805

**Table 4** Weighted rms values for various models, *Swarm Alpha*

Model	weighted rms [pT]	Residual power (normalized)
Full model	168.3	100%
No $s_{\beta}$	176.1	107%
No $s_{T\text{sensor}}$	181.7	116%
No non-orthogonalities	250.2	221%
No $\delta \vec{B}_{\text{Sun}}$	962.6	3,269%