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Swarm Expert Support Laboratories  
**Proposal for Update of VFM - STR Euler  
 Angles**

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British Geological Survey (BGS)  
 National Space Institute – DTU Space (DTU)  
 Delft Institute of Earth Observation and Space Systems (DUT)  
 Helmholtz Centre Potsdam - German Research Centre for Geosciences (GFZ)  
 Eidgenössische Technische Hochschule Zürich (ETH)  
 Institut de Physique du Globe de Paris (IPGP)  
 The Swedish Institute of Space Physics (IRF)  
 Laboratoire d'électronique des technologies de l'information (Leti)  
 University of Calgary (UoC)  
 Aerospace Research And Test Establishment (VZLU)  
  
 with additional contributions from  
  
 NASA Goddard Space Flight Center (GSFC)  
 University of Colorado (CIRES)  
 Charles University Prague (CUP)

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## Record of Changes

| Reason          | Description                  | Rev | Date       |
|-----------------|------------------------------|-----|------------|
| Initial release | Initial version of document. | 1dA | 2014-06-30 |



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**Table of TBDs**None

## 1 Introduction

### 1.1 Scope and applicability

This document is a constituent of the Design Definition file and is provided in response to an Action Item from the Swarm Quality Working Group meeting in Copenhagen 2014-06-18 to provide an updated set of transformations from the VFM vector magnetometer sensor frame to the STR Star Tracker common reference frame for all three Swarm spacecrafts. Within the scientific community these transformations are often described by sets of Euler angles and are often simply referred to as "*The Euler Angles of Swarm*".

## 2 Applicable and Reference Documentation

### 2.1 Applicable Documents

The following documents are applicable to the definitions within this document.

[AD-1] RFQ/3-13759/12/I-NB, Request For Quotation

[AD-2] SWAM-GSEG-EOPG-SW-12-0059, ESL Statement of Work (Appendix 1 of [AD-1])

### 2.2 Reference Documents

None.

### 2.3 Abbreviations

| <b>Acronym<br/>or abbreviation</b> | <b>Description</b>   |
|------------------------------------|--|
| APDF                               | Archiving and Payload Data Facility  |
| Aux                                | Auxiliary  |
| BGS                                | British Geological Survey, GB  |
| CCDB                               | Characterisation and Calibration DataBase  |
| CCN                                | Contract Change Notice   |
| CIRES                              | Cooperative Institute for Research in Environmental Sciences,<br>University of Colorado, Boulder, US |
| CUP                                | Charles University Prague, CZ  |
| DTU                                | Technical University of Denmark, DK  |
| DUT                                | Delft University of Technology, NL   |
| EFI                                | Electrical Field Instrument, including the TII and the LP  |
| ESA                                | European Space Agency  |

| <b>Acronym<br/>or abbreviation</b> | <b>Description</b>   |
|------------------------------------|--|
| ESL                                | Swarm Expert Support Laboratories  |
| ESRIN                              | European Space Research Institute, Frascati, IT  |
| ETH                                | Eidgenössische Technische Hochschule Zürich, CH  |
| GFZ                                | Helmholtz Centre Potsdam - German Research Centre for Geoscience, DE   |
| GSFC                               | NASA Goddard Space Flight Center, US   |
| IGRF                               | International Geomagnetic Reference Field  |
| IOC                                | In Orbit Commissioning   |
| IOCR                               | In Orbit Commissioning Review  |
| IPGP                               | Institut de Physique du Globe de Paris, FR   |
| JIRA                               | Atlassian JIRA internet based tool for tracking issues with server located at DTU<br><a href="https://jira.spacecenter.dk/">https://jira.spacecenter.dk/</a>   |
| L0                                 | Level 0 (satellite data)   |
| L1                                 | Level 1 (satellite data)   |
| L1b                                | Level 1b (satellite data)  |
| MPPF                               | Mission Planning and Performance Facility  |
| NEC                                | Nort-East-Center reference frame   |
| PDGS                               | Payload Data Ground Segment  |
| PP                                 | Prototype Processor  |
| QWG                                | Quality Working Group  |
| SCARF                              | Satellite Constellation Application and Research Facility. Same as L2PS.   |
| STR                                | Star Tracker   |
| SVN                                | SVN Repository with server located at DTU. Presently, the following URLs apply:<br><a href="https://smart-svn.spacecenter.dk/svn/smart/SwarmESL-All">https://smart-svn.spacecenter.dk/svn/smart/SwarmESL-All</a><br><a href="https://smart-svn.spacecenter.dk/svn/smart/SwarmL2">https://smart-svn.spacecenter.dk/svn/smart/SwarmL2</a> (heritage from the L2PS Project) |
| Swarm                              | Constellation of 3 ESA satellites,<br><a href="http://www.esa.int/esaLP/ESA3QZJE43D_LPswarm_0.html">http://www.esa.int/esaLP/ESA3QZJE43D_LPswarm_0.html</a>  |
| TBC                                | To Be Confirmed  |
| TBD                                | To Be Defined  |

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| <b>Acronym<br/>or abbreviation</b> | <b>Description</b>   |
|------------------------------------|--|
| TDS                                | Test Data Set  |
| UoC                                | University of Calgary (CA)   |
| VFM                                | Vector Field Magnetometer  |
| VZLU                               | Výzkumný a zkušební letecký ústav, or Aerospace Research And Test Establishment (CZ) |

### 3 CCDB Update Summary

The proposed updates of the Swarm CCDB auxiliary files are given in the following tables. The justification of the updates is given in Section 4.

**Table 3-1 Swarm A CCDB Update**

|                                      |   |
|--------------------------------------|---|
| Filename                             | SW_OPER_AUXASW1_C_20000101T000000_9999999T999999_0007.EEF   |
| Complete XPATH or Columns/rows index | TBD   |
| File line                            | 239-242   |
| Tag affected                         | Structure.STR_q_VFM   |
| Field Format                         | Quaternion  |
| Old value                            | <Q1>-0.013315150439779</Q1><br><Q2>0.618889028865068</Q2><br><Q3>0.022648803785932</Q3><br><Q4>0.785038921586876</Q4>   |
| New value                            | <Q1>-0.013231661342904</Q1><br><Q2>0.618887980270184</Q2><br><Q3>0.022658176820283</Q3><br><Q4>0.785040889405373</Q4>   |
| Start validity                       | 20000101T000000   |
| Stop validity                        | 99999999T999999   |
| TDS package name                     | SW-TN-DTU-GS-004_TDS-1:<br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip</a><br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip</a> |
| Note                                 | Ref. SW-TN-DTU-GS-004   |

**Table 3-2 Swarm B CCDB Update**

|                                |   |
|--------------------------------|---|
| Filename                       | SW_OPER_AUXBSW1_C_20000101T000000_9999999T999999_0007.EEF |
| Complete XPATH or Columns/rows | TBD   |

# Swarm Expert Support Laboratories

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|                  |   |
|------------------|---|
| index            |   |
| File line        | 239-242   |
| Tag affected     | Structure.STR_q_VFM   |
| Field Format     | Quaternion  |
| Old value        | <Q1>0.011647432672848</Q1><br><Q2>0.619604649109814</Q2><br><Q3>-0.014720424875213</Q3><br><Q4>0.784689572509491</Q4>   |
| New value        | <Q1>0.011665364843673</Q1><br><Q2>0.619618032648957</Q2><br><Q3>-0.014476629065635</Q3><br><Q4>0.784683273741830</Q4>   |
| Start validity   | 20000101T000000   |
| Stop validity    | 99999999T999999   |
| TDS package name | SW-TN-DTU-GS-004_TDS-1:<br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip</a><br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip</a> |
| Note             | Ref. SW-TN-DTU-GS-004   |

**Table 3-3 Swarm C CCDB Update**

|                                      |   |
|--------------------------------------|---|
| Filename                             | SW_OPER_AUXCSW1_C_20000101T000000_99999999T999999_0007.EEF  |
| Complete XPATH or Columns/rows index | TBD   |
| File line                            | 239-242   |
| Tag affected                         | Structure.STR_q_VFM   |
| Field Format                         | Quaternion  |
| Old value                            | <Q1>-0.001663135699780</Q1><br><Q2>0.621398648445704</Q2><br><Q3>0.003605958231516</Q3><br><Q4>0.783484492989318</Q4> |
| New value                            | <Q1>-0.001666461237559</Q1><br><Q2>0.621375398504043</Q2>   |

|                  |   |
|------------------|---|
|                  | <Q3>0.003700375477998</Q3><br><Q4>0.783502485166580</Q4>  |
| Start validity   | 20000101T000000   |
| Stop validity    | 99999999T999999   |
| TDS package name | SW-TN-DTU-GS-004_TDS-1:<br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test.zip</a><br><a href="ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip">ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip</a> |
| Note             | Ref. SW-TN-DTU-GS-004   |

## 4 Description of Swarm Euler Angle Update

The update of the “Swarm Euler Angles”, i.e. of the transformation from the VFM vector magnetometer sensor frame to the STR Star Tracker Common Reference Frame (CRF), is aimed at improving the accuracy of the Swarm vector magnetic data provided in the North-East-Center (NEC) frame, i.e. of the B\_NECK elements of the Level 1b low-rate magnetic products, MAGX\_LR\_1B. These products are expected to be widely used by the geomagnetic science community for the upcoming International Geomagnetic Reference Field model (IGRF) epoch 2015.

### 4.1 Derivation

The updated VFM → STR transformations are obtained through advanced modelling of Earth’s magnetic field performed by GFZ and DTU independently using Swarm MAGX\_LR\_1B products version 0301 covering the period from launch (2013-11-22) until end of May 2014. The modelling of GFZ also includes a model of the observed discrepancies between the Absolute Scalar Magnetometer (ASM) and VFM readings. Note that this model of the ASM-VFM discrepancies has not been incorporated in the TDS.

The estimated transformations and their deviations with respect to one-another and with respect to the values in CCDB version 0007 (cf. Section 3) are given in Table 4-1.

**Table 4-1 Estimated Transformations and Differences**

| S/C | GFZ   | DTU   | Deviation, arc-sec. |           |           |
|-----|---|---|---------------------|-----------|-----------|
|     |   |   | GFZ-DTU             | GFZ- CCDB | DTU- CCDB |
| A   | -0.013269375978100<br>0.618902374293704<br>0.022669990762100<br>0.785028563985805 | -0.013231661342904<br>0.618887980270184<br>0.022658176820283<br>0.785040889405373 | 18.1                | 21.9      | 34.7      |
| B   | 0.011677752680200<br>0.619629627018087<br>-0.014419179131600<br>0.784674991755783 | 0.011665364843673<br>0.619618032648957<br>-0.014476629065635<br>0.784683273741830 | 24.9                | 125.5     | 101.0     |
| C   | -0.001685485468600<br>0.621383811058280<br>0.003731711833400<br>0.783495623995575 | -0.001666461237559<br>0.621375398504043<br>0.003700375477998<br>0.783502485166580 | 15.8                | 53.2      | 40.8      |

### 4.2 Justification

The estimated transformations listed in Table 4-1 have been applied to Swarm MAGX\_LR\_1B products version 0301 covering the months December 2013 and May 2014 to form the Test Data Set (TDS). The TDS has been analysed by Arnaud Chulliat and Patrick Alken of NOAA and the reports on their findings are enclosed in Annex A. Based on their results and in agreement with GFZ (cf. Annex B), the transformations estimated by DTU are proposed implemented within PDGS.

**Annex A      TDS Analyses**

On the following pages, the analyses by NOAA of the TDS are provided.

# **Analysis of Swarm datasets prepared from revised Euler angles**

Arnaud Chulliat, Univ. Colorado & NOAA/NGDC

2014-06-27

## **Method:**

For each dataset (DTU and GFZnew), MF models were calculated from one month of data and one satellite. Hence a total of 12 models were calculated. Preprocessing of the data included standard data selection for quiet-time and nighttime data; vector data below +/-55 degrees geomagnetic latitude and scalar data at higher latitudes. Crustal (MF7 model) and external (POMME7) models were removed from the data prior to the inversion. MF was calculated until degree 20 and damped with minimum energy norm at the core.

## **Results:**

See Tables 1-2 and Figures 1-3 below.

1. The overall situation is much improved by using the new datasets. There are many more green cells than yellow and red cells in Table 2.
2. The DTU dataset consistently improves the situation for all satellites and epochs. The biggest deterioration for this dataset (in May 2014, satellite B, mean dB\_r residuals) is less than 0.5 nT (Table 2). The average slopes in the residuals vs. colatitude graphs for the Y component are much reduced with respect to the baseline dataset, although not entirely horizontal (Figs. 1-3).
3. The GFZnew dataset consistently improves the situation for satellites A and C, all epochs, although with slightly more yellow cells than the DTU dataset (Table 2). This is also seen in the residuals vs. colatitude graphs in which the average slopes are larger than for the DTU dataset (Figs. 1 and 3).
4. There seems to be a problem with the GFZnew dataset for satellite B, December 2013, as the mean dB\_r and dB\_phi residuals are deteriorated with respect to the baseline dataset (Table 2). This is also prominent in the residuals vs. colatitude graph (Fig. 2). Interestingly, the mean dB\_phi residuals for the DTU dataset are smaller but the difference between December and May (-1.96-1.84=-3.80) is comparable with that for the GFZ dataset (-3.87+0.11=-3.76). This could suggest that the time variation of the Euler angles for that satellite is not negligible.

### Satellite A

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 0.53          | 2.14 | 0.31       | 2.07 | 1.02          | 2.33 |
| dB_theta | 0.37          | 3.61 | 0.37       | 3.65 | 0.35          | 3.60 |
| dB_phi   | 1.33          | 4.73 | -0.93      | 2.92 | -0.41         | 3.62 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.24         | 2.31 | -0.19      | 2.24 | -0.76         | 2.36 |
| dB_theta | 0.30          | 4.67 | 0.34       | 4.56 | 0.34          | 4.60 |
| dB_phi   | 2.98          | 4.51 | 0.74       | 2.66 | 1.27          | 2.94 |

### Satellite B

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 0.05          | 3.38 | 0.51       | 3.11 | 1.05          | 3.22 |
| dB_theta | 0.39          | 4.70 | 0.42       | 4.40 | 0.40          | 4.39 |
| dB_phi   | 3.23          | 6.45 | -1.96      | 3.37 | -3.87         | 5.02 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.15         | 2.29 | -0.61      | 2.20 | -1.09         | 2.39 |
| dB_theta | 0.48          | 4.23 | 0.24       | 4.52 | 0.29          | 4.48 |
| dB_phi   | 2.73          | 6.40 | 1.84       | 3.19 | -0.11         | 2.27 |

### Satellite C

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 1.04          | 2.67 | 0.21       | 2.51 | 0.61          | 2.54 |
| dB_theta | 0.32          | 3.86 | 0.32       | 3.94 | 0.31          | 3.93 |
| dB_phi   | 1.97          | 4.17 | -0.65      | 2.78 | -1.13         | 3.57 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.89         | 2.49 | 0.11       | 2.20 | -0.18         | 2.17 |
| dB_theta | 0.32          | 4.61 | 0.32       | 4.52 | 0.35          | 4.55 |
| dB_phi   | 3.29          | 5.92 | 0.61       | 2.68 | 0.15          | 2.46 |

mean < 1  
1 < mean < 2  
mean > 2

rms < 4  
4 < rms < 5  
rms > 5

Table 1: Mean and rms residuals for each model, with cells colored so as to highlight the largest mean and rms values.

### Satellite A

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 0.53          | 2.14 | 0.31       | 2.07 | 1.02          | 2.33 |
| dB_theta | 0.37          | 3.61 | 0.37       | 3.65 | 0.35          | 3.60 |
| dB_phi   | 1.33          | 4.73 | -0.93      | 2.92 | -0.41         | 3.62 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.24         | 2.31 | -0.19      | 2.24 | -0.76         | 2.36 |
| dB_theta | 0.30          | 4.67 | 0.34       | 4.56 | 0.34          | 4.60 |
| dB_phi   | 2.98          | 4.51 | 0.74       | 2.66 | 1.27          | 2.94 |

### Satellite B

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 0.05          | 3.38 | 0.51       | 3.11 | 1.05          | 3.22 |
| dB_theta | 0.39          | 4.70 | 0.42       | 4.40 | 0.40          | 4.39 |
| dB_phi   | 3.23          | 6.45 | -1.96      | 3.37 | -3.87         | 5.02 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.15         | 2.29 | -0.61      | 2.20 | -1.09         | 2.39 |
| dB_theta | 0.48          | 4.23 | 0.24       | 4.52 | 0.29          | 4.48 |
| dB_phi   | 2.73          | 6.40 | 1.84       | 3.19 | -0.11         | 2.27 |

### Satellite C

| Dec 2013 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | 1.04          | 2.67 | 0.21       | 2.51 | 0.61          | 2.54 |
| dB_theta | 0.32          | 3.86 | 0.32       | 3.94 | 0.31          | 3.93 |
| dB_phi   | 1.97          | 4.17 | -0.65      | 2.78 | -1.13         | 3.57 |

| May 2014 | 0301 baseline |      | DTU angles |      | GFZnew angles |      |
|----------|---------------|------|------------|------|---------------|------|
|          | mean          | rms  | mean       | rms  | mean          | rms  |
| dB_r     | -0.89         | 2.49 | 0.11       | 2.20 | -0.18         | 2.17 |
| dB_theta | 0.32          | 4.61 | 0.32       | 4.52 | 0.35          | 4.55 |
| dB_phi   | 3.29          | 5.92 | 0.61       | 2.68 | 0.15          | 2.46 |

|                  |
|------------------|
| improvement      |
| worsening < 1 nT |
| worsening > 1 nT |

Table 2: Same as Table 1, but with cells colored so as to highlight when the new Euler angles lead to an improvement or a worsening of the mean and rms residuals.

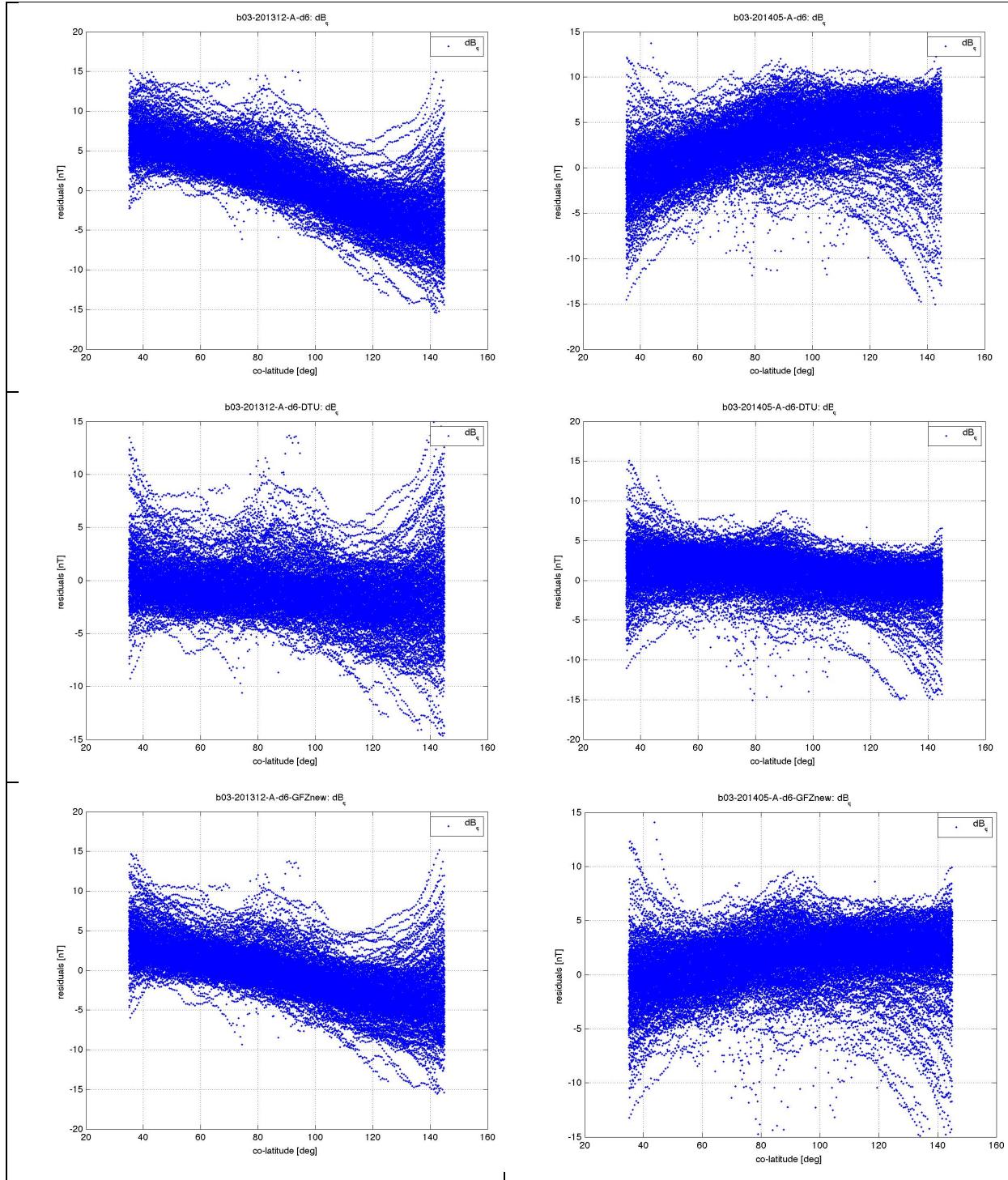


Figure 1:  $B_\phi$  (Y) residuals, satellite A, for December 2013 (left) and May 2014 (right), and for baseline (top), DTU (middle) and GFZnew (bottom) datasets.

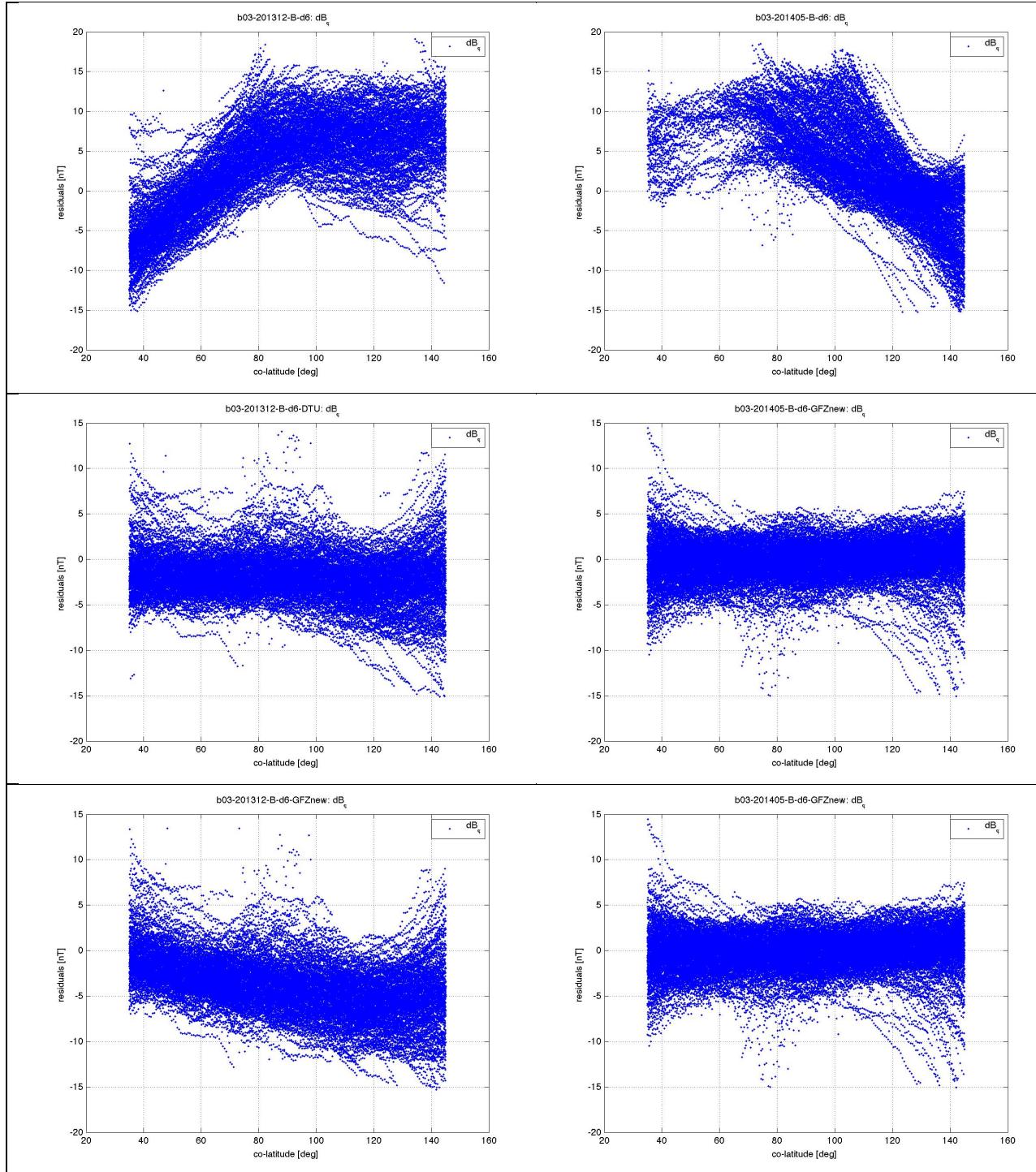


Figure 2:  $B_\phi$  (Y) residuals, satellite B, for December 2013 (left) and May 2014 (right), and for baseline (top), DTU (middle) and GFZnew (bottom) datasets.

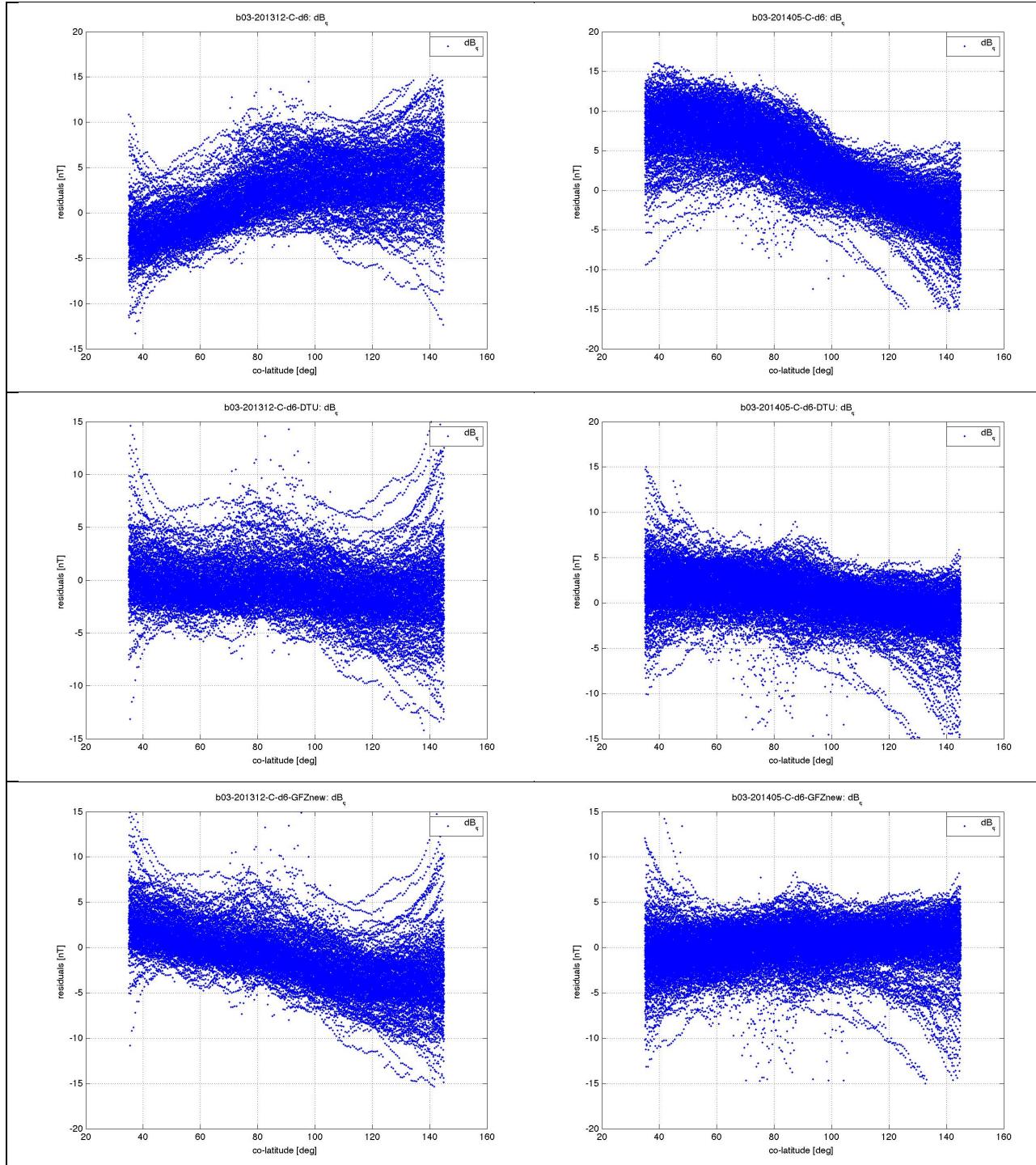


Figure 3:  $B_\phi$  (Y) residuals, satellite C, for December 2013 (left) and May 2014 (right), and for baseline (top), DTU (middle) and GFZnew (bottom) datasets.

## **Summary**

27 June 2014

Patrick Alken

NGDC/NOAA Boulder, CO, USA

To analyze the Euler angle results provided by DTU and GFZ, I've constructed main field models for Swarm A,B,C using the DTU and GFZ datasets. In both datasets, there is drastic improvement over the 0301 baseline in the X and Y NEC components.

The models were constructed to spherical harmonic degree 15, with secular variation to degree 8. The POMME-7 external field was subtracted from the data prior to fitting, and a simple daily ring current field aligned with the internal dipole was coestimated to account for errors in POMME.

I made 3 sets of models. The first uses data only in December 2013, the second uses data in May 2014, and the third combines the two datasets. In the tables below, I provide the rms values for the residuals in X, Y, Z (NEC frame). The color scheme is as follows. If a model based on one set of Euler angles has a lower rms than the same model built from the other set of Euler angles, it is shown in green. Otherwise, it is shown in red. Therefore, when comparing the DTU and GFZ results below, green indicates a better residual distribution.

Generally speaking, I don't find a large difference between the two (ie: sometimes the GFZ dataset gives a lower rms, and sometimes the DTU dataset has a lower rms). In many cases, the rms values between the two datasets are extremely close, though DTU does have (slightly) more green cells than GFZ in the tables below.

For the B satellite in December, both the DTU and GFZ angles give slightly larger rms values for each component, however the GFZ rms is significantly higher in the Y component.

Both datasets exhibit latitudinal dependence in the Y residuals (see the residual plots). I have plotted the residuals only for the DTU dataset, but the GFZ residuals look similar. In both cases, the Y residuals have a clear linear change with respect to latitude, while the X and Z are fairly flat.

My main conclusion is this:

***Both DTU and GFZ angles are a huge improvement over the 0301 baseline. Both DTU and GFZ datasets exhibit a linear latitudinal dependence in Y whose origin is unknown. I am unable to state that either dataset is clearly superior to the other, though DTU has more green cells in the tables below indicating slightly lower rms residual values overall, but these rms differences are generally extremely small.***

## **Residual rms**

### **Swarm A**

#### **DTU**

| <b>Component</b> | <b>December</b> | <b>May</b> | <b>Combined</b> |
|------------------|-----------------|------------|-----------------|
| X                | 3.76            | 4.68       | 4.26            |

|   |      |      |      |
|---|------|------|------|
| Y | 3.54 | 3.53 | 3.57 |
| Z | 2.25 | 2.87 | 2.54 |

### GFZ (new angles)

| Component | December | May  | Combined |
|-----------|----------|------|----------|
| X         | 3.72     | 4.69 | 4.25     |
| Y         | 4.27     | 3.56 | 3.99     |
| Z         | 2.25     | 2.88 | 2.58     |

### **Swarm B**

#### DTU

| Component | December | May  | Combined |
|-----------|----------|------|----------|
| X         | 5.44     | 4.67 | 5.12     |
| Y         | 4.03     | 3.93 | 4.01     |
| Z         | 3.96     | 2.73 | 3.41     |

### GFZ (new angles)

| Component | December | May  | Combined |
|-----------|----------|------|----------|
| X         | 5.55     | 4.64 | 5.16     |
| Y         | 5.61     | 3.28 | 4.62     |
| Z         | 3.98     | 2.69 | 3.46     |

### **Swarm C**

#### DTU

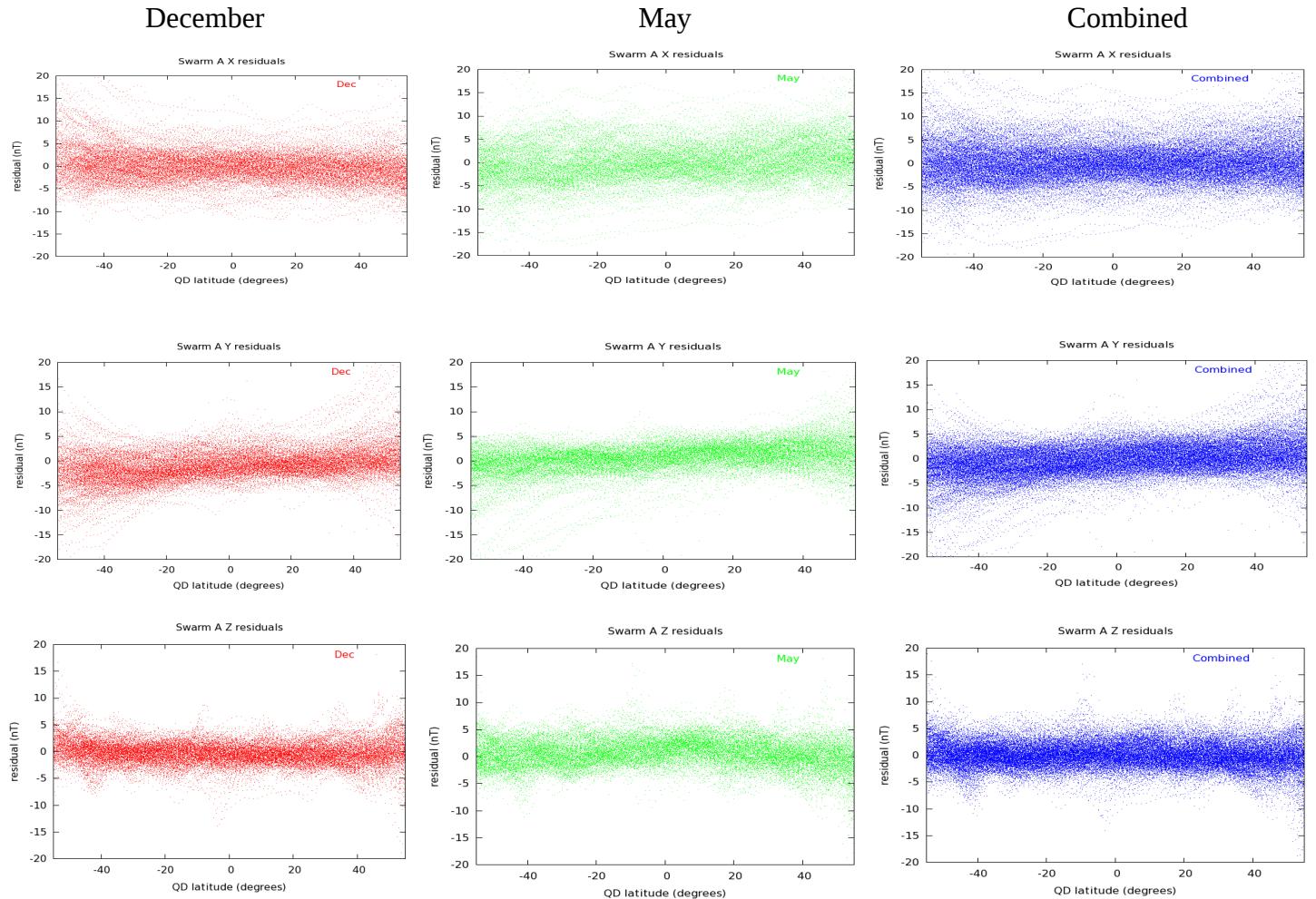
| Component | December | May  | Combined |
|-----------|----------|------|----------|
| X         | 4.59     | 4.55 | 4.64     |
| Y         | 3.19     | 3.63 | 3.46     |
| Z         | 3.33     | 2.82 | 3.08     |

### GFZ (new angles)

| Component | December | May  | Combined |
|-----------|----------|------|----------|
| X         | 4.62     | 4.56 | 4.65     |
| Y         | 4.03     | 3.37 | 3.74     |
| Z         | 3.31     | 2.79 | 3.08     |

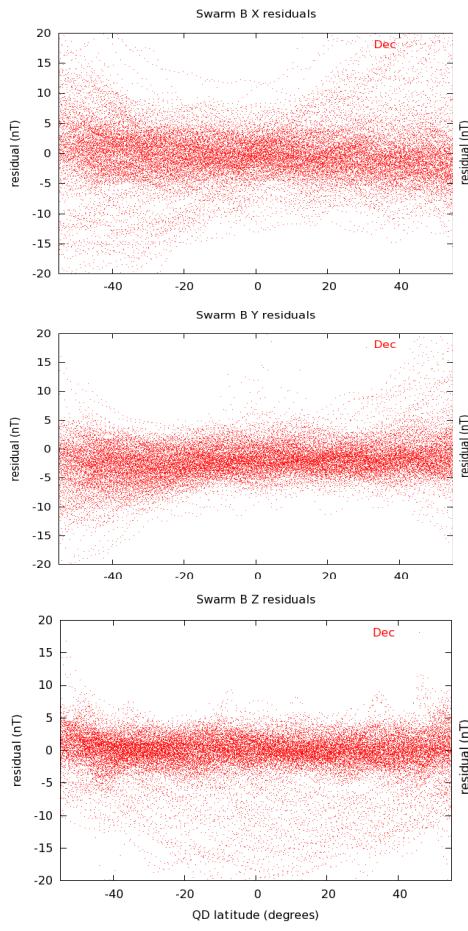
## Residual plots (DTU)

### Swarm A

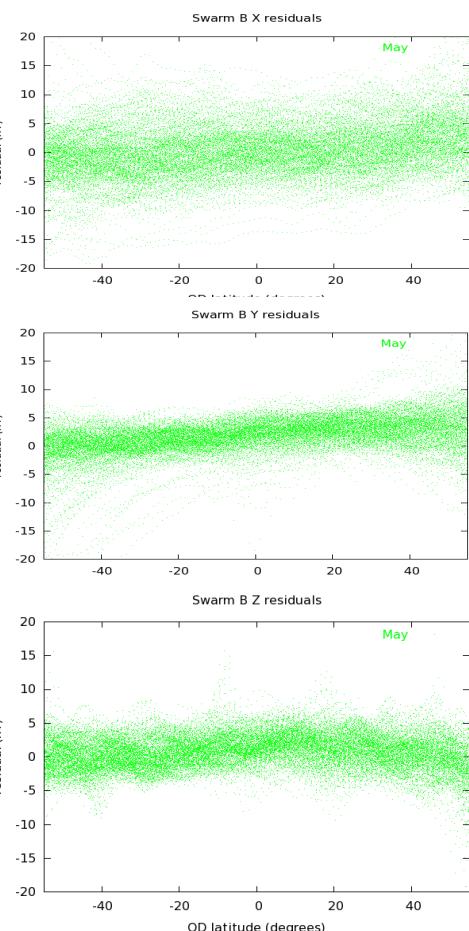


## Swarm B

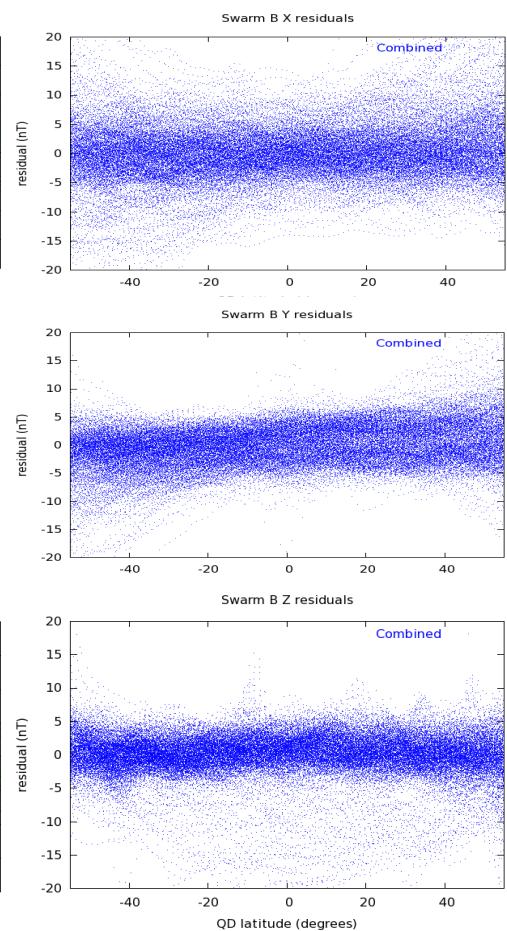
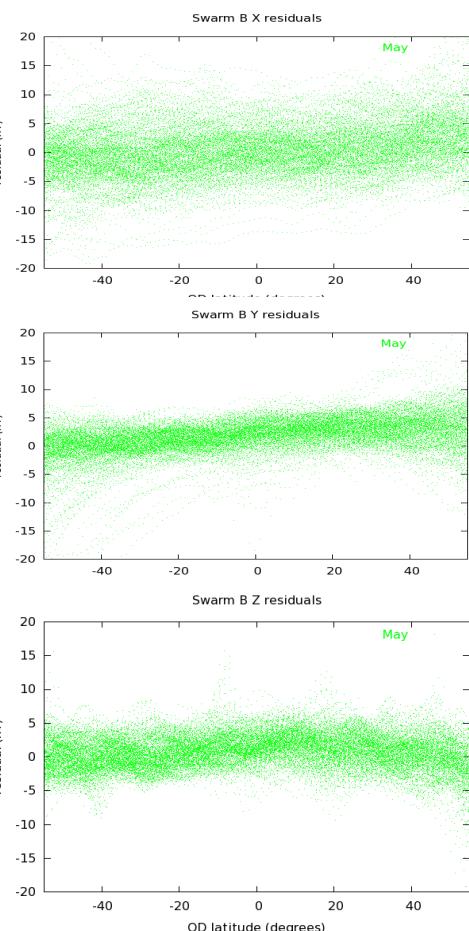
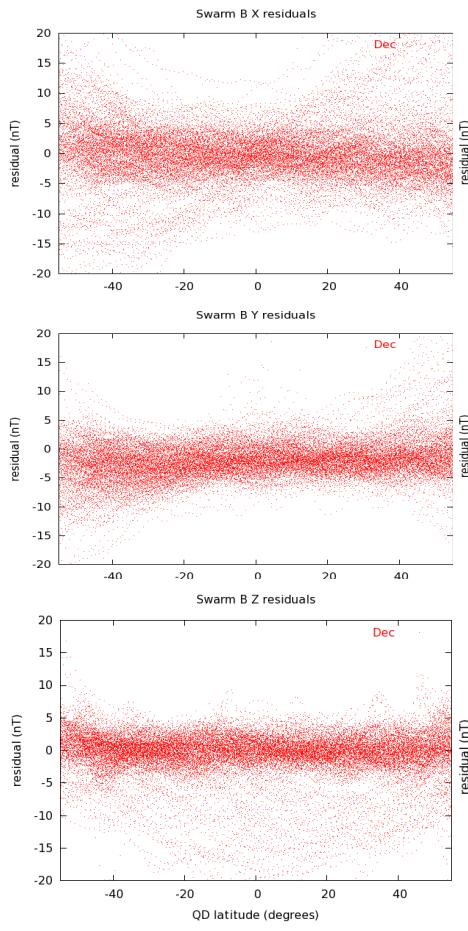
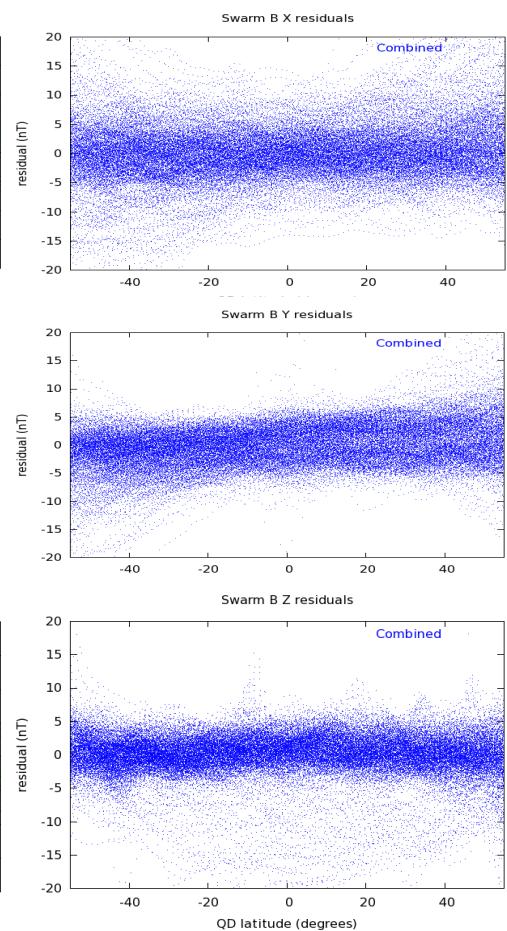
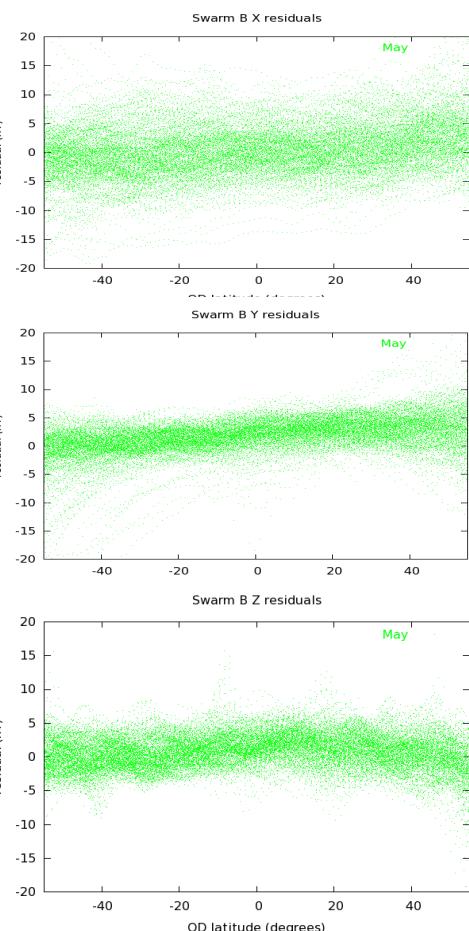
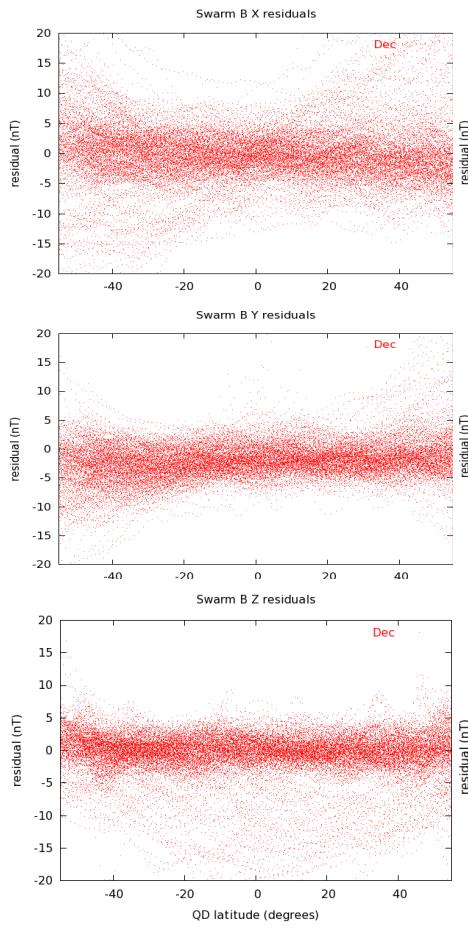
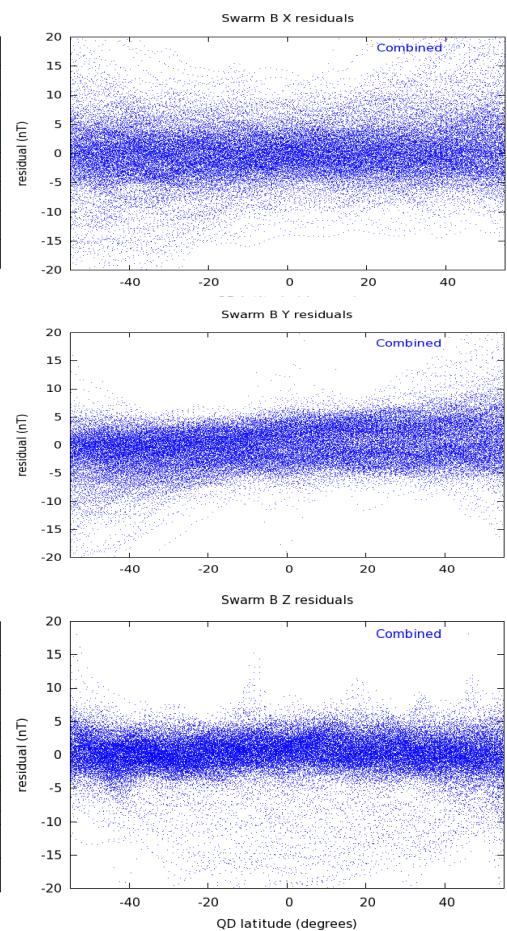
December



May

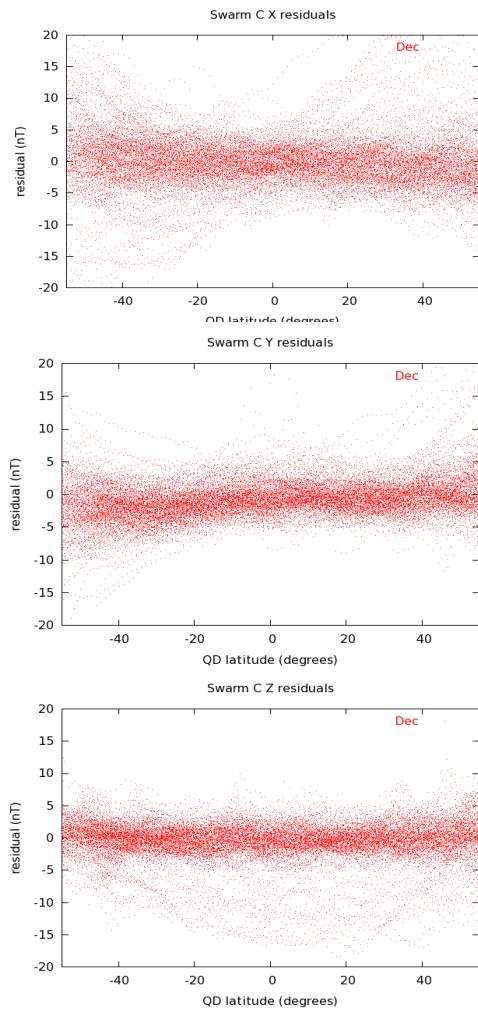


Combined

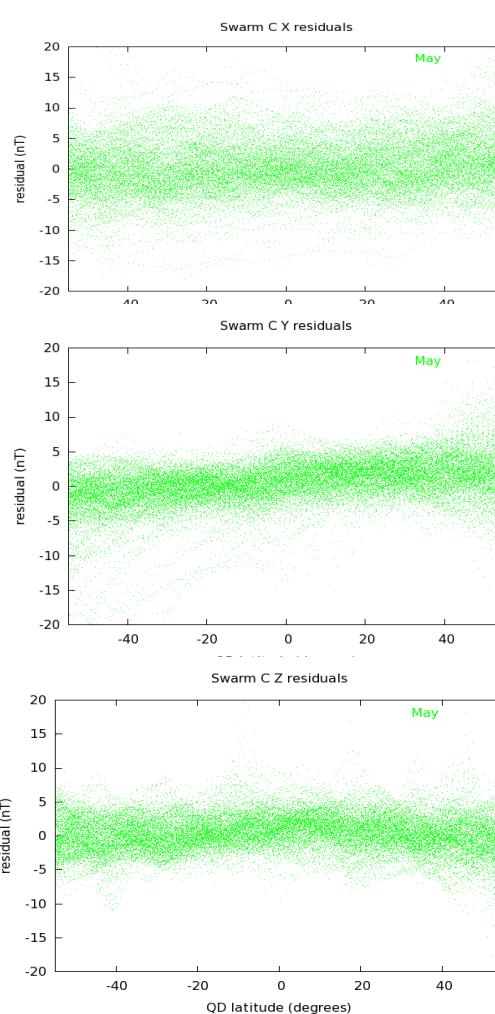


# Swarm C

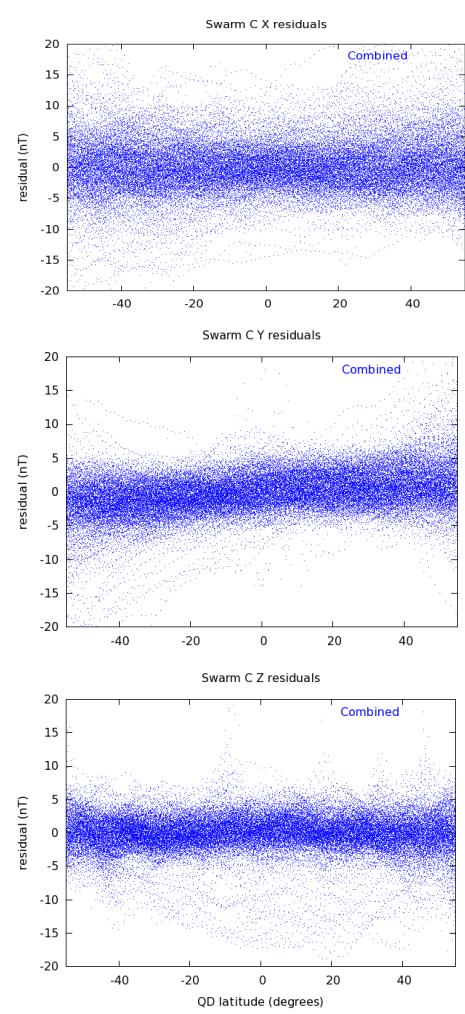
December



May



Combined



**Annex B      Answer from Vincent Lesur, GFZ**

**Subject:** Re: delays in Euler angles processing

**From:** Vincent Lesur <[lesur@gfz-potsdam.de](mailto:lesur@gfz-potsdam.de)>

**Date:** 30-06-2014 09:26

**To:** Arnaud Chulliat - NOAA Affiliate <[arnaud.chulliat@noaa.gov](mailto:arnaud.chulliat@noaa.gov)>

**CC:** Lars Tøffner-Clausen <[lastec@space.dtu.dk](mailto:lastec@space.dtu.dk)>, Nils Olsen <[nio@space.dtu.dk](mailto:nio@space.dtu.dk)>, Chris Finlay

<[cfinlay@space.dtu.dk](mailto:cfinlay@space.dtu.dk)>, Patrick Alken <[patrick.alken@noaa.gov](mailto:patrick.alken@noaa.gov)>, "Martin K.A. Rother"

<[rother@gfz-potsdam.de](mailto:rother@gfz-potsdam.de)>, Gauthier Hulot <[gh@ipgp.fr](mailto:gh@ipgp.fr)>

Dear All,

I looked at Arnaud and Patrick's comments and I think it is very encouraging that the analysis gives similar results. The Euler angle values we sent were based on a data set that has been corrected for a perturbation vector estimated from the ASM/VFM scalar differences. It is therefore not a surprise if the Euler angles we provided are not optimum when used with an un-corrected data set.

However, we have not been able to test if our perturbation vector estimates are valid. This is a work to be done with IPGP. In view of the results, and aware of possible difficulties with our perturbation vector estimates, I would recommend that we use DTU Euler angles data sets to process the next version of Swarm data.

Best regards

Vincent

On 28 Jun 2014, at 02:00, Arnaud Chulliat - NOAA Affiliate <[arnaud.chulliat@noaa.gov](mailto:arnaud.chulliat@noaa.gov)> wrote:

Dear Lars,

Attached are the results of two independent analysis by Patrick and myself of the new "DTU" and "GFZnew" datasets. We note a very significant improvement of the residuals when using either dataset, but there are differences between the two datasets. Overall, the DTU angles give slightly better results, especially for satellite B. Please let us know if you would like us to do other calculations and/or provide other information about our results.

Best regards and have a great week-end!

Arnaud

On Fri, Jun 27, 2014 at 5:26 AM, Lars Tøffner-Clausen <[lastec@space.dtu.dk](mailto:lastec@space.dtu.dk)> wrote:

Dear Arnaud

I have now received the new Euler angles from GFZ and uploaded new data to  
[ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b\\_Euler\\_Test2.zip](ftp://ftp.space.dtu.dk/data/magnetic-satellites/Swarm/SCARF/Test/L1b_Euler_Test2.zip).

Below, I have listed some numbers (as in my previous mail). Please note: GFZ has corrected the vector measurements using Vincent's model of the stray field. This correction has not