

# 30552 – Lecture 11.

## Advanced Satellite altimetry. In-SAR for Elevation and Icesat-2 for Bathymetry

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**DTU Space,**  
**Geodesy and Earth Observation**

DTU Space  
National Space Institute

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$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$
$$\int_a^b \varepsilon \Theta^{\sqrt{17}} + \Omega \int \delta e^{i\pi} = \{2.7182818284\}$$
$$\chi^2 \sum ! >$$



# Before we start:

If you feel ill, go home

Keep your distance to others

Wash or sanitize your hands

Disinfect table and chair

Respect guidelines and restrictions

# Invitation for virtual S6 launch event

## S6\_Invitation\_Virtual.pdf Under fileshare



### sentinel-6 michael freilich

CHARTING SEA LEVEL  
FOR COPERNICUS



ONLINE  
EVENT

ESA, the European Commission and EUMETSAT have the pleasure of inviting you to follow the launch of Copernicus Sentinel-6 Michael Freilich, the latest of the Sentinel satellites of the Copernicus programme on **21 November 2020 | 18:17 CET**

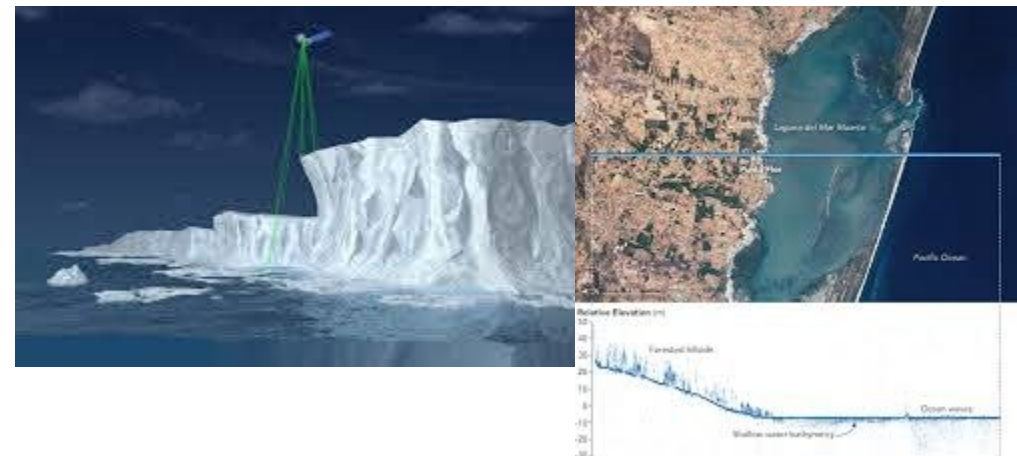
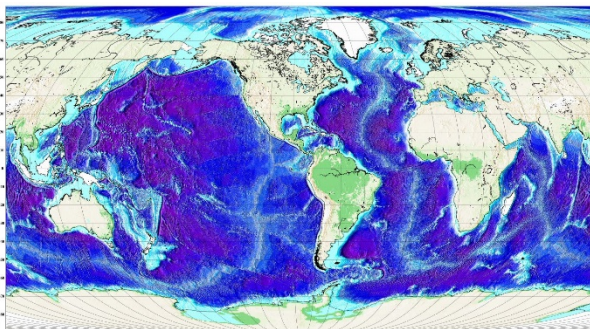
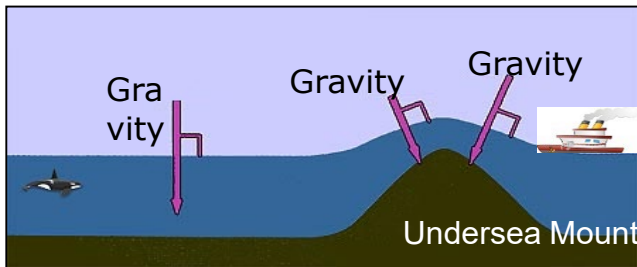
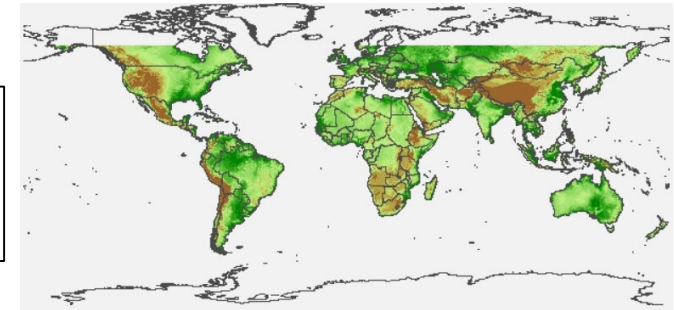
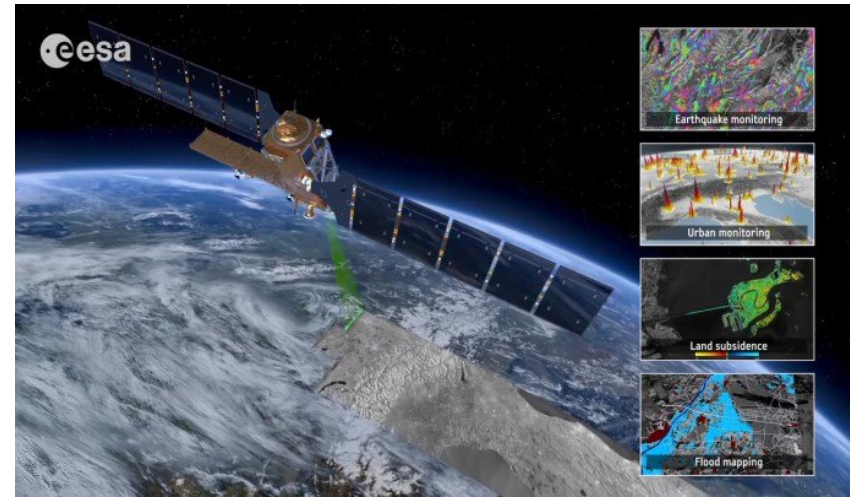
Streamed by ESA Web TV <https://esawebtv.esa.int>

The ESA Web TV programme will start at 17:45 CET

Any change in the launch date and time will be announced on our website: [www.esa.int/sentinel-6](http://www.esa.int/sentinel-6) and via ESA Facebook or via Twitter @esa\_eo | @esaoperations

# Figure of the Earth.

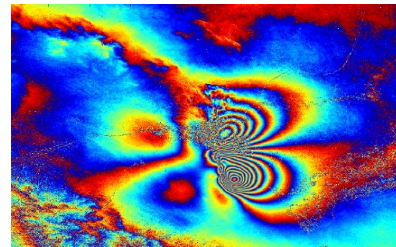
- Lecture 8.
- Bathymetry in the deep Ocean
- (gravity inversion)
- Today. IN-SAR for topography
- Laser altimetry for coastal bathymetry



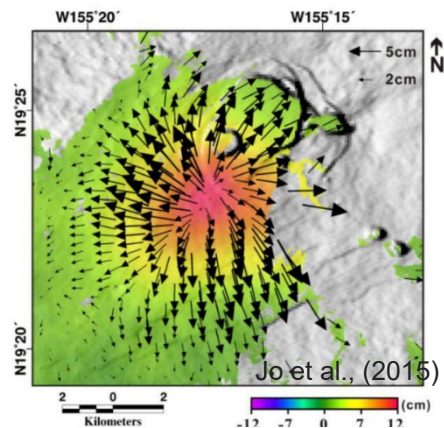
**Seeber (2003): SAR does not belong to satellite geodesy, but is usually treated within "remote sensing" - well times are changing.....**

## Motion -> Geodesy

Large displacements /  
fast motion

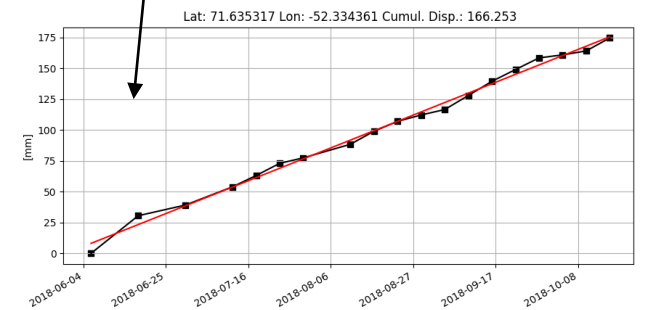
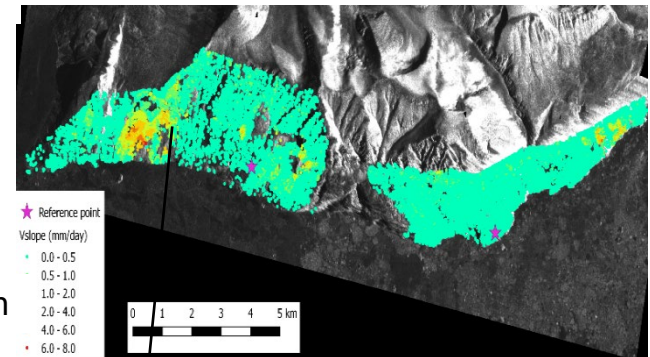


2003 Bam earthquake, Iran



Kilauea volcano, Hawaii

Slow deformations



Karrat fjord, Greenland. Downslope deformation time-series.

- **Synthetic Aperture Radar (SAR).**
  - “Synthetic Aperture”
  - Azimuth and range accuracy
  - SAR and INSAR systems/satellites.

## **Interferometric SAR (INSAR)**

**Observation principle**

**Height accuracy**

**Data and Software**

## **Differential INSAR (DINSAR)**

**Deformation accuracy**

**Multiple INSAR and Persistent Scatterer and geodesy**

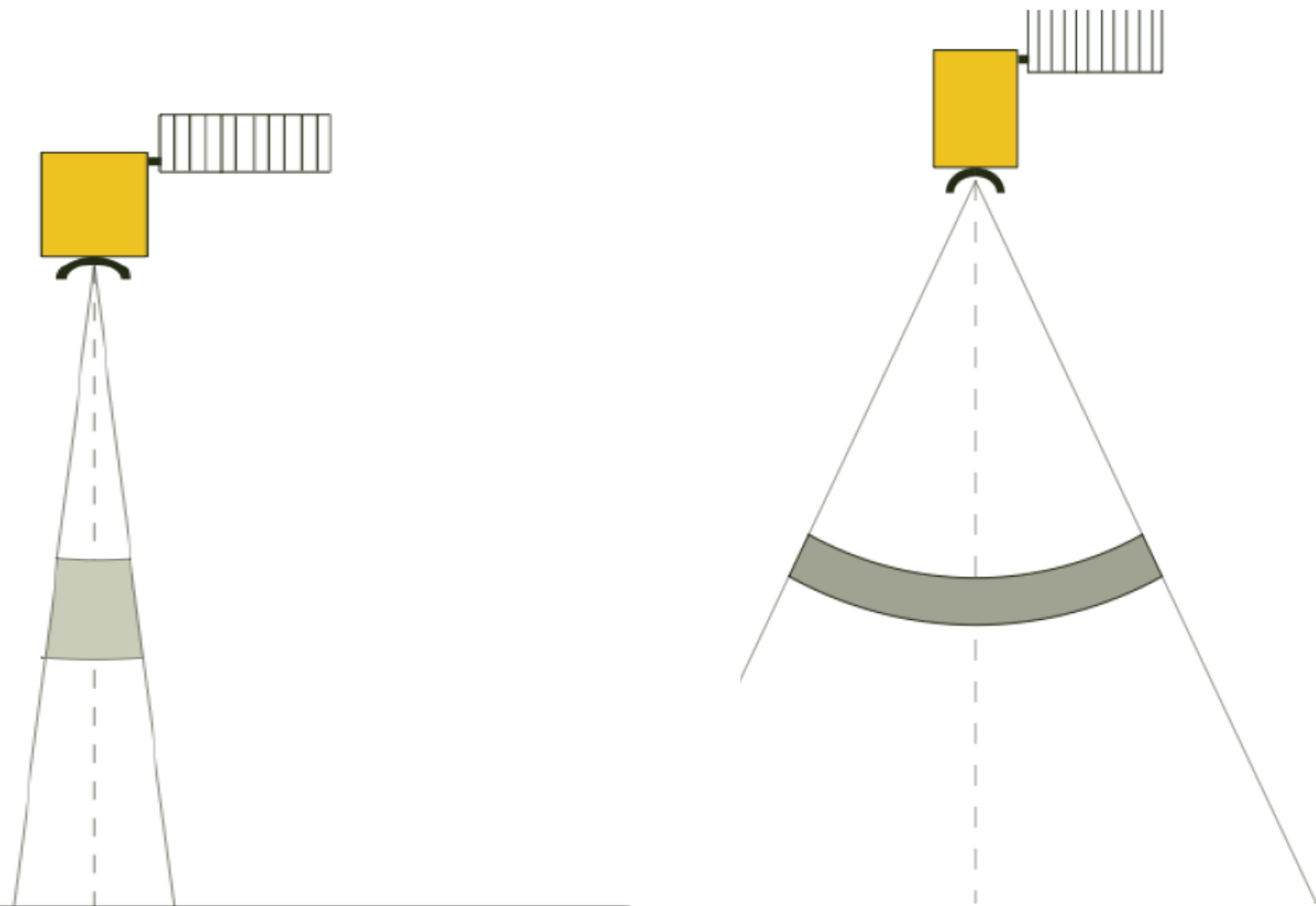
## **Next Generation altimeter**

**Surface water and Ocean topography. SWOT**

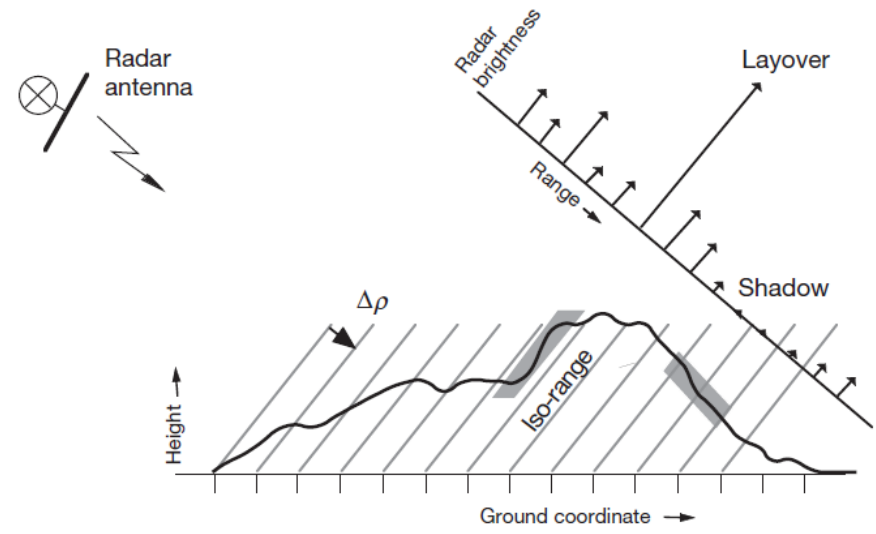
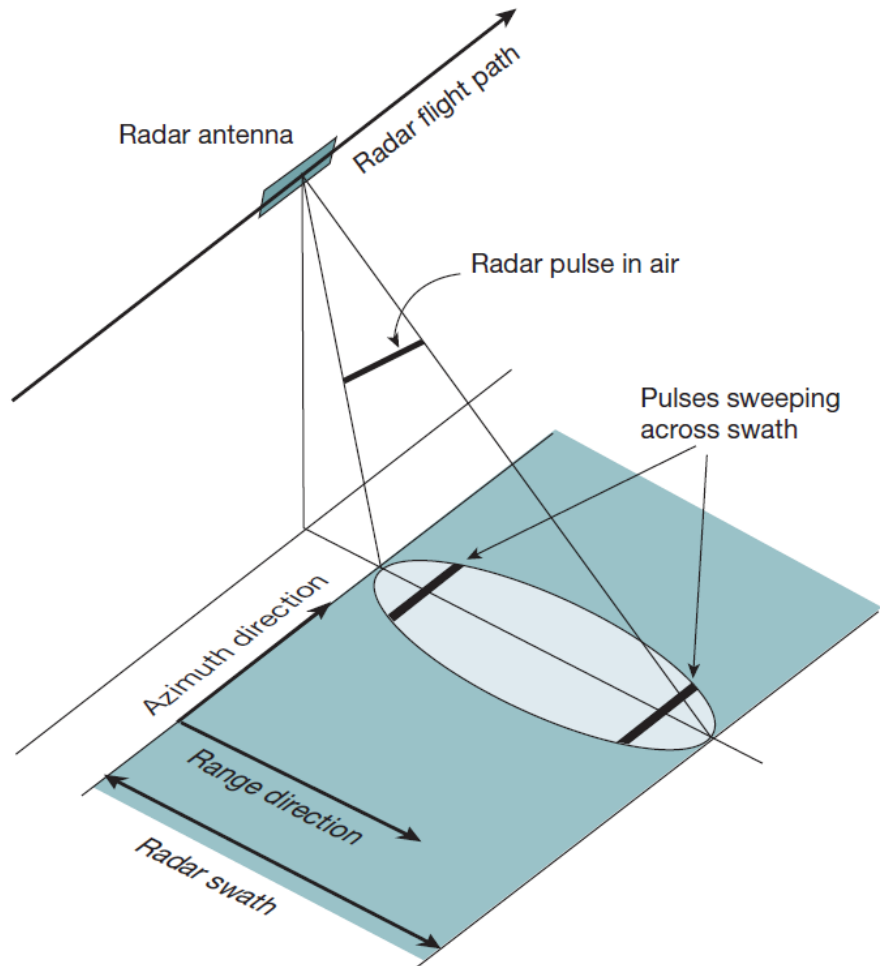
## **Laser Altimetry for Bathymetry (Heidi Ranndal).**

**Acknowledging teaching material supplied by John Merryman Baconi (Measurement tech)  
Henning Skriver and Le Lueng Fu (NASA)**

# Beam limited (along) Pulse limited (across)



# SAR receiver detects time and power/backscatter





# Azimuth and Range resolution

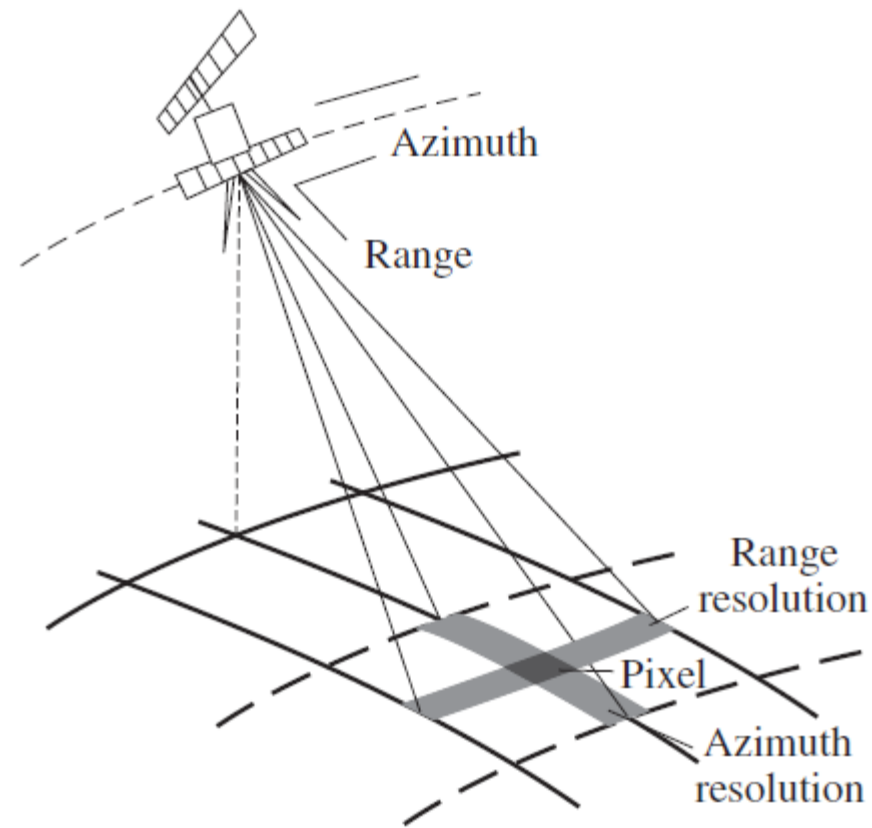
- Azimuth resolution (Seeber 11.1)  $\epsilon \approx \frac{\lambda}{d}$

with

$\epsilon$  resolution, (actually beam width)

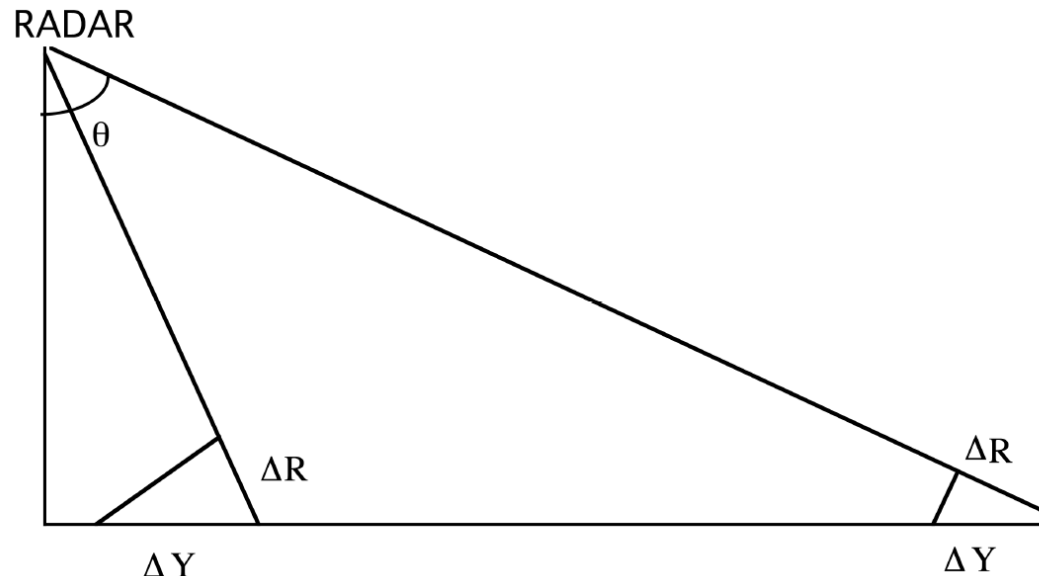
$\lambda$  wavelength of the particular radiation, and  
 $d$  telescope diameter.

- 100 m resolution requires  $d > 100$  meters
- Range resolution (pulse) (H. Skrive



$$\Delta Y = \frac{\Delta R}{\sin \theta}$$

$$\Delta R_{range} = \frac{1}{2} c T$$



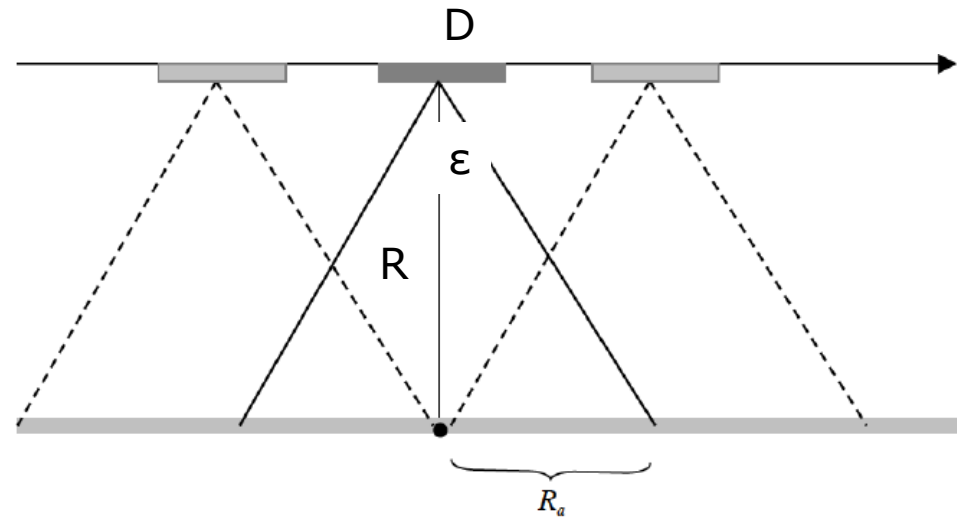
# Synthetic Aperture.

Azimuthal resolution

$$\epsilon = \lambda / D$$

$$R_a = R \tan(\epsilon) = R \epsilon$$

$$R_a = R \lambda / D$$



Length of illumination is  $2 R_a$

Assuming that scatterer remains stationary while satellite passage.

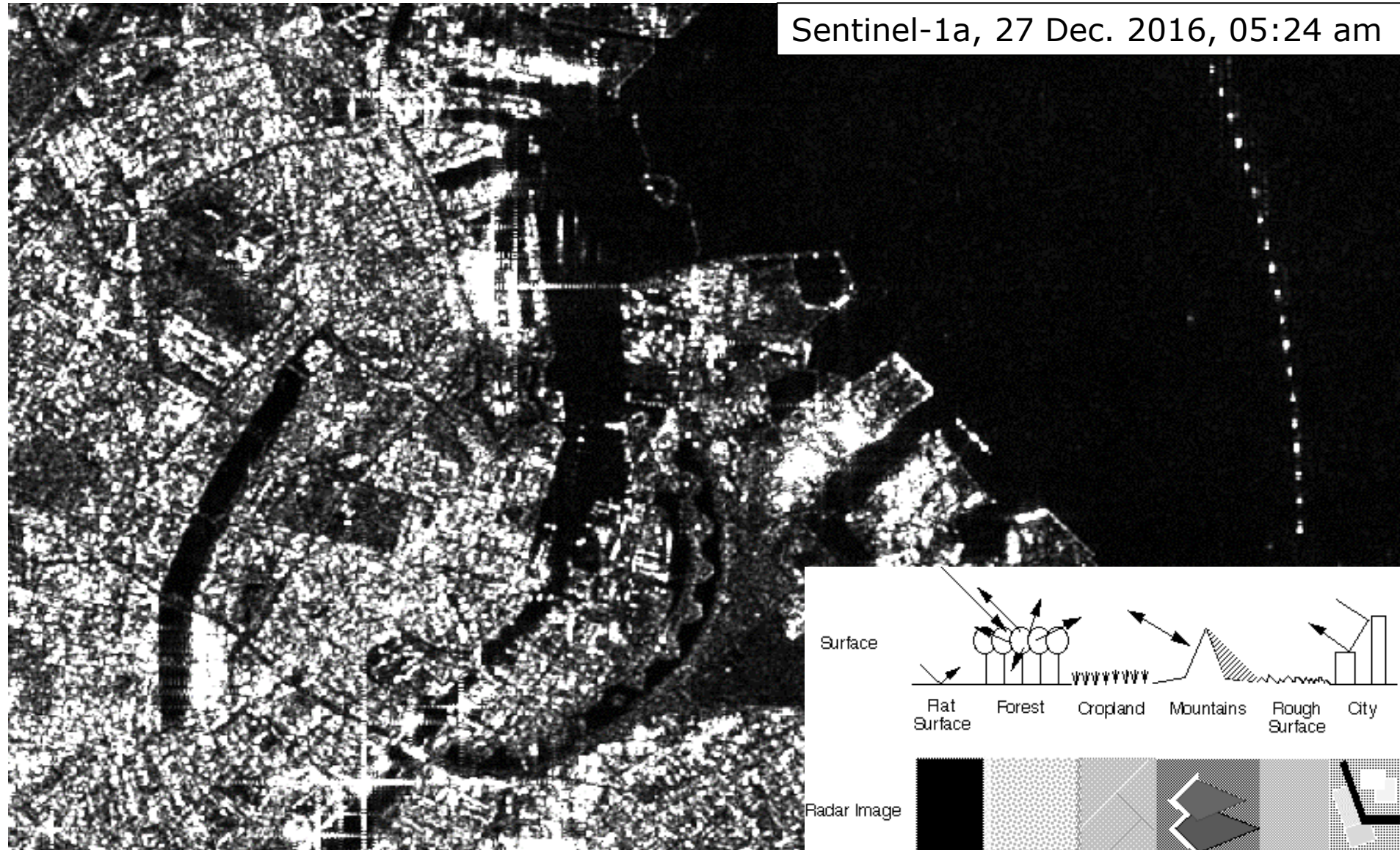
“Synthetic Aperture” becomes equal to  $2 R_a$ .

Hence  $R_a^* = D / 2$

Observations from different “bursts” are separated using Delay Doppler.

# SAR image amplitude

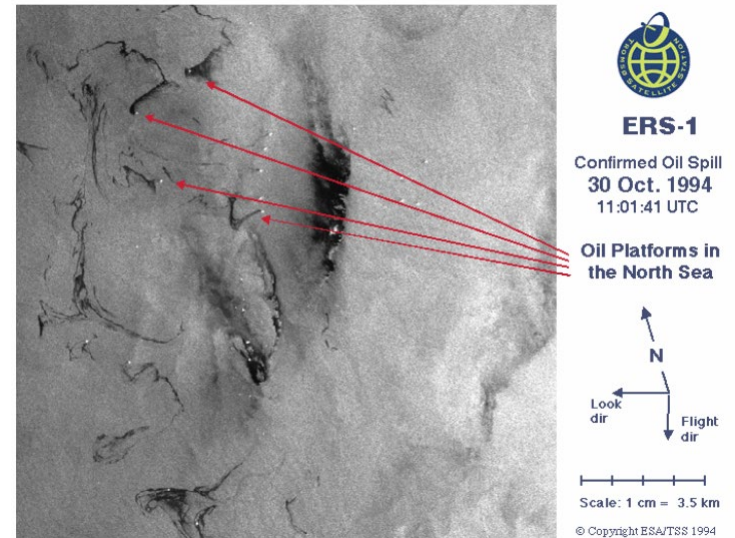
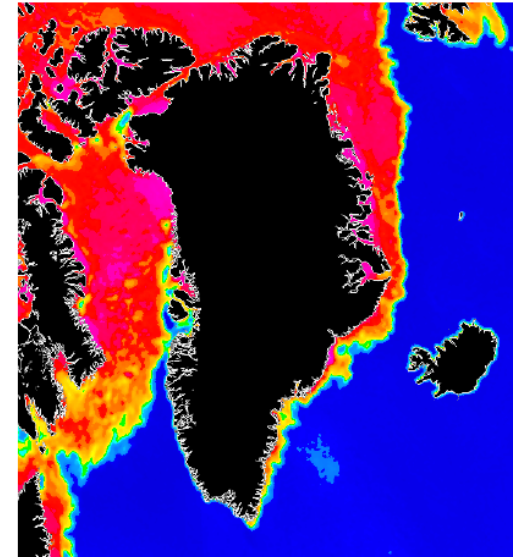
Sentinel-1a, 27 Dec. 2016, 05:24 am



# Danjaj Longfors Berg (Masters projekt)

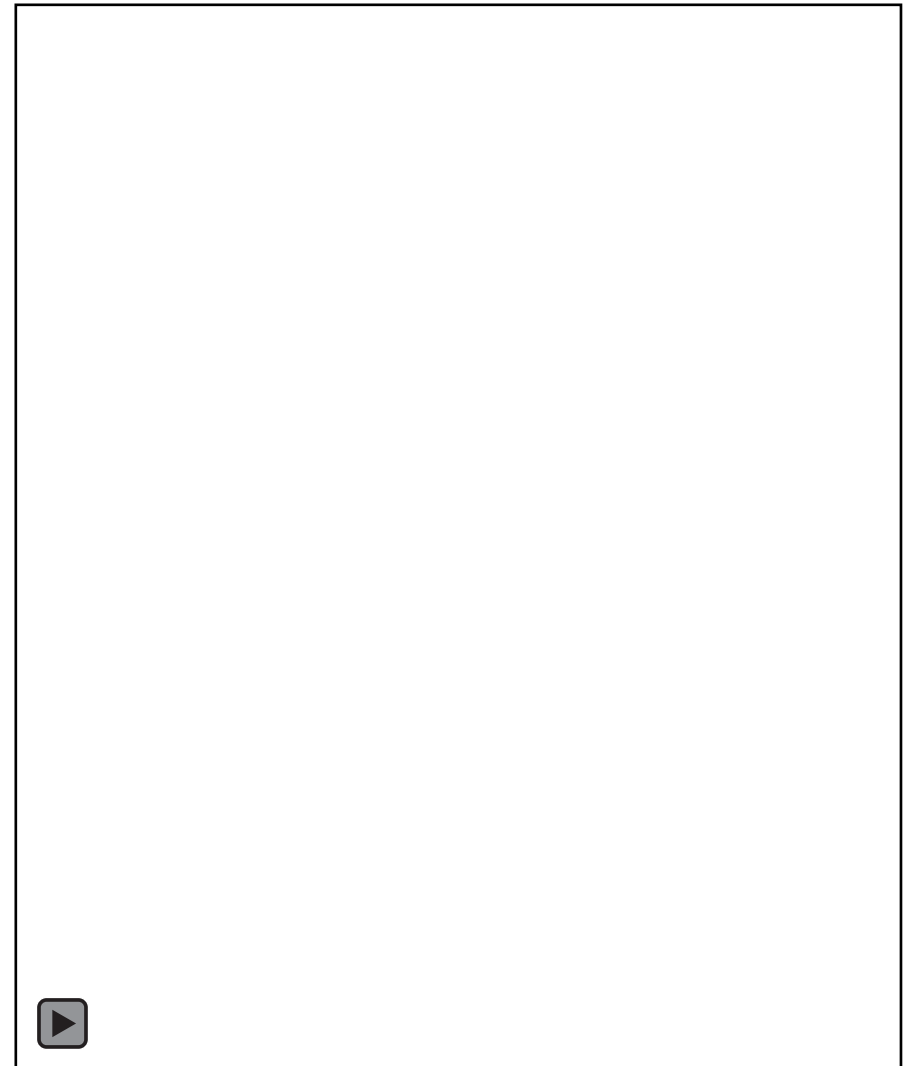
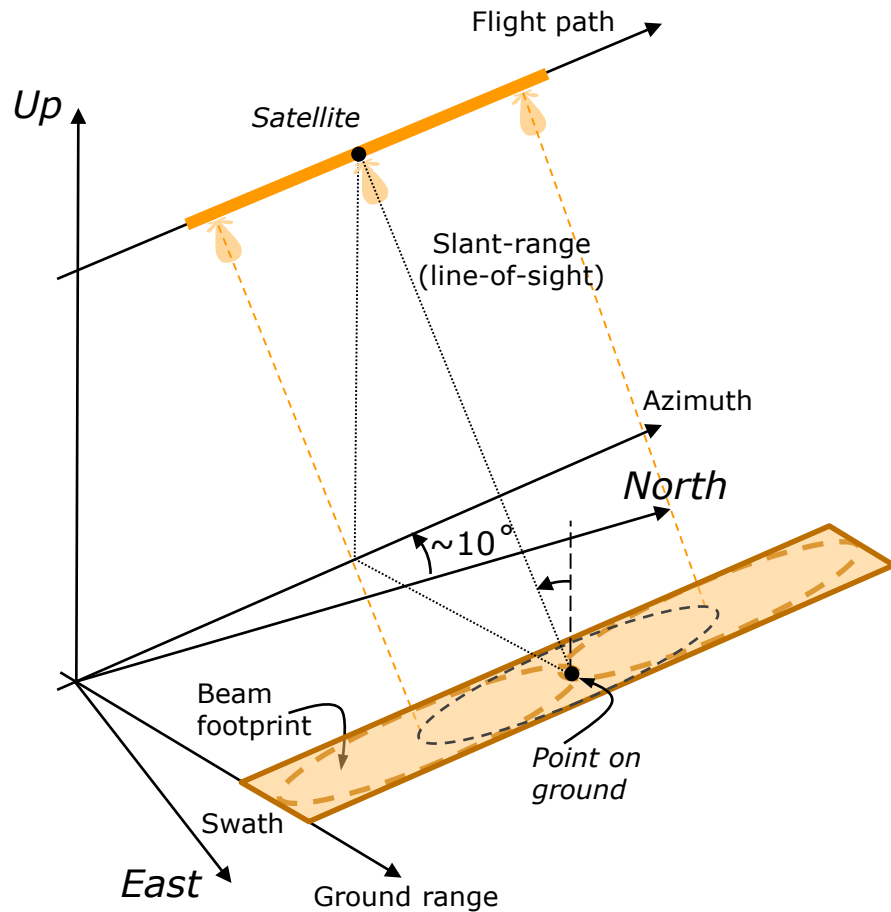
- Ship and Iceberg detection in Sentinel-1
- using Deep Learning (Heisenberg and Andersen).

AMSR2 (JAXA)  
All Arctic in NRT



Seice.dk : State of the art SAR archive.

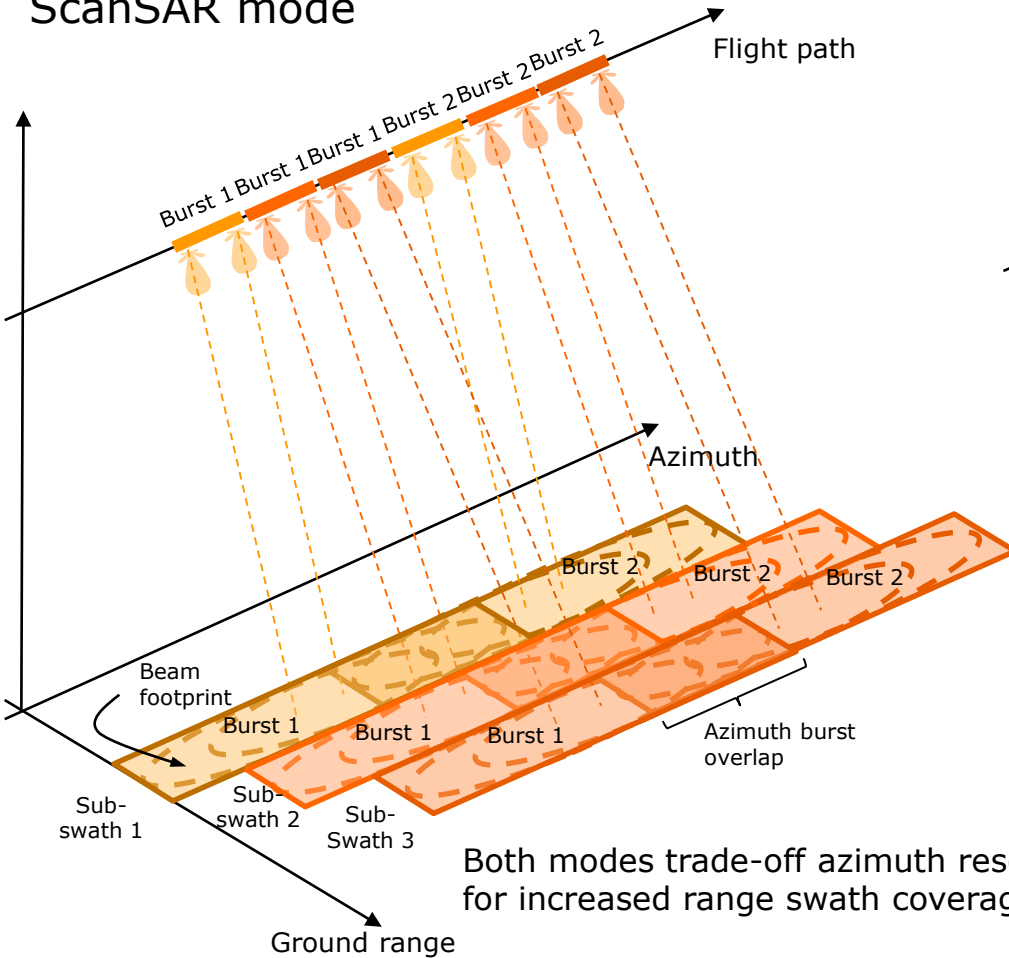
# SAR acquisition geometry and orbits



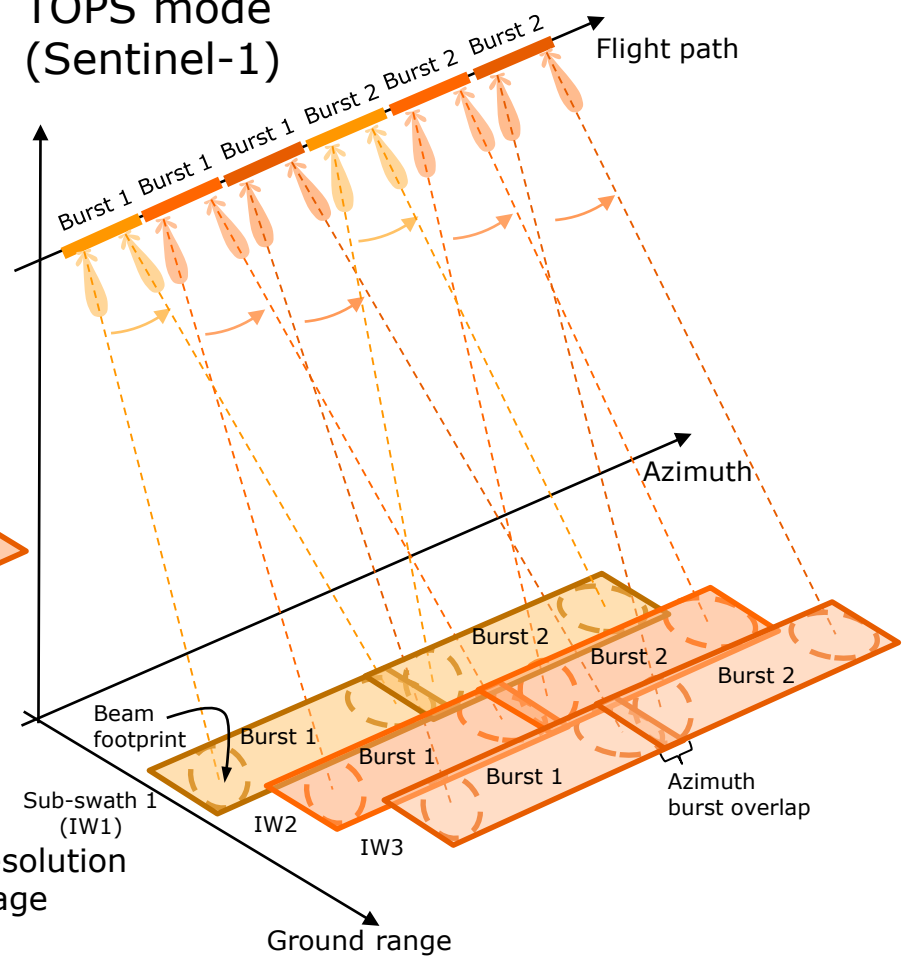
Example: Stripmap acquisition mode, ascending orbit

# Wide-area acquisition modes

ScanSAR mode



TOPS mode (Sentinel-1)



Both modes trade-off azimuth resolution for increased range swath coverage

ESA TOPS animation: [https://www.esa.int/esatv/Videos/2014/03/Sentinel-1\\_Radar\\_mission/SAR\\_scanning\\_animations\\_ESA\\_2013](https://www.esa.int/esatv/Videos/2014/03/Sentinel-1_Radar_mission/SAR_scanning_animations_ESA_2013)

## Different SAR systems uses different wavelength ( $\lambda$ ).

Different wavelength or frequencies have different characteristics /advantages.

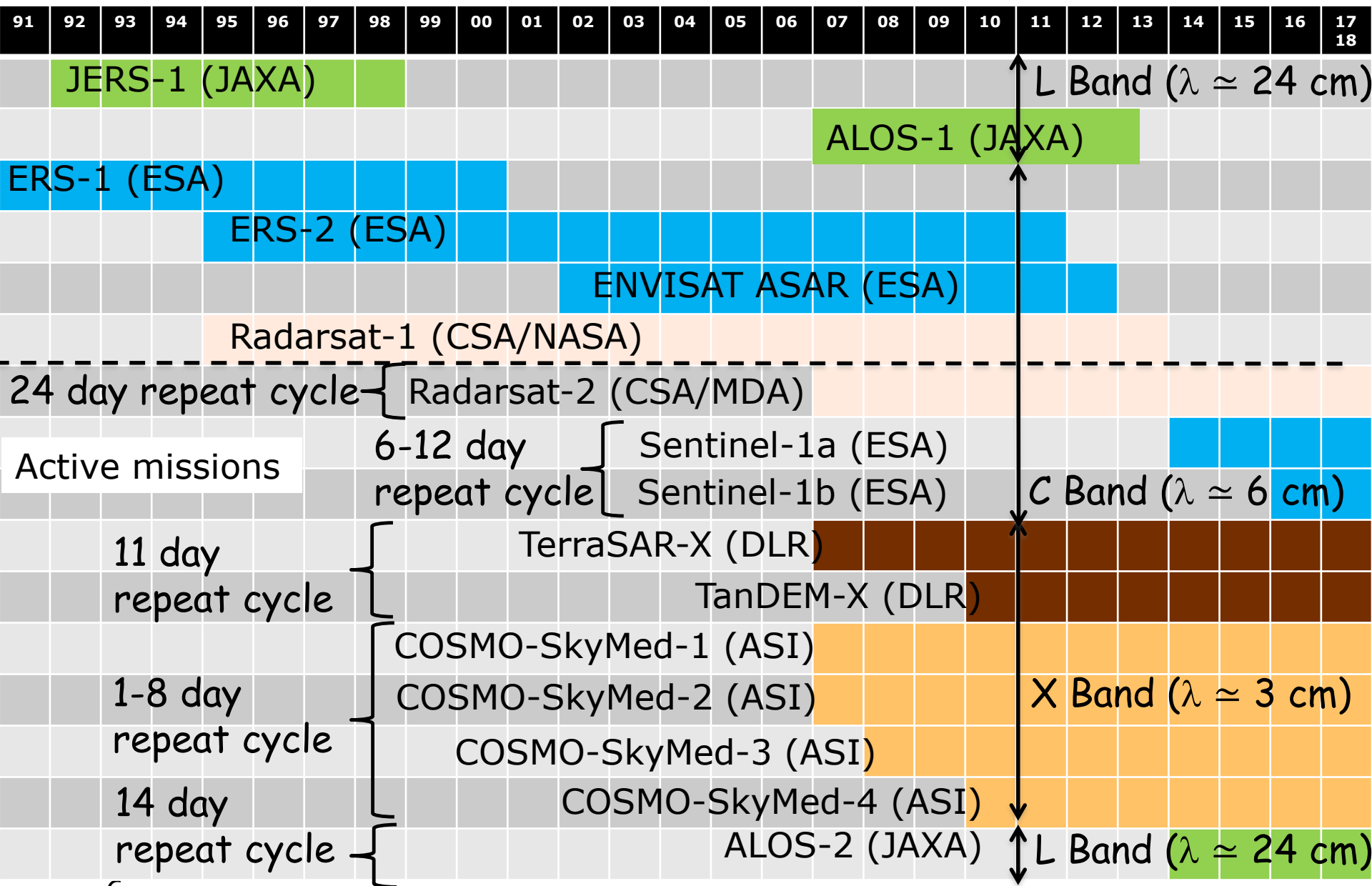
For ground: little penetration.

For ice:  
L band penetrates the  
Deepest (up to km)

Ku band penetrate 1-100 cm

Ka band very little.

Band	Frequency [GHz]	Wavelength [cm]
VHF	0.03-0.3	1000-100
UHF, P	0.3-1	100-30
L	1-2	30-15
S	2-4	15-7.5
C	4-8	7.5-3.75
X	8-12.5	3.75-2.4
Ku	12.5-18	2.4-1.7
Ka	18-40	1.7-0.75
V	50-75	0.60-0.40
W	75-111	0.40-0.27





# Selected acquisition mode parameters

Satellite	Launch date	Revisit time (days)	Mode	Wavelength (cm)	Incidence angle (deg)	Image Size (km)		Resolution (m)	
						Ground Range	Azimuth	Ground range	Azimuth
ALOS-2	24.05.2014	14	ScanSAR	24.25	8-70	350-490	350	10-20	57-78
			Stripmap		8-70	50-70	70	3-9	3-5.3
COSMO-SkyMed-1/2/3/4	08.06.2007/09.12.2010	1-8	Stripmap	3.11	20-60	40	40	3	3
Sentinel-1a/b	03.04.2014/25.04.2016	6-12	TOPS	5.55	30-46	250	250	5	20
			Stripmap		22-44	80	80	5	5
Radarsat-2	14.12.2007	24	Stripmap	5.55	10-60	20-170	20-170	2.6-22	2.1-5.1
TerraSAR-X/ TanDEM-X	15.06.2007/21.06.2010	11	Stripmap	3.11	15-60	30	50	2 (J. Merrymann)	

Image resolutions are computed for an incidence angle of 37 deg (J. Merrymann)

- Synthetic Aperture Radar.
  - “Synthetic Aperture”
  - Azimuth and range accuracy
  - SAR and SARin systems/satellites.

## Interferometric SAR

**Observation principle**

**Height accuracy**

**Data and Software**

**What does phase differences mean**

## Differential INSAR (DINSAR)

Deformation accuracy

Multiple INSAR and Persistent Scatterers and geodesy

## Next Generation altimeter

Surface water and Ocean topography. SWOT

## Laser Altimetry for Bathymetry (Heidi Ranndal).

# Interferometric SAR.

Requires a Baseline (B) to observe object at different Vantage points  
Antenna transmit "bursts" with signal of same phase

Increase Range resolution looking at phase differences

Phase of a pixel  $\phi$  includes scatterer and range contrib:

$$\phi = \phi_s + \phi_p$$

Where  $\phi_s$  = scatter differences (we ignore)

$$\phi_p = R \cdot 4\pi / \lambda$$

$\phi_p$  can only be measured modulo  $2\pi$

Differencing two images (Assuming  $\phi_{s1} = \phi_{s2}$ )

Interferometric phase will be.

$$\phi_{int} = \phi_{p2} - \phi_{p1}$$

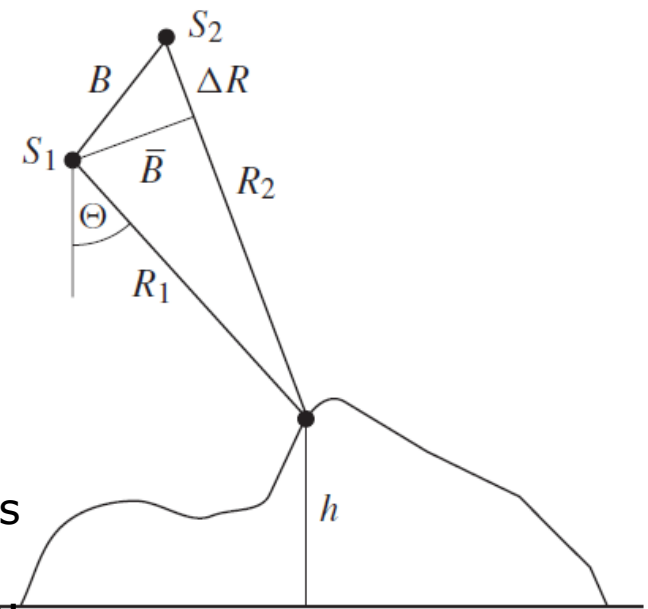
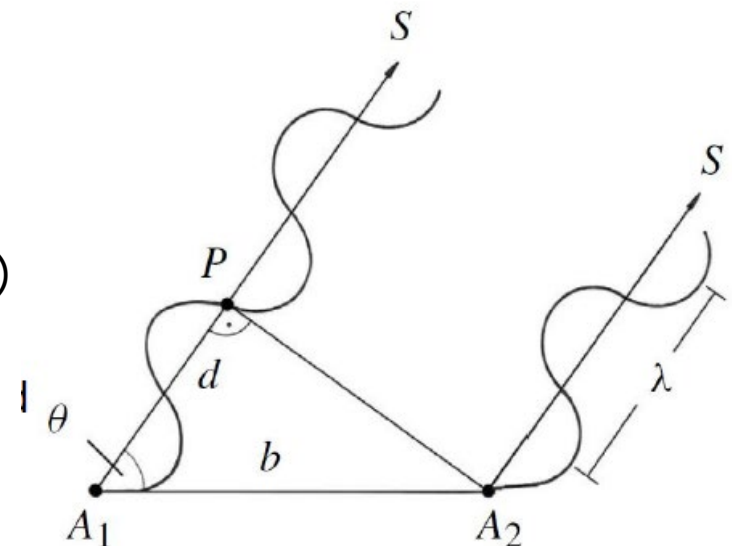


Figure 11.9. InSAR geometry



## Two ways of obtaining IN-SAR

### Single pass Across-track interferometry

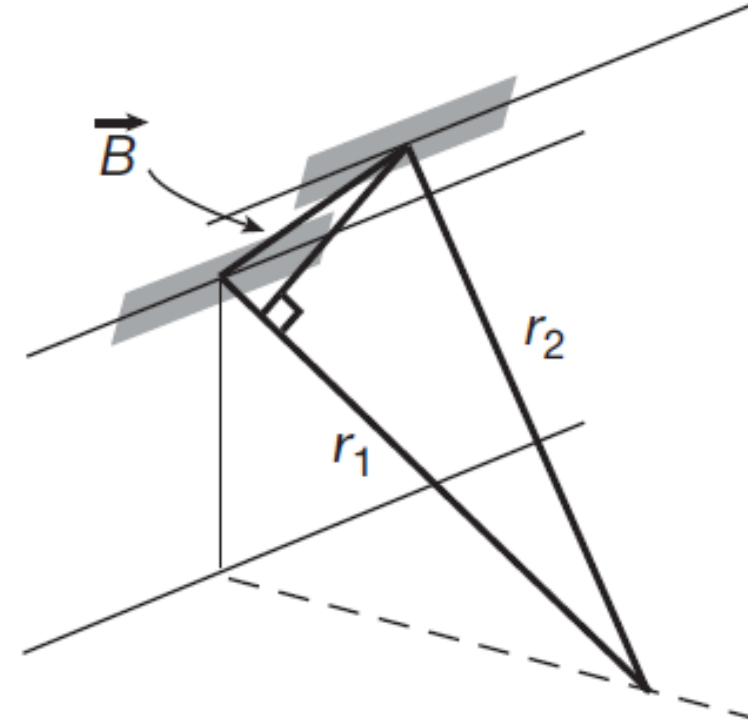
Good for Digital Elevation Models (DEM)  
Antennas separated.  
Height resolution  
(from full phase cycle)

$$\Delta h = \frac{\lambda}{2} \frac{R}{B} \tan \theta.$$

$\theta$  incident angle  
Typically 5-10 meters.  
(Seeber 11.17)

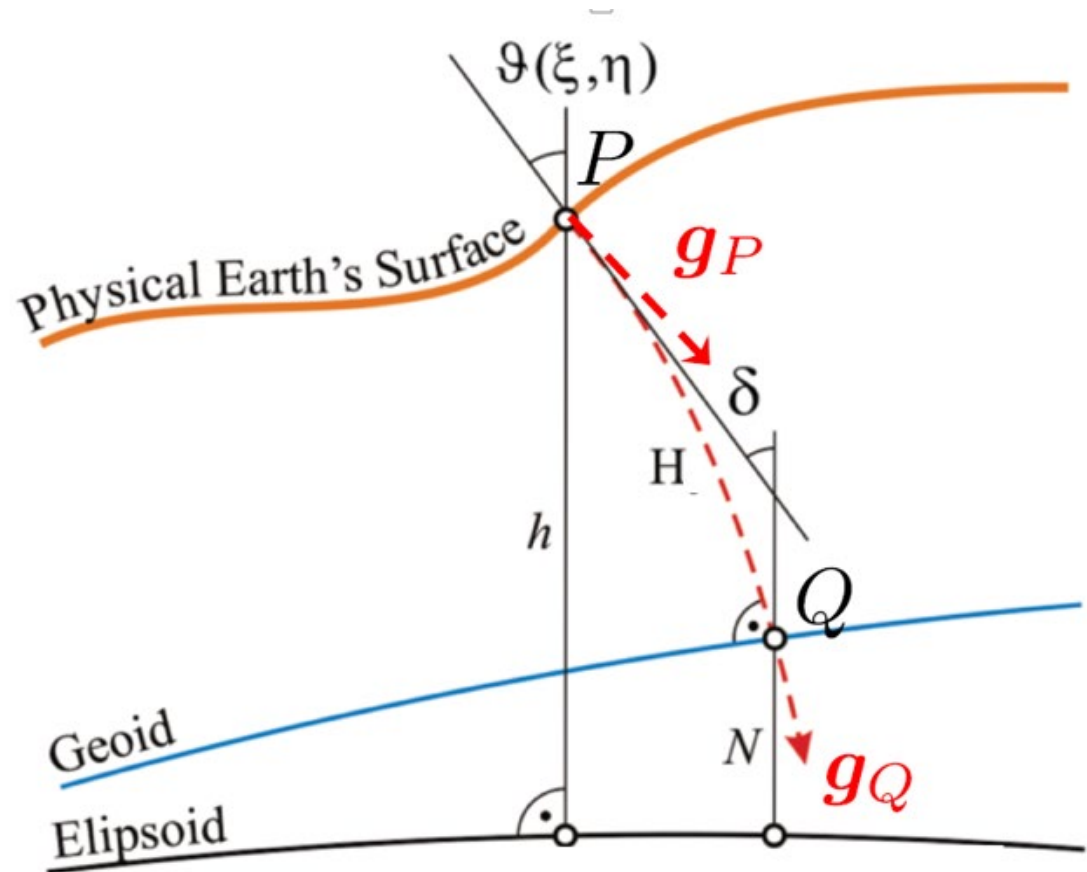
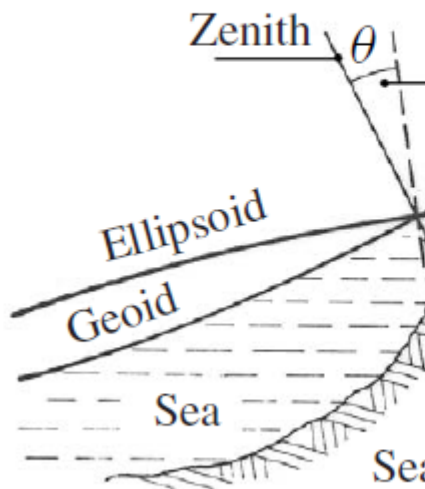
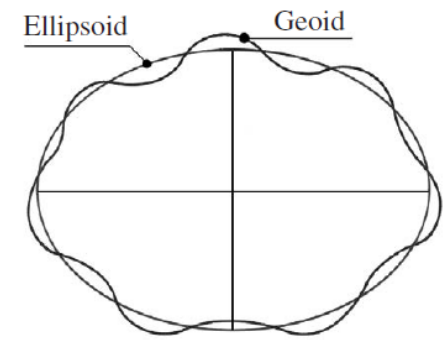
Limitations:

- accuracy of phase obs
- SAR geometry
- Atmospheric effect

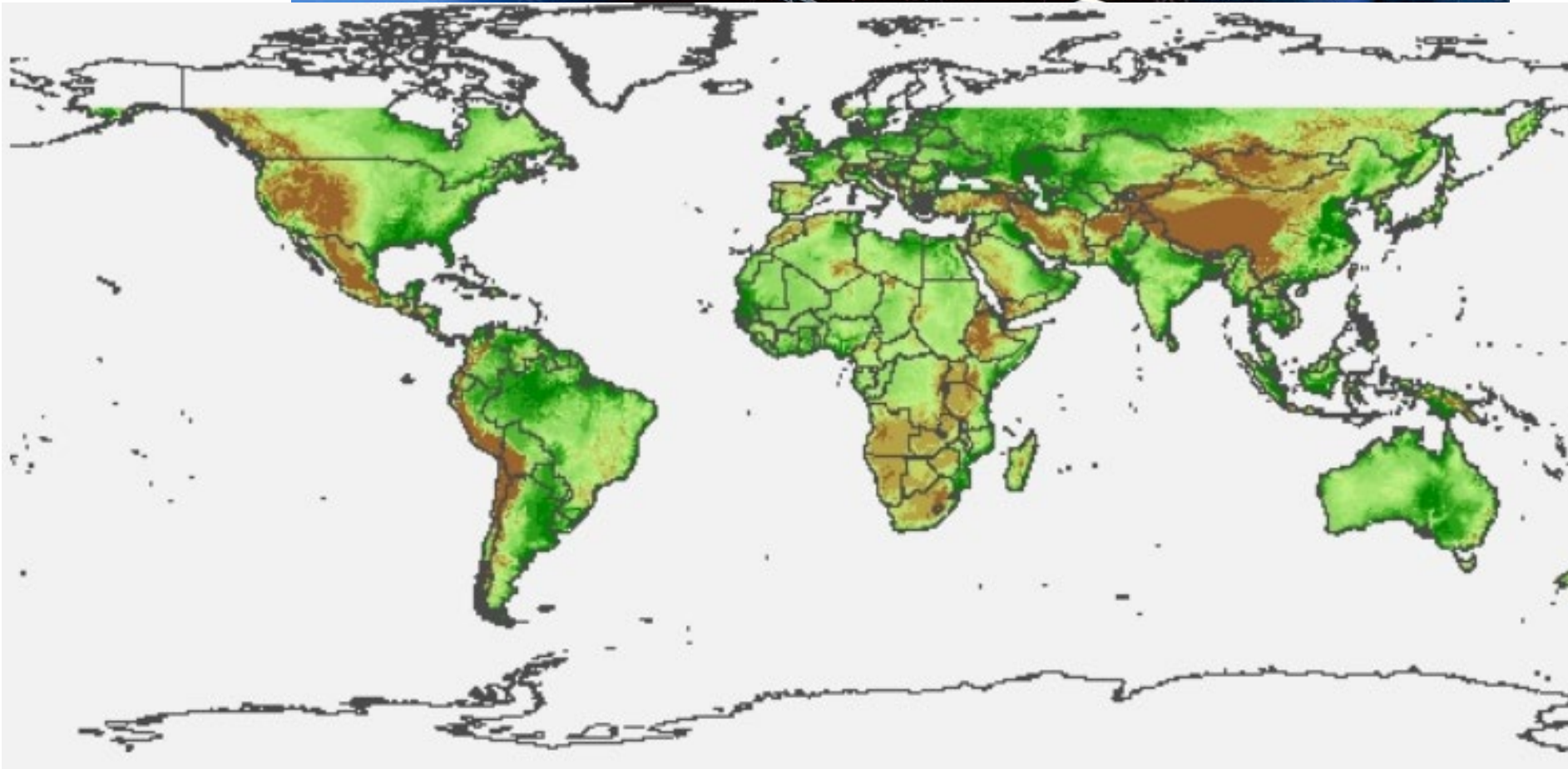


# Heights

$h = H + N$  for small height.  
 $h$  is ellipsoidal height,  
 $N$  geoid undulation (Height)  
 $H$  is orthometric height  
 $\Theta$  is the Vertical deflection



# Shuttle Radar Topography Mission



## Geodynamics

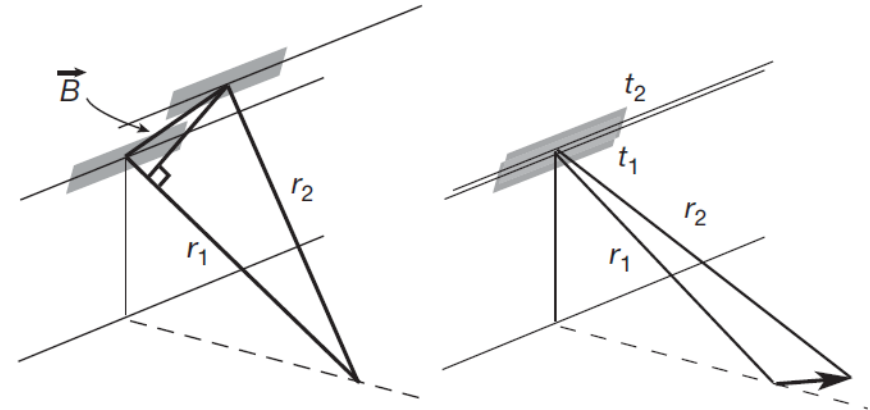
### Repeat pass interferometry

Several days or month between

Requirement depends "on target"  
Target scattering behavior must not  
change too much.

Baseline must be reasonable short  
(hence accurate orbit).  
Max is around 1 km at 800 km altitude

Otherwise Decorrelation.



**Figure 3** Interferometric SAR for topographic mapping uses two apertures separated by a 'baseline,'  $B$ , to image the surface. The phase difference between the apertures for each image point, along with the range and knowledge of the baseline, can be used to infer the precise shape of the imaging triangle to derive the topographic height of the image point. At left, a range difference exists because the scene is viewed from two different vantage points. This is described by a shift in the point target response as presented in the text. At right, a range difference is generated by a change in the position of the scene from one time to the next, imaged from the same vantage point. This range difference is described by a scene shift, not a point target response shift; the mathematics is the same but for a sign change.

## Example of Observation

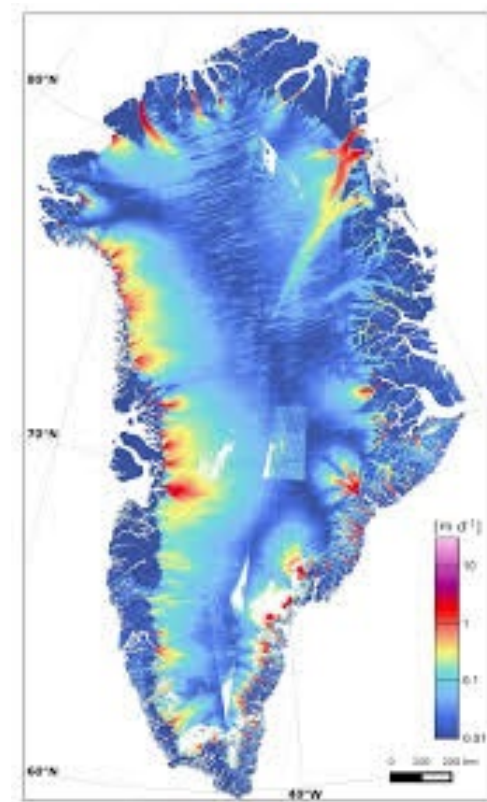
Image containing power and phase will be Complex image

Looking at one returned Single Look Complex Image (SLC)

ESA SNAP toolbox.

<https://step.esa.int/main/toolboxes/snap/>

It can help you with a lot of the processing of SAR images  
i.e. phase unwrapping etc, Atmospheric corrections. And  
Geo-location. We generally use it for projects.

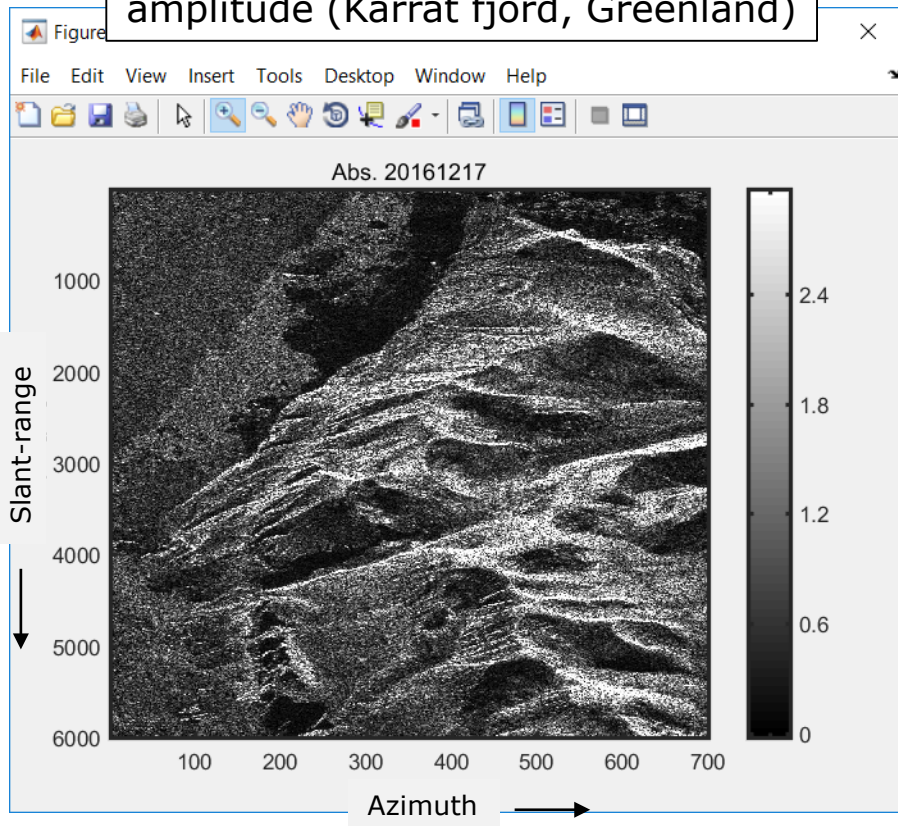




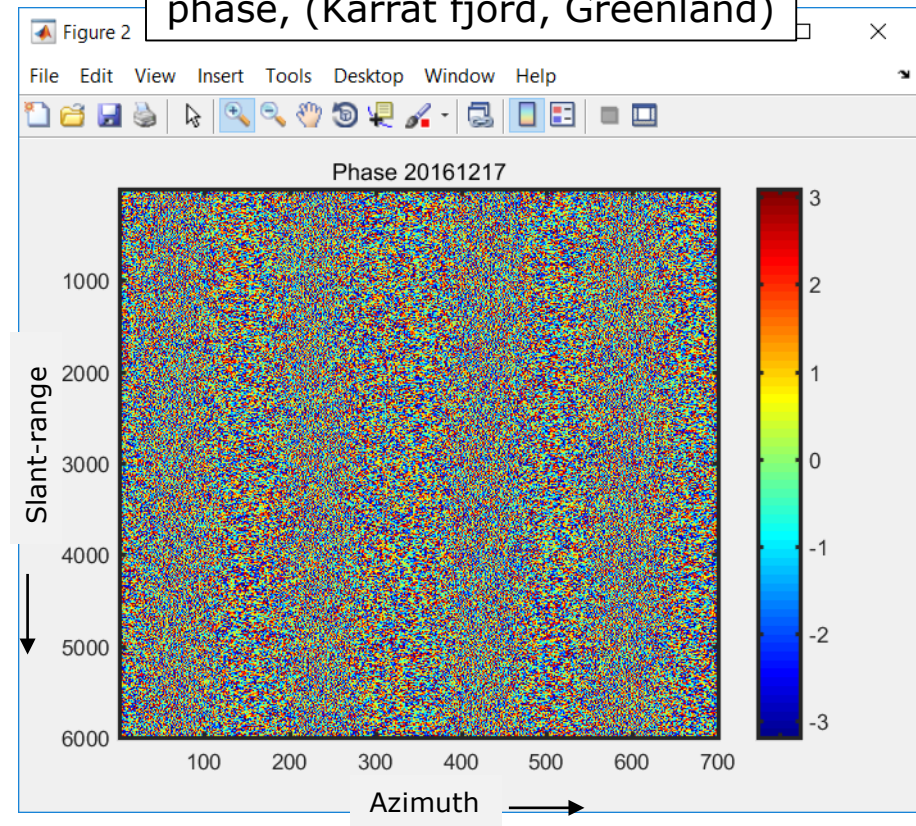
# Single Look Complex (SLC) image

(i.e. a focused full-resolution SAR image)

Sentinel-1a, ascending image  
amplitude (Karrat fjord, Greenland)



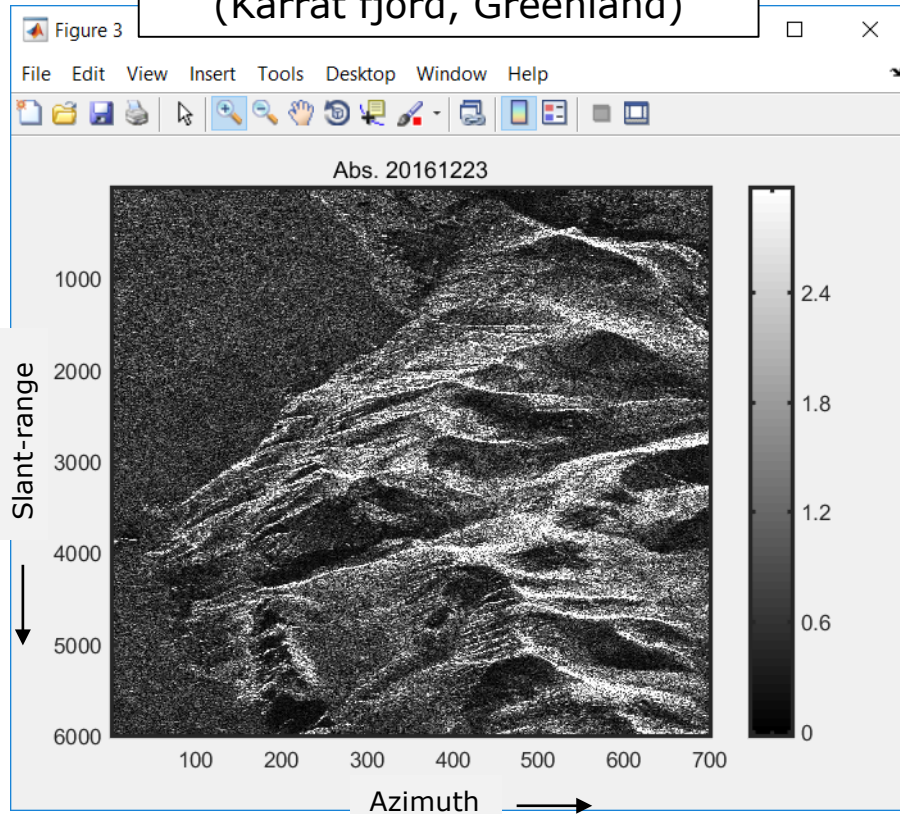
Sentinel-1a, ascending image  
phase, (Karrat fjord, Greenland)



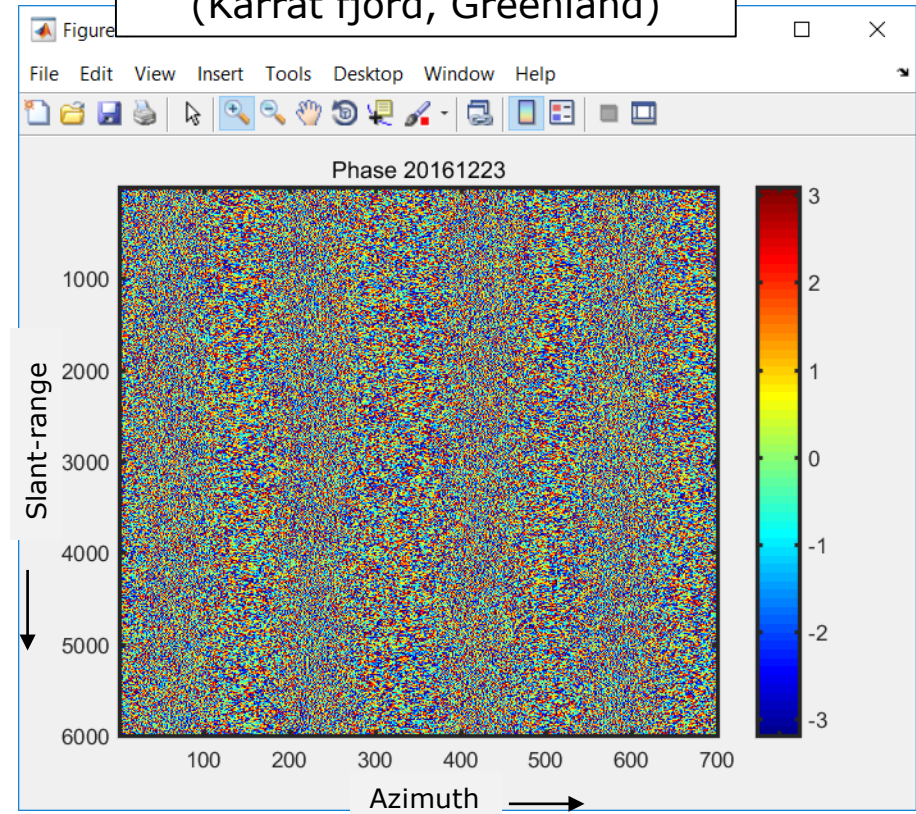
**The phase of an SLC image looks random**

# We try again 6 days later ...

Sentinel-1b, image Amplitude  
(Karrat fjord, Greenland)



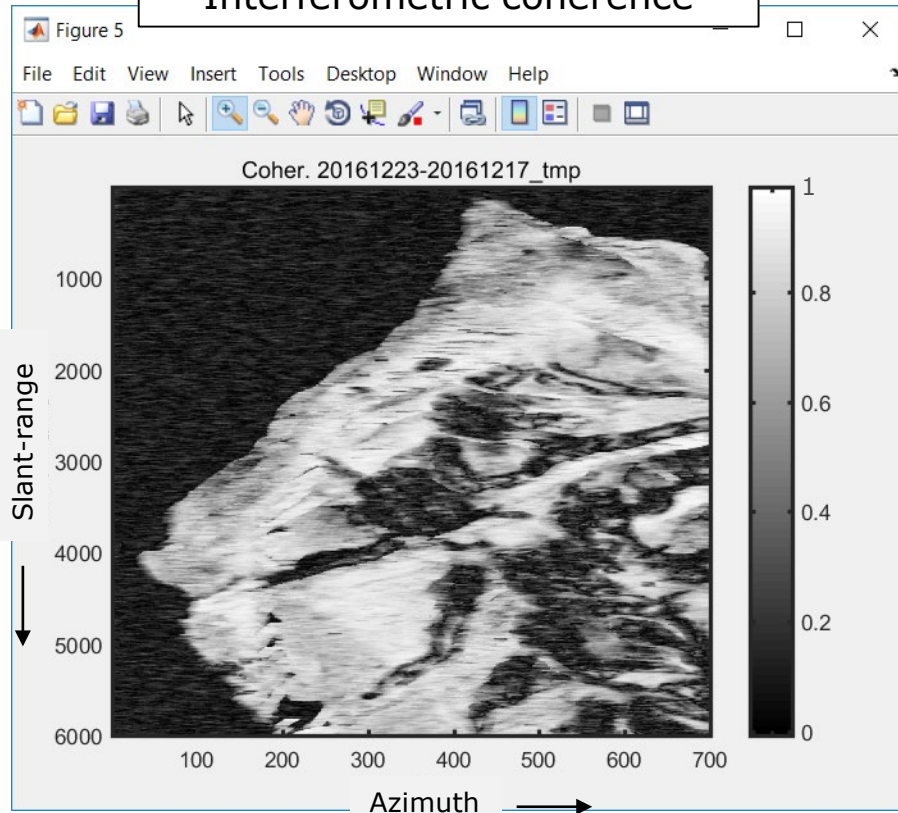
Sentinel-1b, image Phase,  
(Karrat fjord, Greenland)



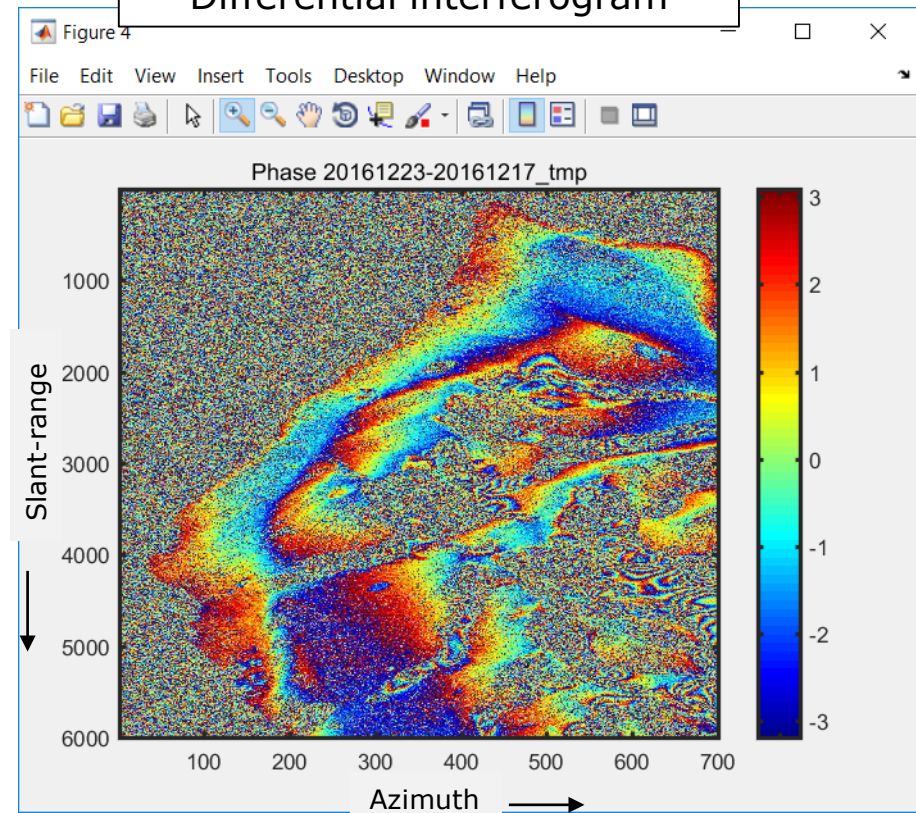
**Still random**

# How about the phase difference?

Interferometric coherence



Differential interferogram



**Luckily the phase *difference* is not random everywhere!**

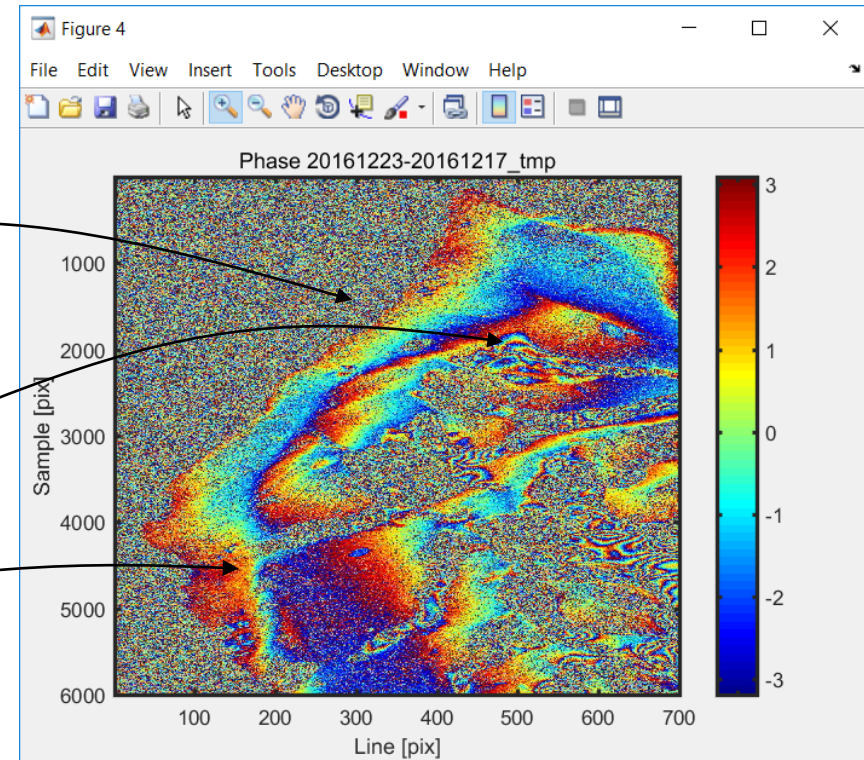
# So what are the colours we see in an interferogram?

$$\phi_{\text{int}} = \left[ \underbrace{-\frac{4\pi}{\lambda} (R_0^1 - R_0^2) - 2\pi f_c (\tau_{\text{atmo}}^2)}_{\text{Spatially-correlated terms}} + \underbrace{\phi_b^1 - \phi_b^2}_{\text{Spatially-uncorrelated (noisy) term}} \right] \text{mod } 2\pi$$

$$\phi_{\text{flat}} + \phi_{\text{topo}} + \phi_{\text{defo}}$$

Area where the random phase contributions prevail  
-> noisy phase

Areas where the spatially-correlated (more deterministic) phase contributions prevail  
-> clear phase fringes



- Synthetic Aperture Radar.
  - “Synthetic Aperture”
  - Azimuth and range accuracy
  - SAR and SARin systems/satellites.

## Interferometric SAR

Observation principle

Height accuracy

Data and Software

What does phase differences mean

## Differential and Multiple INSAR (DINSAR)

Deformation accuracy

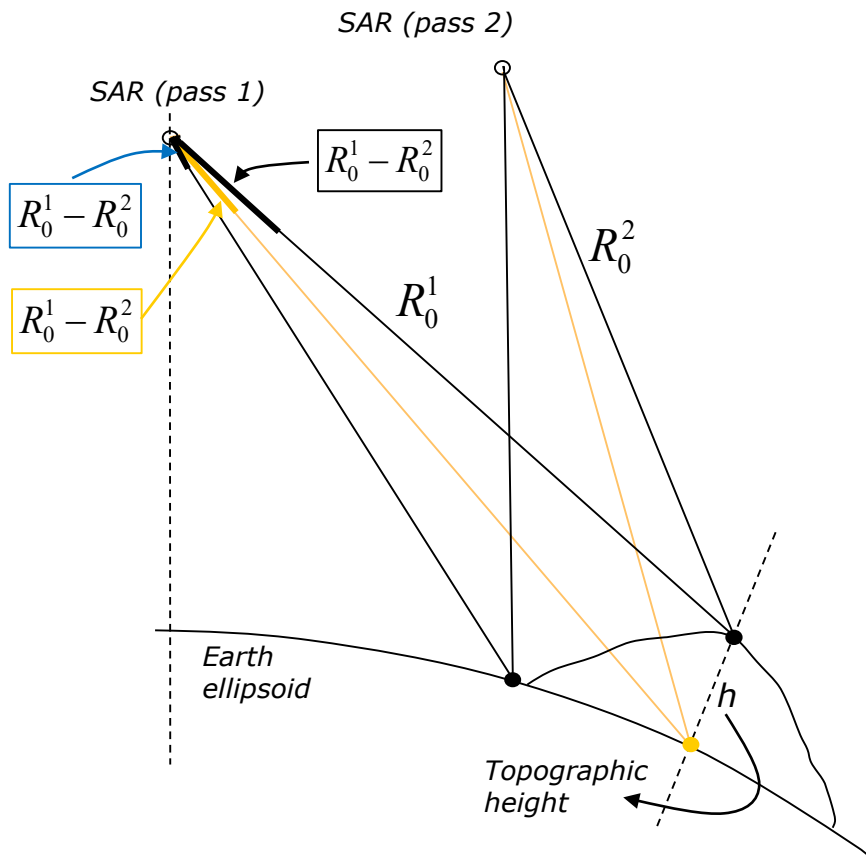
Persistent Scatterers and geodesy

## Next Generation altimeter

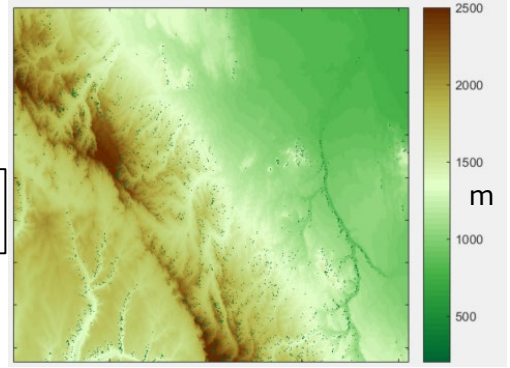
Surface water and Ocean topography. SWOT

Laser Altimetry for Bathymetry (Heidi Ranndal).

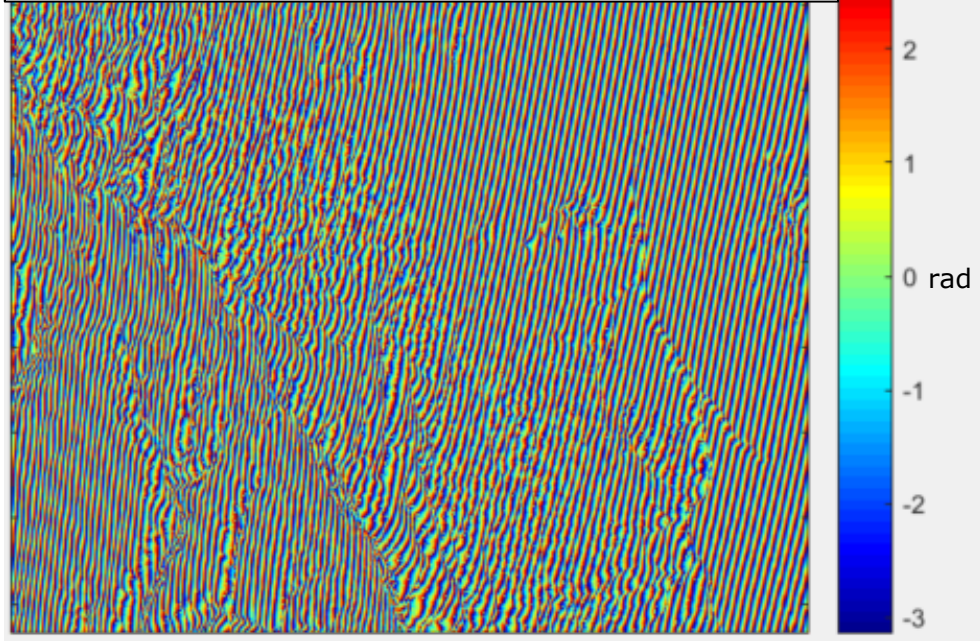
Differencing interferograms (or double difference interferogram) enhances deformations.  
In a differential interferogram  $\phi_{flat}$  and  $\phi_{topo}$  are removed based on an Earth ellipsoid and a Digital Elevation Model



SRTM Digital Elevation Model, Rift Valley, Ethiopia



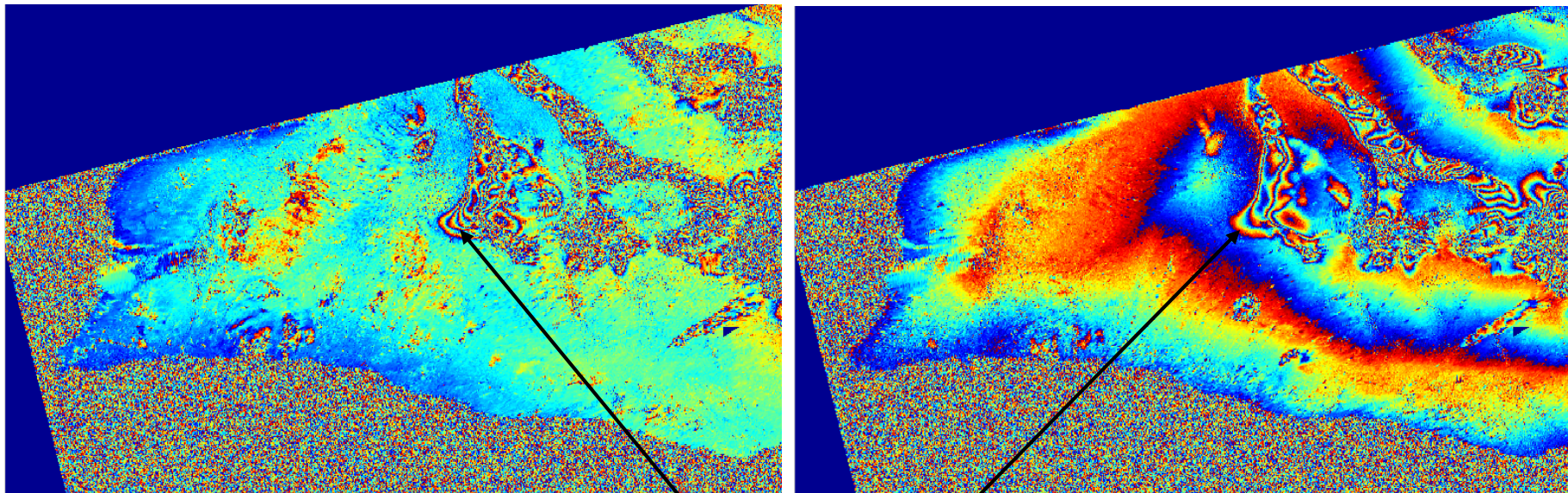
Sentinel-1a (wrapped flattening + topographic phase) 28 Mar. 2015 - 21 Apr. 2015,  $B_n = -36$  m,  $B_{temp} = 24$  days



## Sensitivity to motion (in pictures)

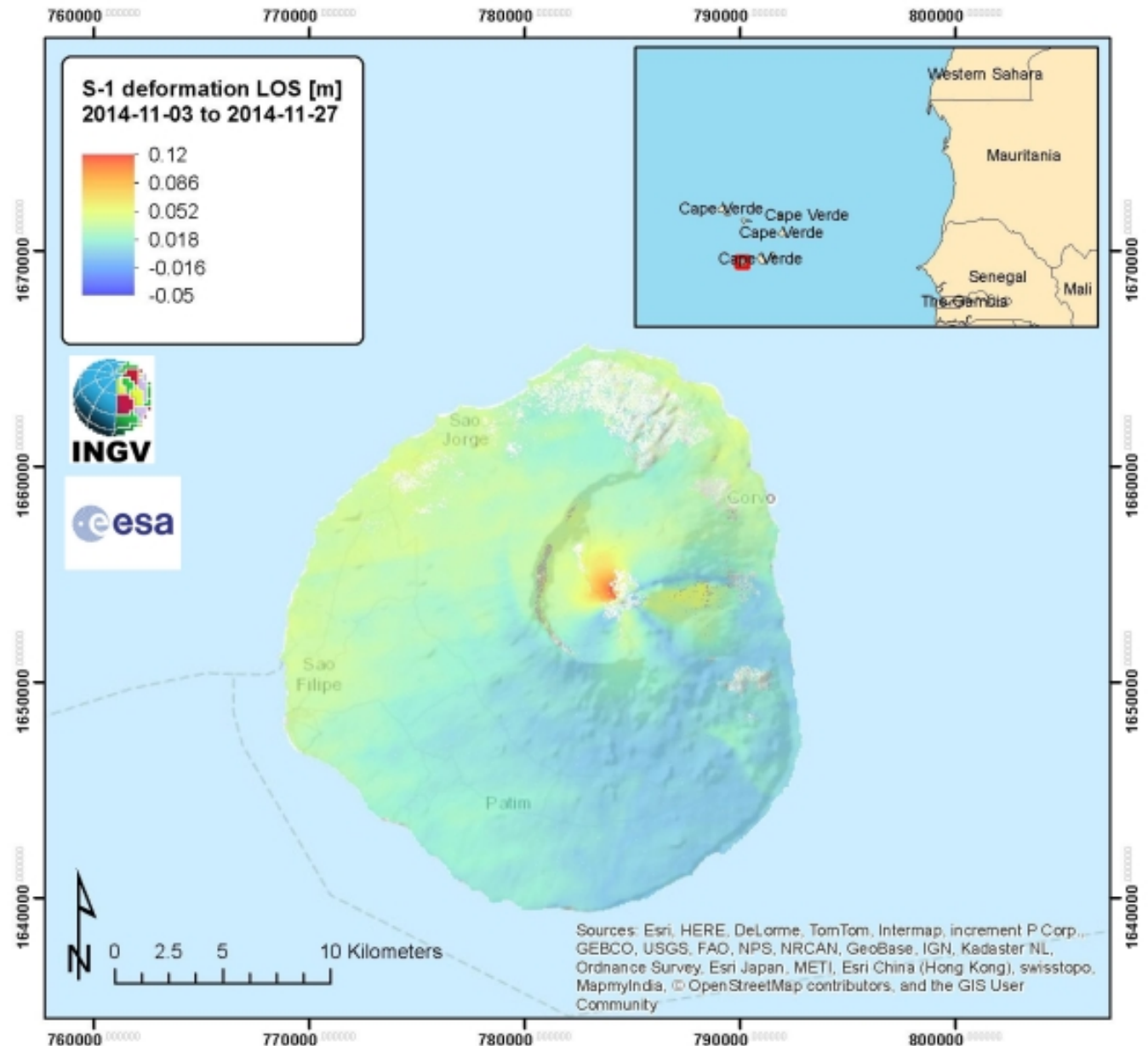
23 Oct. - 04 Nov. 2014,  $B_n=2$  m,  
 $B_{temp}=12$  days

17 Dec. - 23 Dec. 2016,  $B_n=-6$  m,  
 $B_{temp}=6$  days



Larger time separation -> more fringes (motion)

# Volcanos





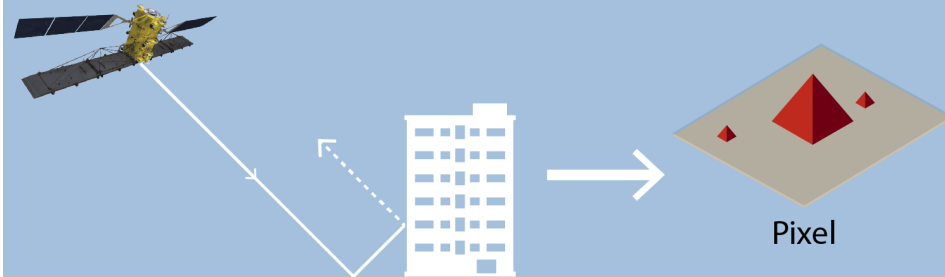
# Multi-temporal DINSAR

Requires stable **DOMINATING** scatterer over time.  
Could be buildings

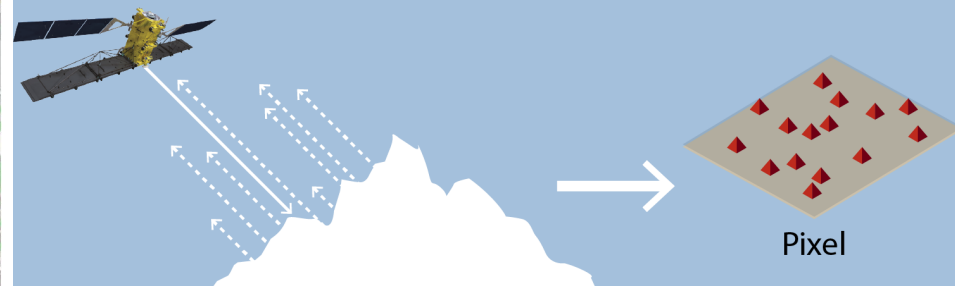
If these are geodetic tied to ground  
(using i.e. GPS) then deformation on  
Cm or better can be determined.



**Point Scatterer:**  
One pixel is dominated by a single large reflector

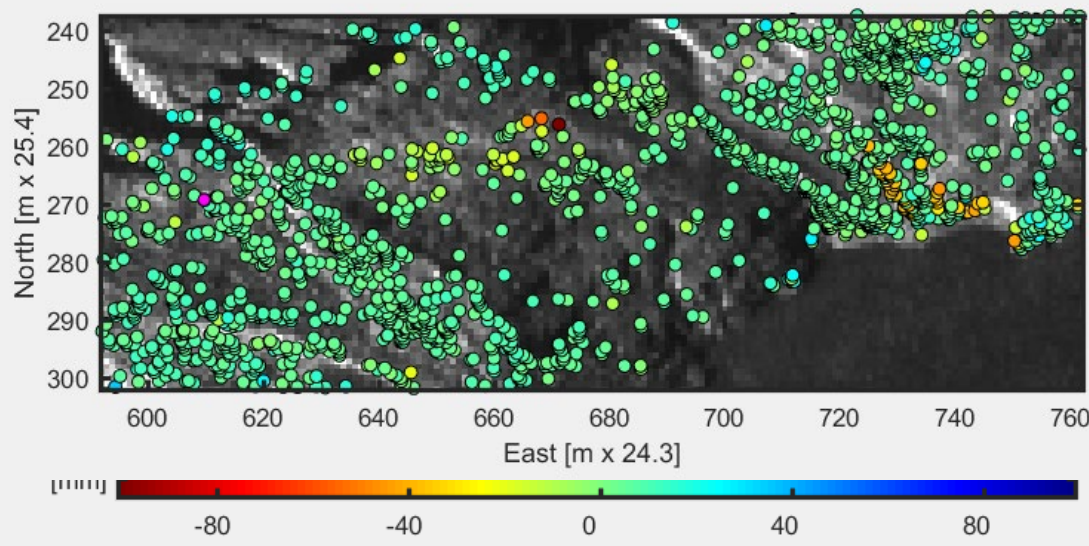


**Distributed Scatterer:**  
One pixel contains many small reflectors

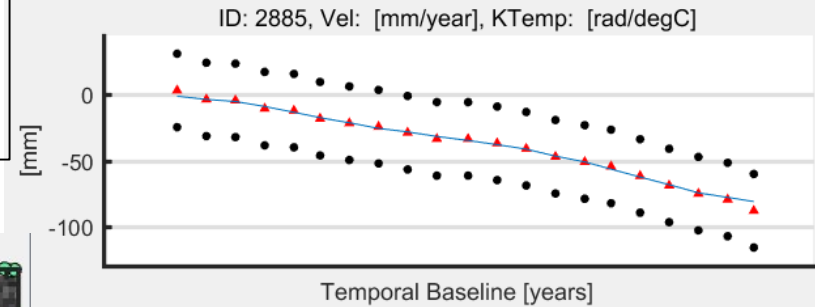


Motion can be distinguished from error sources (e.g. atmosphere) by analyzing a set of sparse points with stable radar returns (PSs or DSs) and several (tens of) DInSAR interferograms

Cumulative deformation



Deformation time-series



Deformations are relative

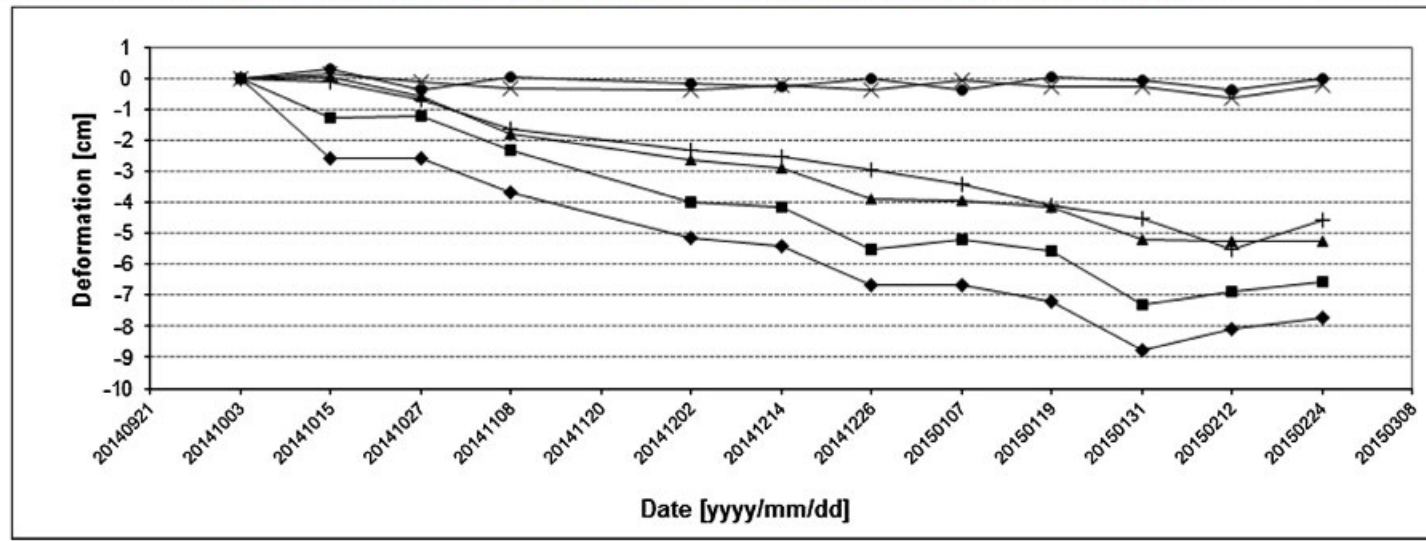
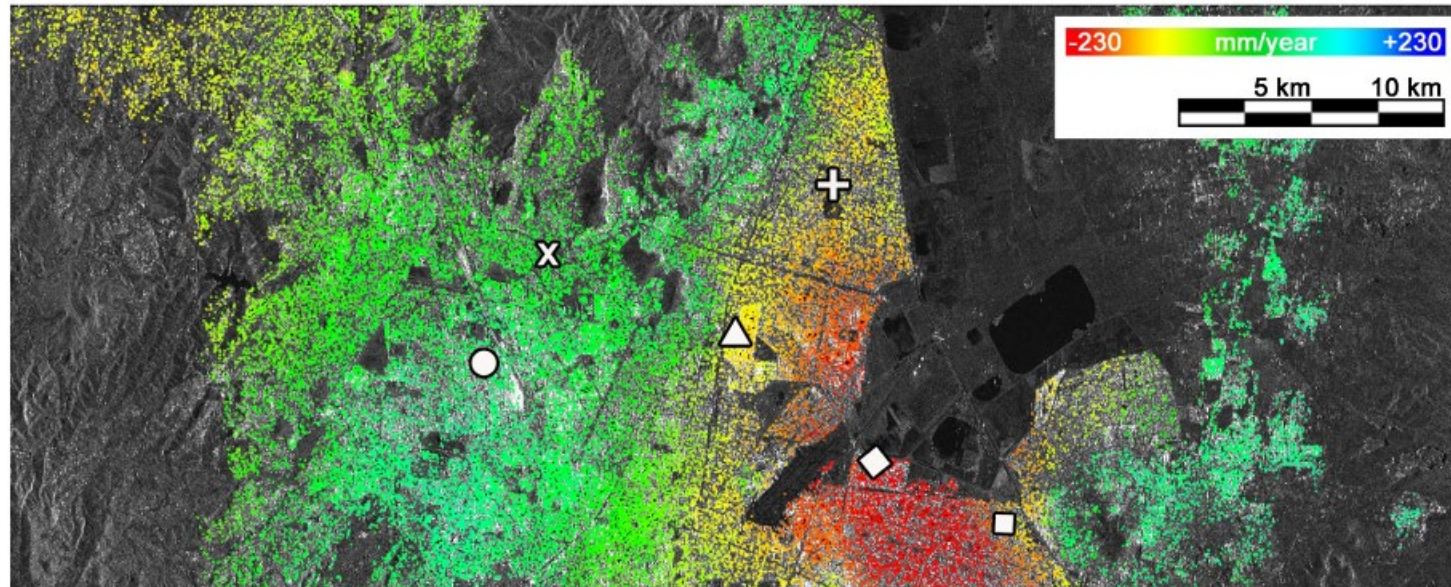
- in space (reference PS/DS)
- in time (first processed image)

Away from the radar

Towards the radar

Measurements are 1D (projection of 3D deformation along the SAR line-of-sight)

- Deformation (subsidence) of Mexico City (i.e. due to extraction of fresh-water)



- Synthetic Aperture Radar.
  - “Synthetic Aperture”
  - Azimuth and range accuracy
  - SAR and SARin systems/satellites.

## Interferometric SAR

Observation principle

Height accuracy

Data and Software

## Differential INSAR (DINSAR)

Deformation accuracy

Multiple INSAR and Persistent Scatterers and geodesy

## Next Generation altimeter

Surface water and Ocean topography. SWOT

Laser Altimetry for Bathymetry (Heidi Ranndal).

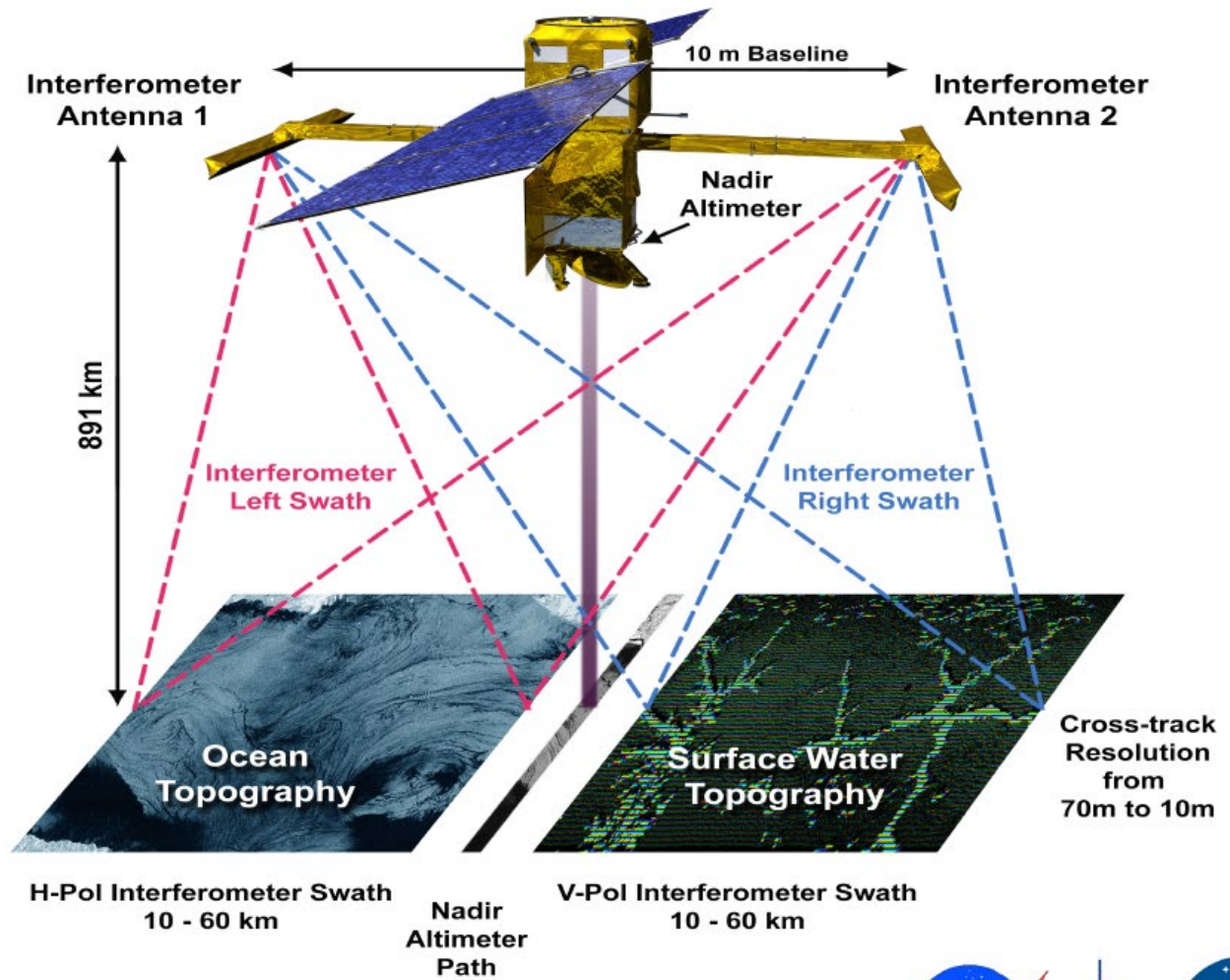
**Precise height at NADIR using satellite altimetry (points).**

**Precise height **variations** away from NADIR using INSAR (pictures)**

**Why don't we merge these  
to get accurate height everywhere in the pictures**



### SWOT -2D measurement of surface water topography



# SWOT orbits

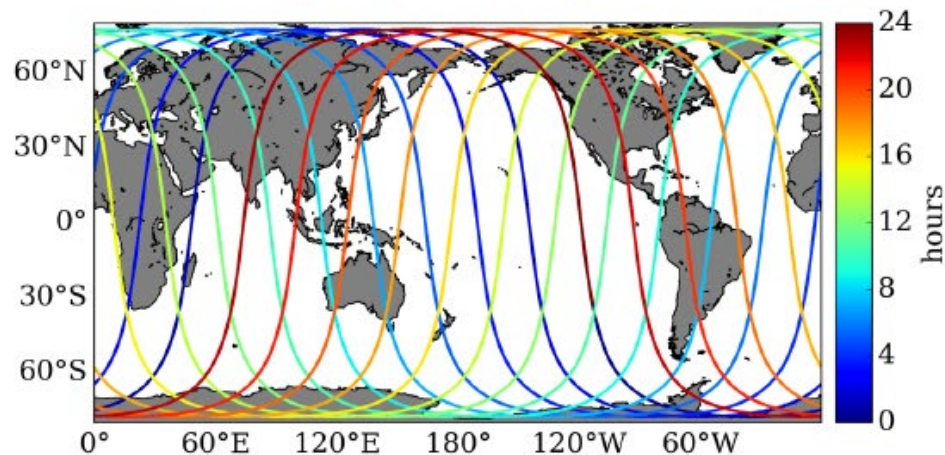
Nominal Launch date : Sept 2021

**First 6 months : 1-day orbit :**

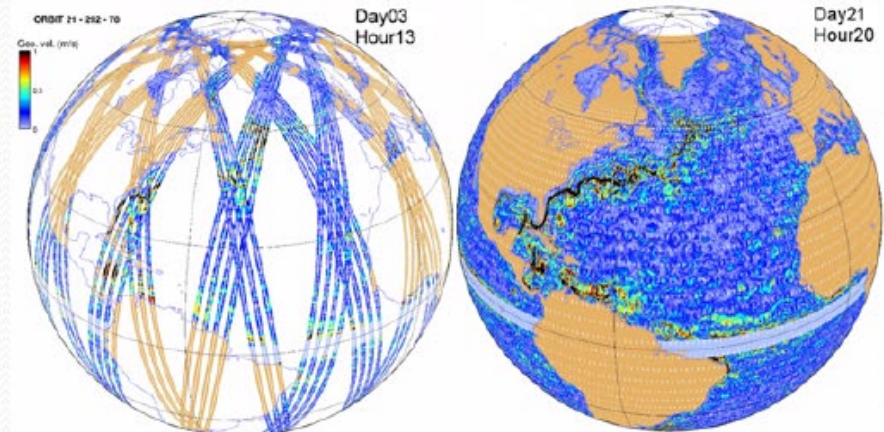
1st 3 months – instrument checkout

2<sup>nd</sup> 3 months - Dec-Feb 2022 – Science orbit

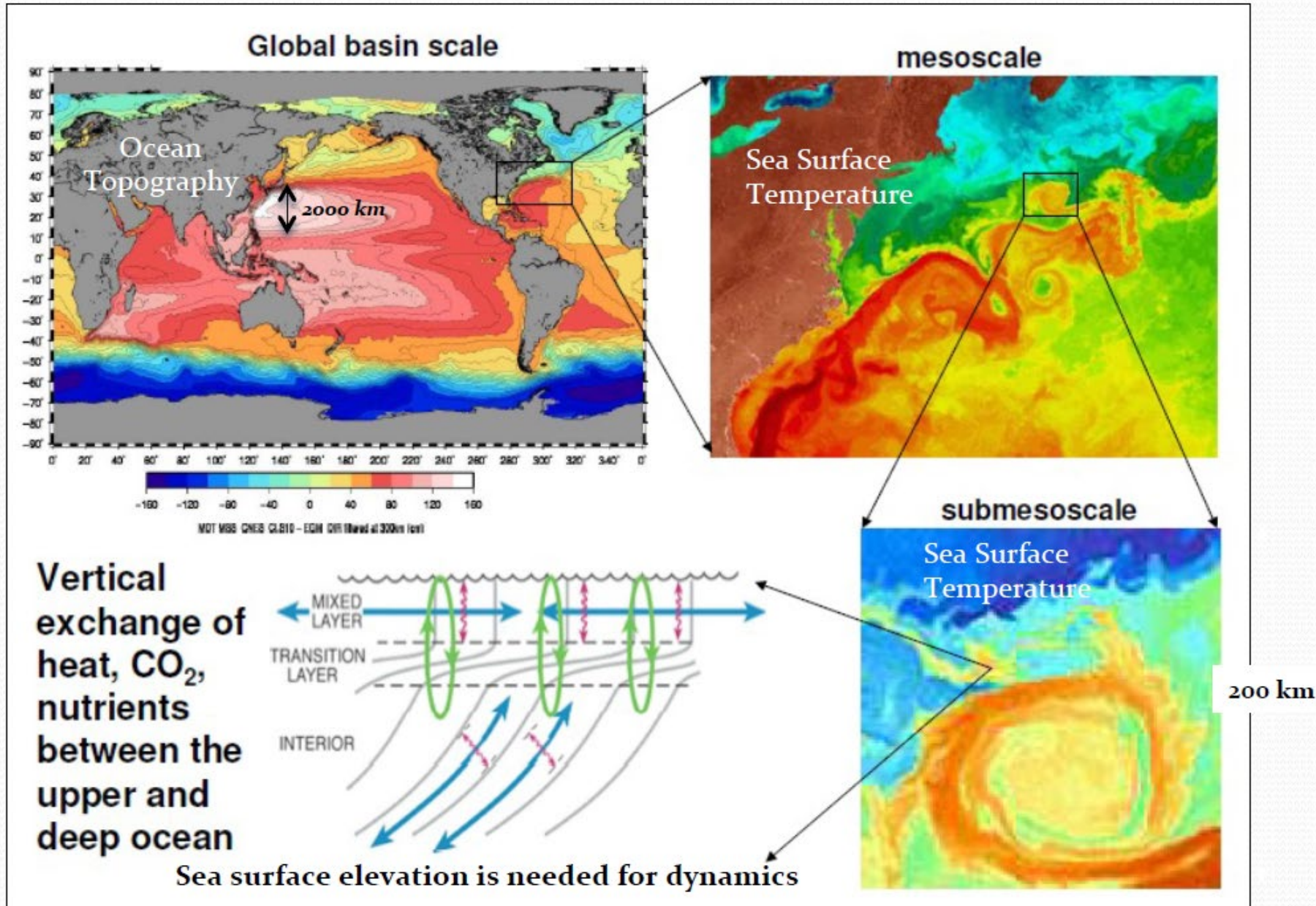
➤ Ideal for ocean studies of rapidly evolving small mesoscales and submesoscales



**3-year 21-day repeat orbit**  
**Nominally : Mar 2022 to Mar 2025**  
Full global coverage  
1-day and 10-day sub-cycles for  
better mesoscale coverage

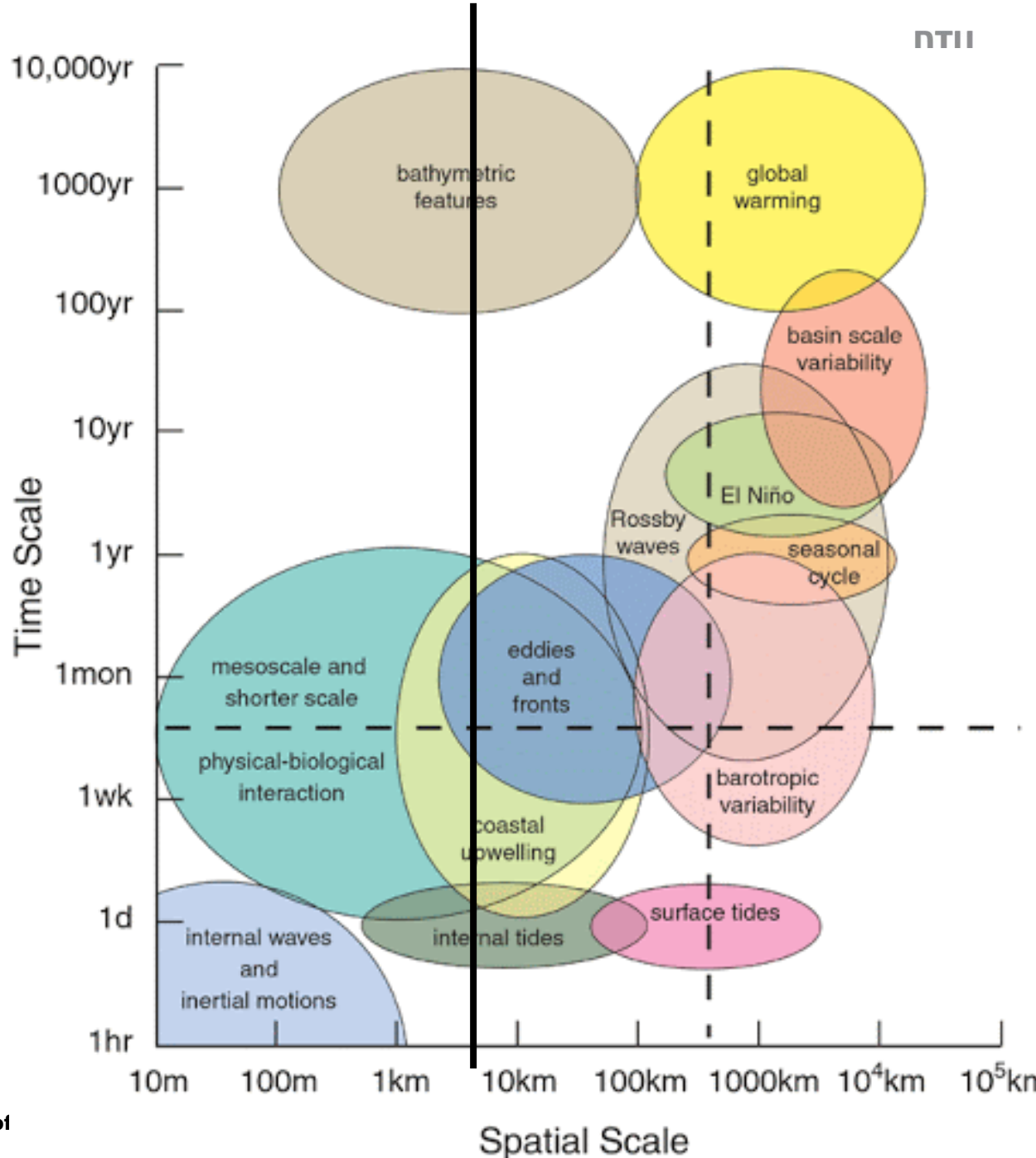


# Targeting the smaller scales of ocean dynamics





# Scales in the Ocean drive SWOT accuracy



Resolution is around  
5 x 5 meters.  
However need to  
average ocean cells  
to have phase  
robustness (50x50m)

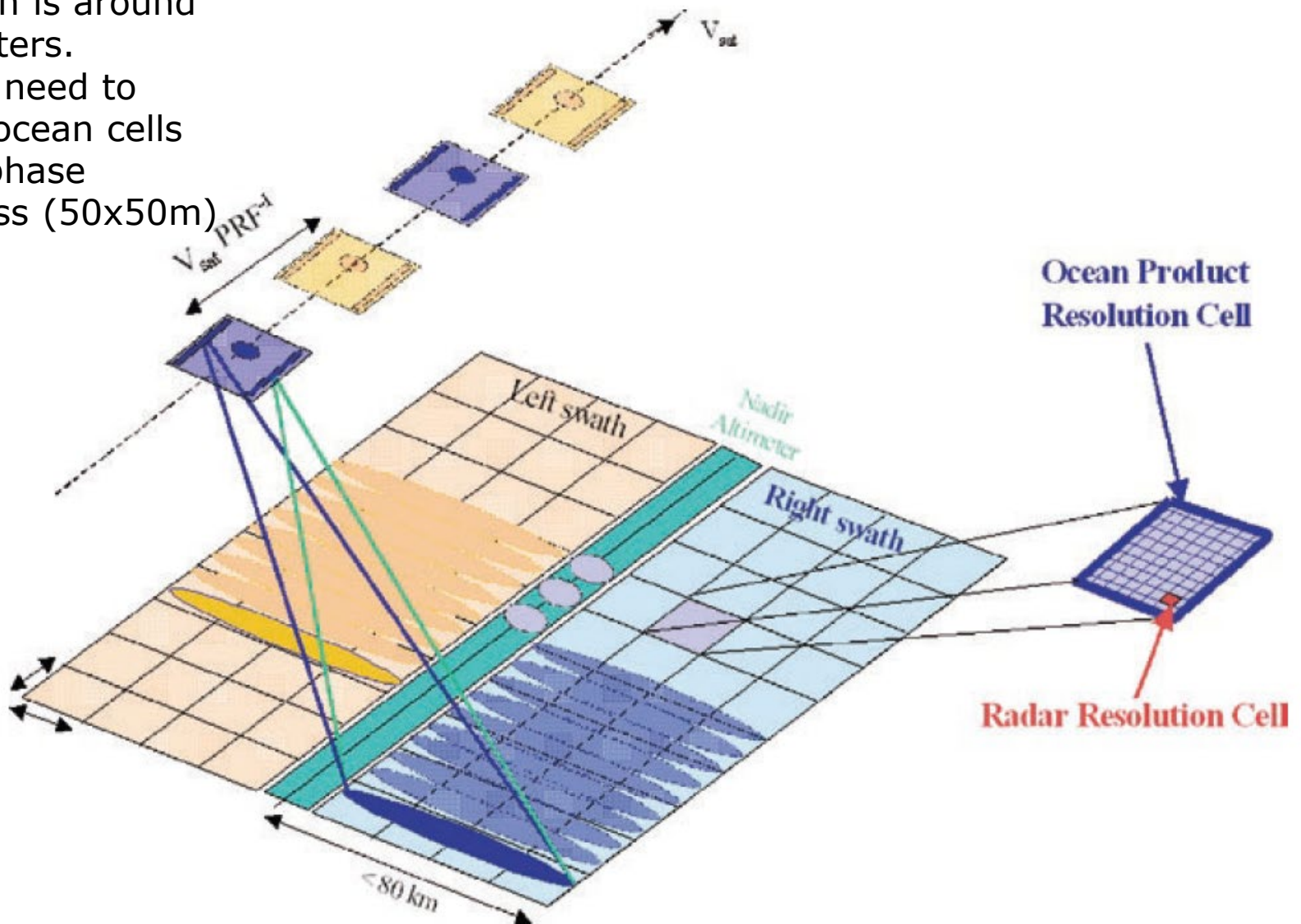
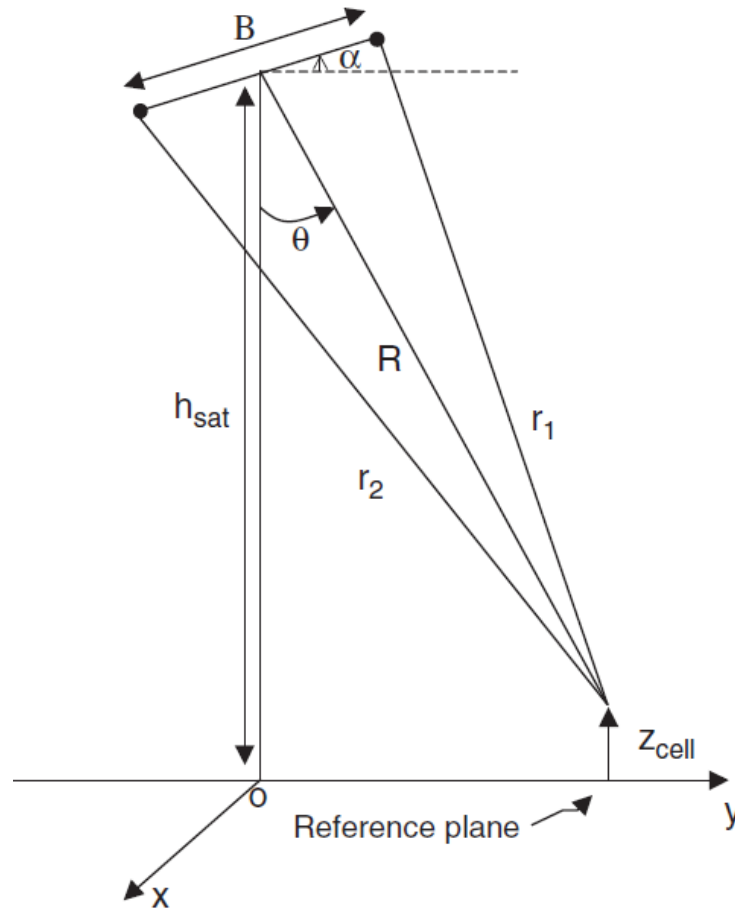


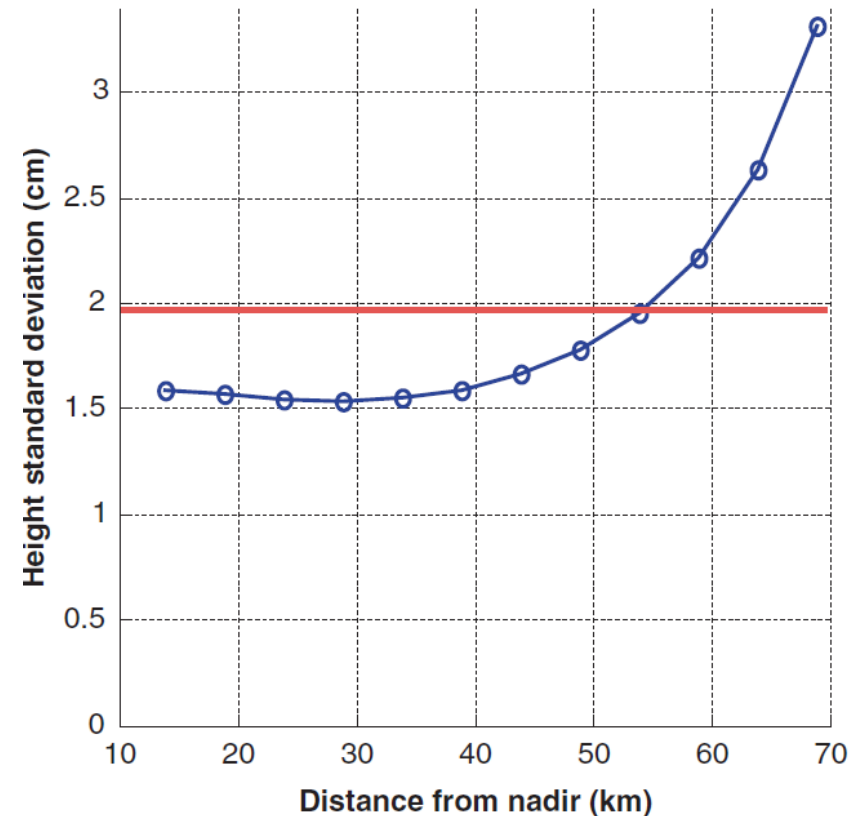
Fig. 20.3 Geometry and resolution cells for a swath altimeter

Uncertainty of baseline roll (instrument)  
And Distance  $y$  away from nadir.



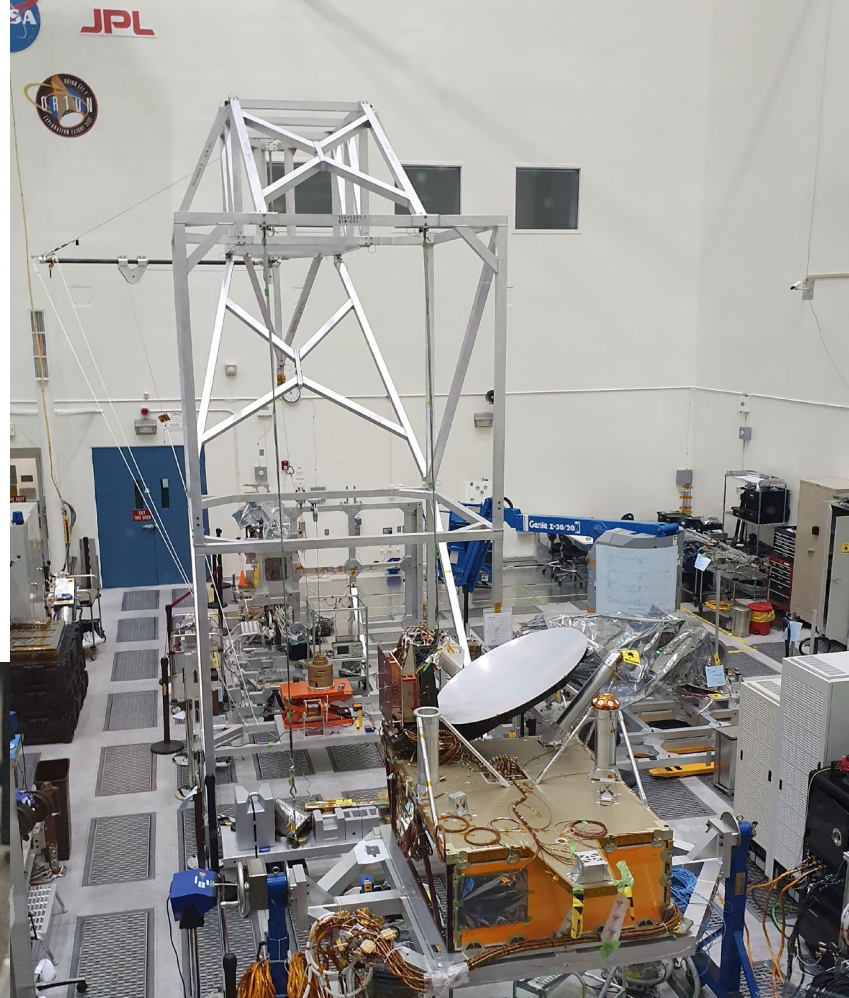
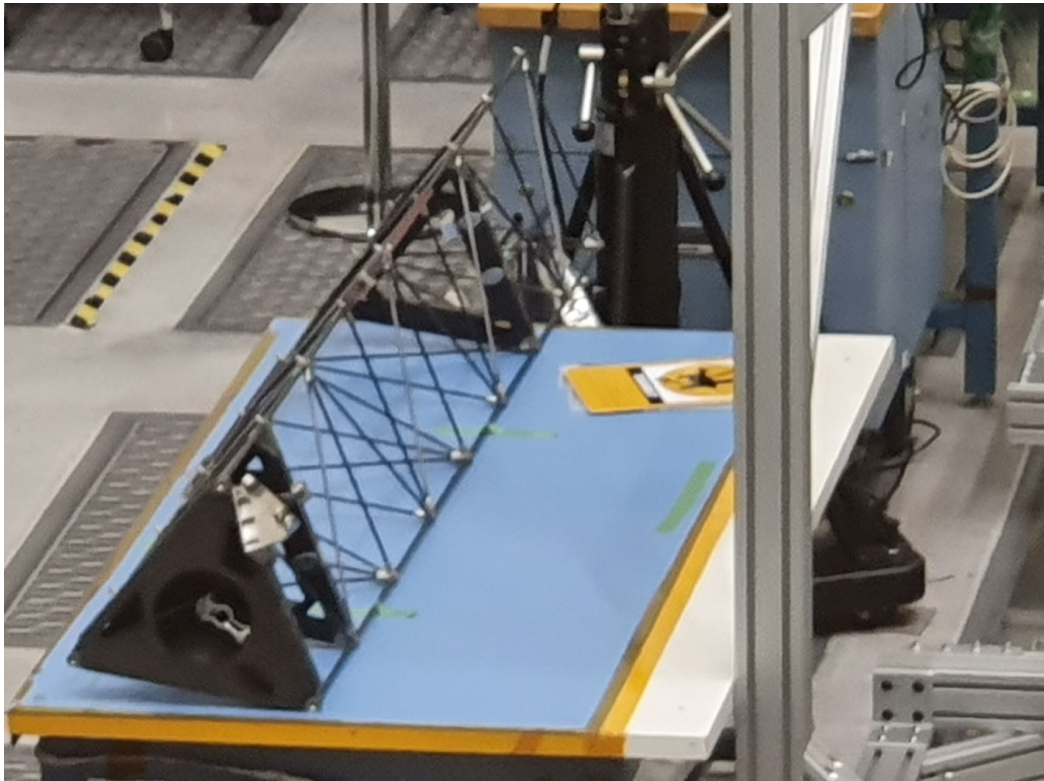
$$\delta z \approx R\theta \delta\alpha = y\delta\alpha$$

Instrumental Height Error Budget SAR Mode Pixel  
5.0 km by 5.0 km



## Status on SWOT

**We participate in SWOT Science team.  
I Visited JPL facility in January 2020  
Launch delayed from Sep 2021  
to Feb 2022 (due to covid)**

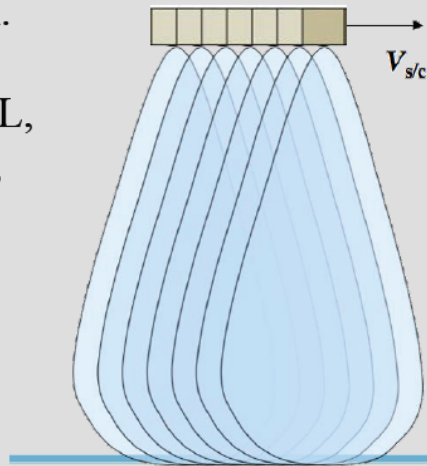


# Until then – we can use FF SAR of C2.



## Conventional Altimeter

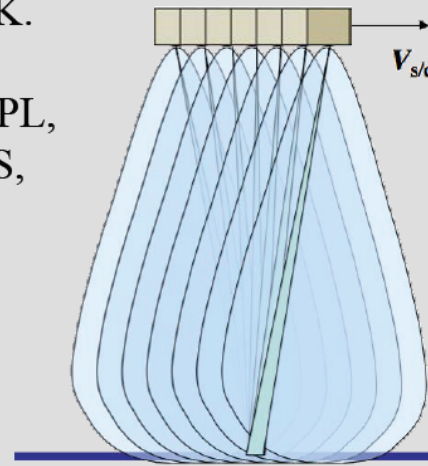
Image K.  
Raney,  
JHU/APL,  
TGARS,  
1998



- Low Resolution Mode
- Pulse limited footprint (circular)
- 1.5 / 5 km res. depending on SWH
- Open burst operation
- PRF ~ 2 kHz

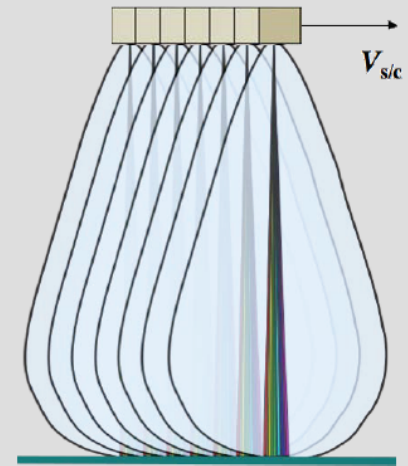
## Delay-Doppler Altimeter

Image K.  
Raney,  
JHU/APL,  
TGARS,  
1998



- Unfocused SAR processing
- ~300 m resolution Along-Track
- Pulse limited across-track
- Closed Burst
- PRF ~ 18 KHz

## Focused SAR Altimeter

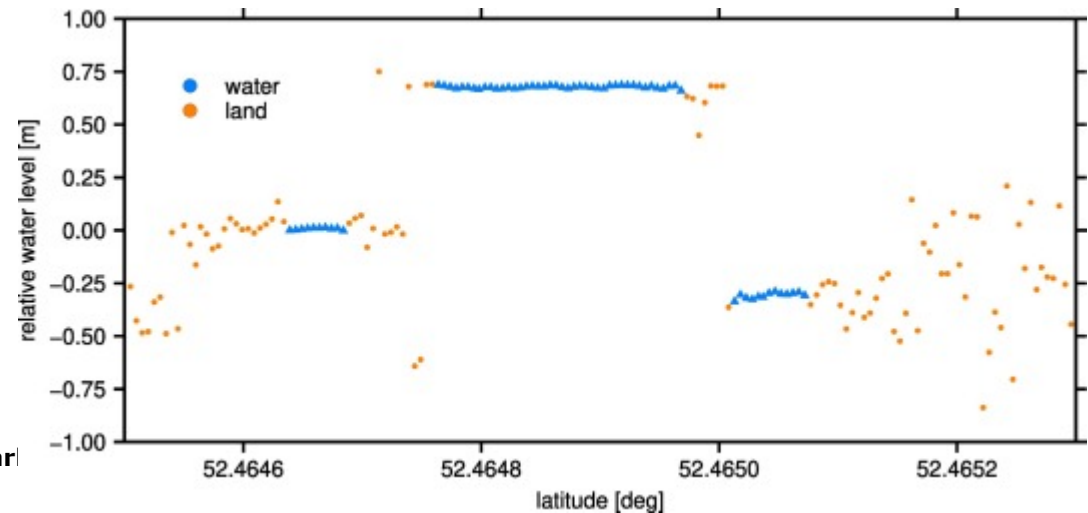
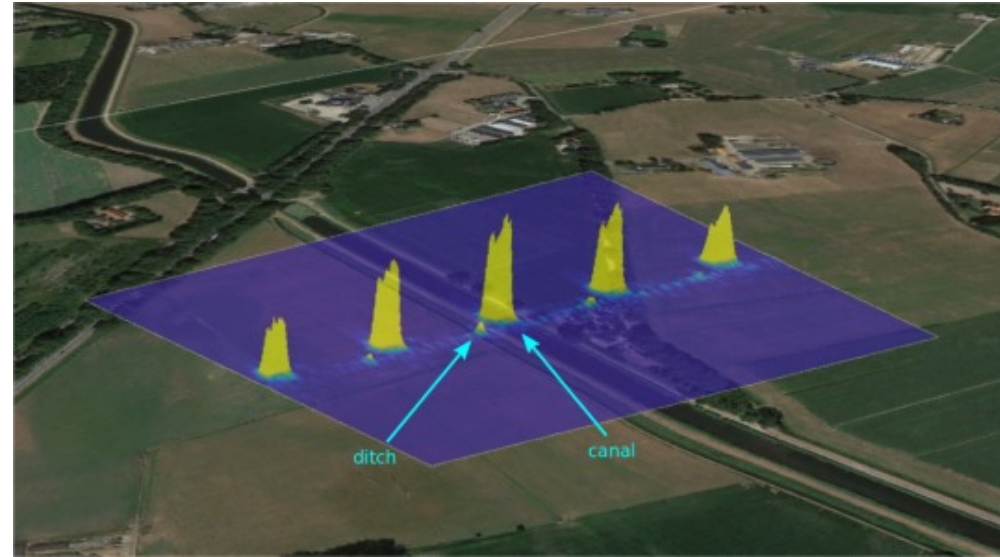


- Fully Focused SAR processing
- Coherent processing for ~2 seconds
- Resolution Along-Track ~ 0.5 m
- Pulse limited across-track
- Closed Burst
- PRF ~ 18 KHz

The main beam is 8 km in Radius, but if you use information from the side lobes the "total beam" can be considered to be much 3 x wider.

# Taking SAR to the limit. Fully Focused SAR-

- Target must be stable over 2 sec
- Ocean is NOT.....
- Inland water is.....



# Content

- Synthetic Aperture Radar.
  - Measurements
  - Theory

Interferometric SAR  
Topography  
Deformation.

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Multiple INSAR and Persistent Scatterers

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**Laser Altimetry (Heidi Ranndal).**