



THE DANISH NATIONAL SPACE CENTER IS A PART OF THE NEW TECHNICAL UNIVERSITY OF DENMARK

X-ray bursters

Course on Compact Objects Niels Bohr Institute (KU) 29 May 2007

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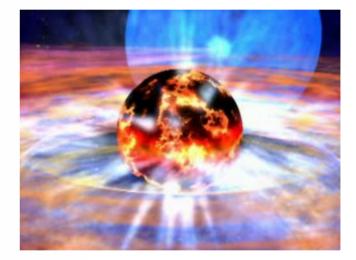
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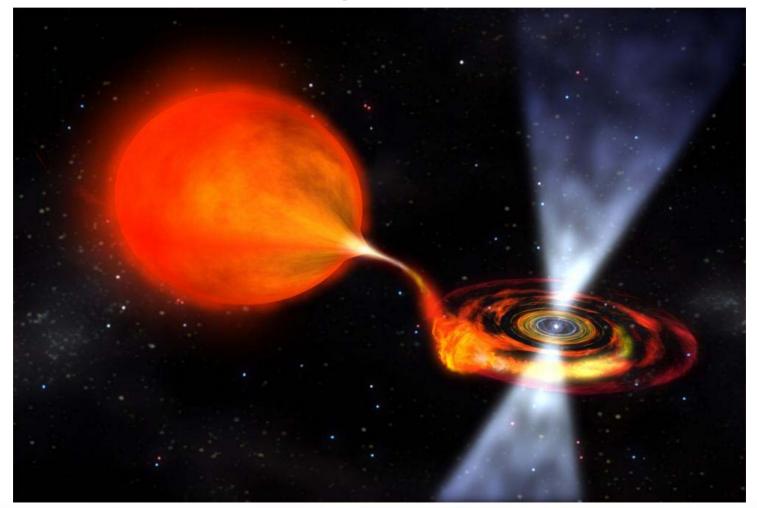
- 1.Neutron stars as X-ray bursters 1.1 LMXB 1.2 Type I vs. Type II X-ray bursts
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- 2.4 Recurrence intervals Accretion rate; burst parameters
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 - Accretion rate regimes Nuclear processes; H, He, H/He, and C burning
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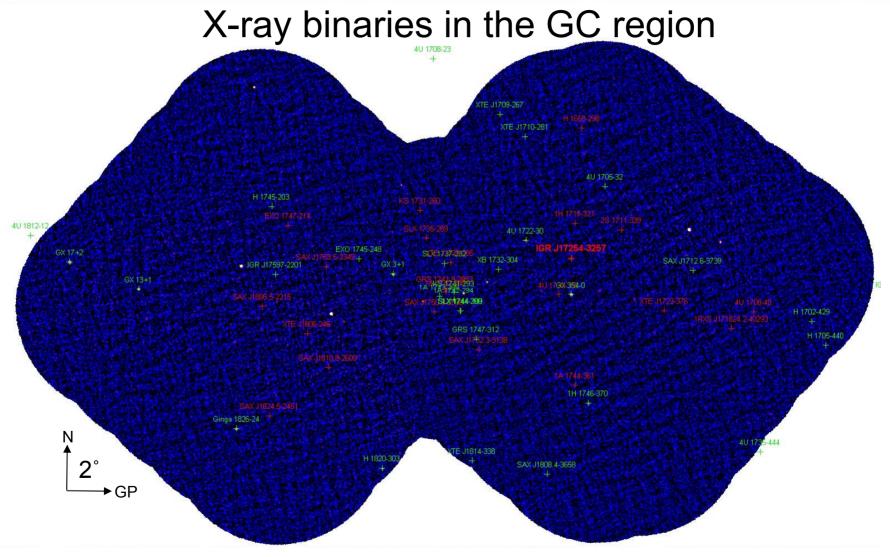


X-ray binaries









84 type I X-ray bursters known to date; ~2/3 located in the Galactic Bulge





Classification after the mass of the companion

Characteristics

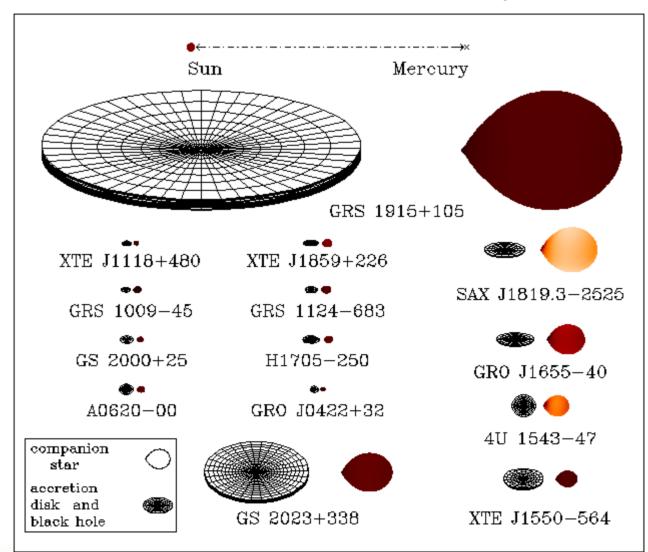
HMXB		LMXB	
X-ray spectra:	$kT \ge 15 \text{ keV} \text{ (hard)}$	$kT \leq 10 \text{keV}$ (soft)	
Type of time variability:	regular X-ray pulsations no X-ray bursts	only a very few pulsars often X-ray bursts	
Accretion process:	wind (or atmos. RLO)	Roche-lobe overflow	
Timescale of accretion:	10 ⁵ yr	10 ⁷ -10 ⁹ yr	
Accreting compact star:	high B-field NS (or BH)	low B -field NS (or BH)	
Spatial distribution:	Galactic plane	Galactic center and spread around the plane	
Stellar population:	young, age $< 10^7$ yr	old, age > 10^9 yr	
Companion stars:	luminous, $L_{opt}/L_x > 1$ early-type O(B) stars > 10 M_{\odot} (Pop. I)	faint, $L_{opt}/L_x \ll 0.1$ blue optical counterpart $\leq 1 M_{\odot}$ (Pop. I and II)	
	$M_{Comp} > M_{CO}$	$M_{Comp} < M_{CO}$	

IMXB: Intermediate-Mass X-ray Binaries (M_{comp} 1-10 M_☉)





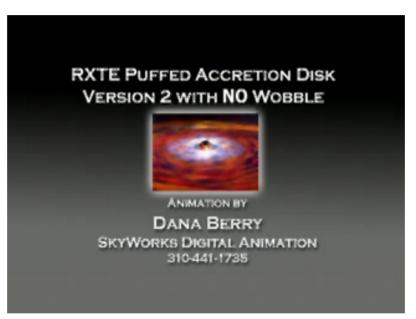
Black Holes have no surface \Rightarrow no X-ray bursts!







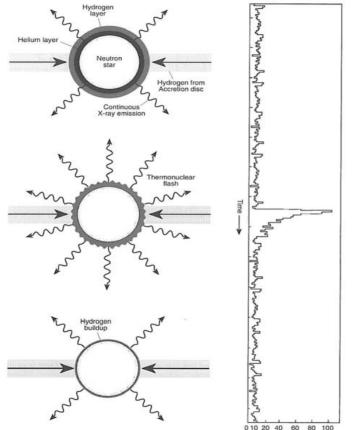
X-ray bursters



Type I X-ray bursts are thermonuclear explosions in the surface layers of a neutron star accreting H and/or He from the envelope of a companion star. Their emission is described by blackbody radiation with peak temperature ~ 2 keV and X-ray softening during the decay.

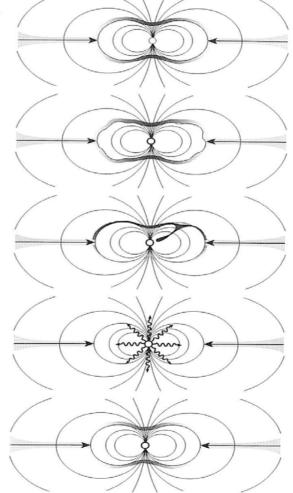






THERMONUCLEAR BURNING ON THE NEUTRON STAR 201

Fig. 8.19 Magnetospheric gate model of the Rapid Burster. Material accreting from the disc is held back (top panel) by the neutron star's magnetosphere. When enough material has built up outside this gate, the magnetosphere can no longer hold it and it ruptures (middle panel), thereby allowing it to fall onto the neutron star, producing a type II burst. With the material gone, the gate re-forms and the process starts again. (Diagram by Walter Lewin, MIT.)



TYPE II

THE KAPID BURSTER

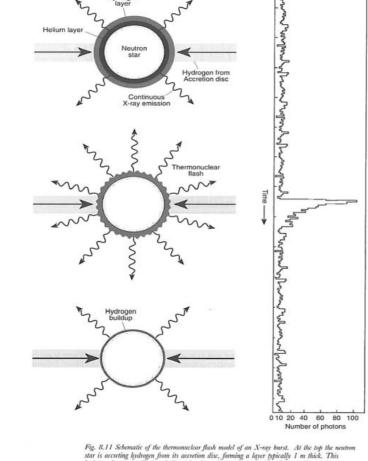


Fig. 9.11 Schematic of the thermonuclear flash model of an X-ray burst. At the top the neutron star is accreting hydrogen from its accretion disc, forming a layer typically 1 m thick. This hydrogen burns steadily into helium, forming a layer of comparable thickness. Exentually the conditions in the helium layer go critical and a thermonuclear flash takes place (centre panel). The process then begins again. (Diagram by Walter Lawin, MIT.)

TYPE I





3 33

Only 2 Type II X-ray bursters known so far: MXB 1730-335 (Rapid Burster) and the Bursting Pulsar GRO J1744-28 (no type I).

Rapid Burster
24-minute snapshots from 8 orbits on March 2/3,1976
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win et al. 1995 Eig. (1.19)

(Lewin et al., 1995, Fig. 4.19)

Bursting of the "Rapid Burster" 1730--335: Type I and Type Il bursts.

Type II bursts: magnetospheric gate model: B-field blocks accretion until gas pressure > magnetic pressure \Longrightarrow BOOM.

Low Mass X-ray Binaries

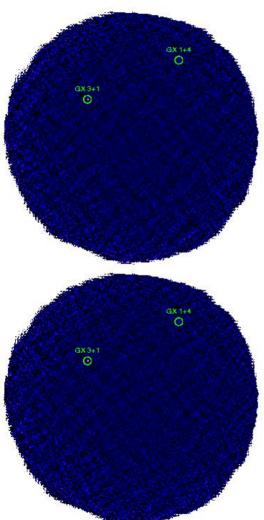
IAAI

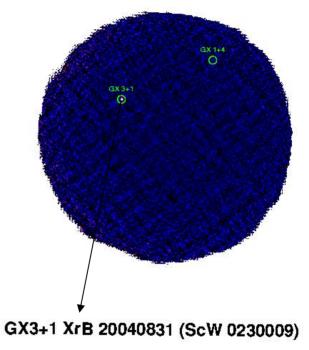
OBSERVATIONS





Example 1: X-ray burst detection in JEM-X images



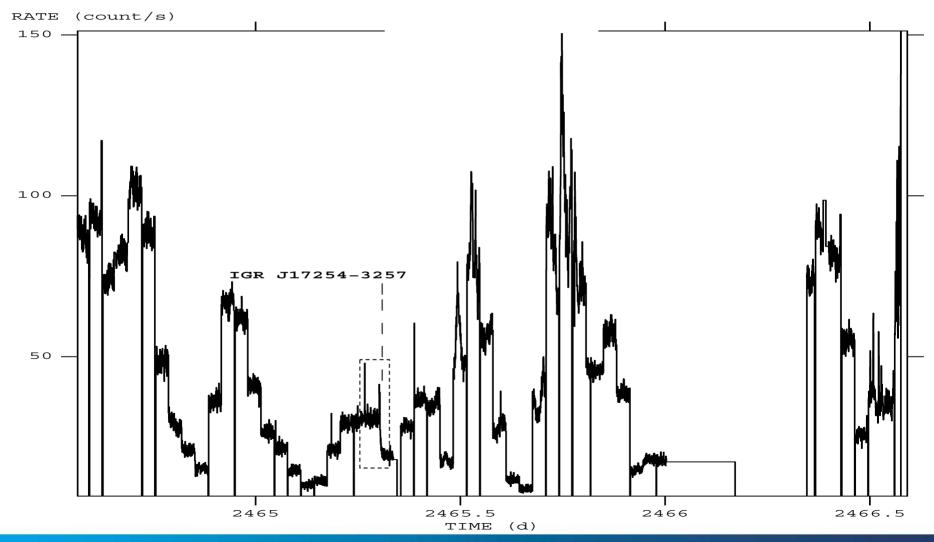


400s exposure 3-10 keV



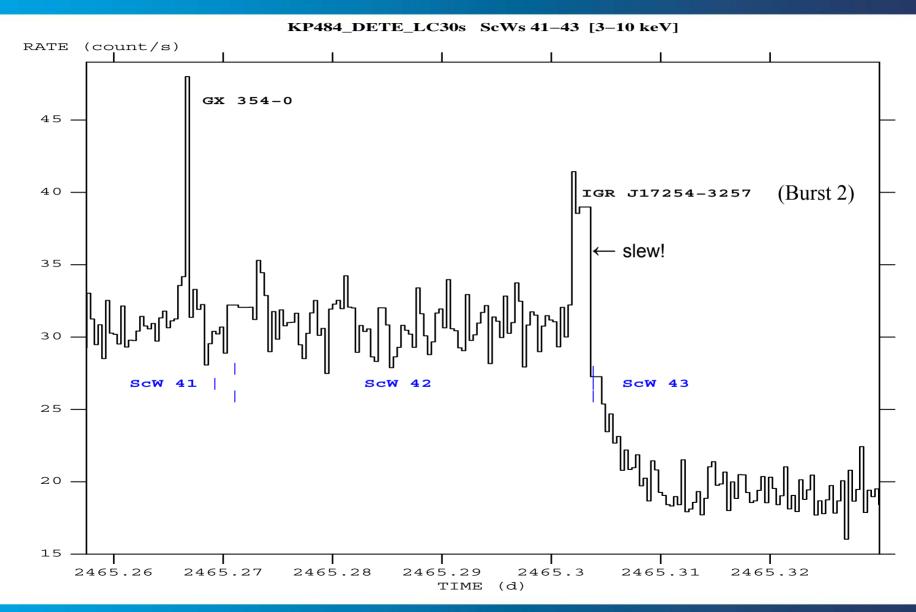


Example 2: JEM-X detector light curve (30s bins)



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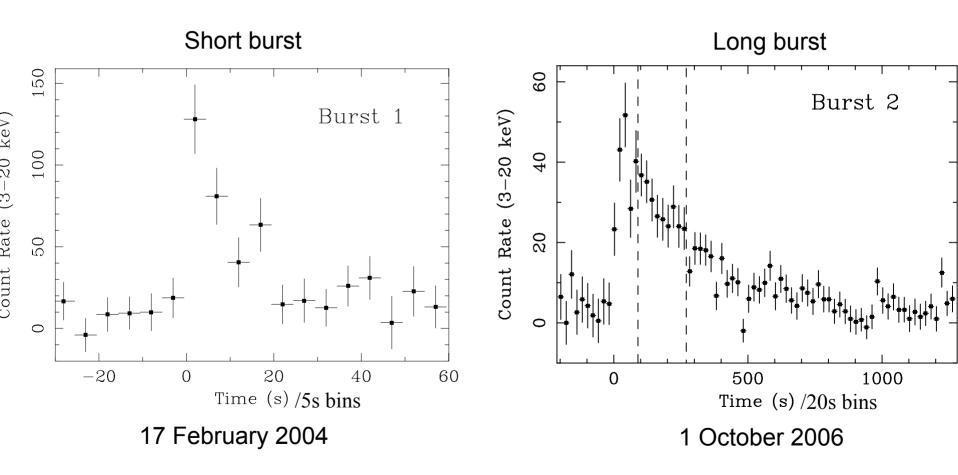








IGR J17254-3257 X-ray burst light curves







Light curves and hardness profiles

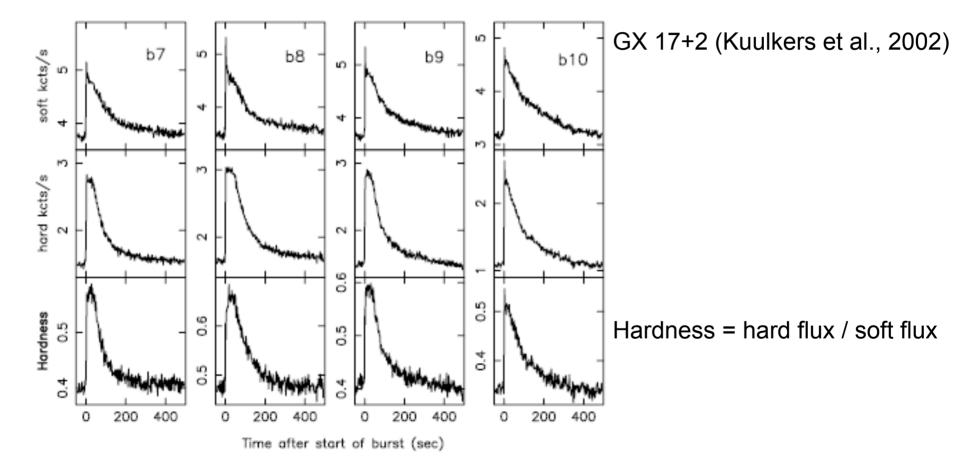
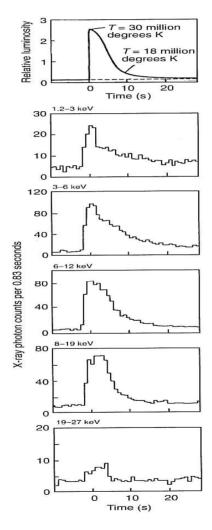






Fig. 8.9 X-ray burst profiles observed by SAS-3 in different energy bands from MXB1728-34. Note how in the lowest energies the burst persists for much longer (it has a tail), which does not happen at higher energies. This is because the radiating material cools significantly during the burst, as indicated in the theoretical burst profile shown at top. (Original diagram by Walter Lewin, MIT.)



Shorter tails at harder energies: Softening

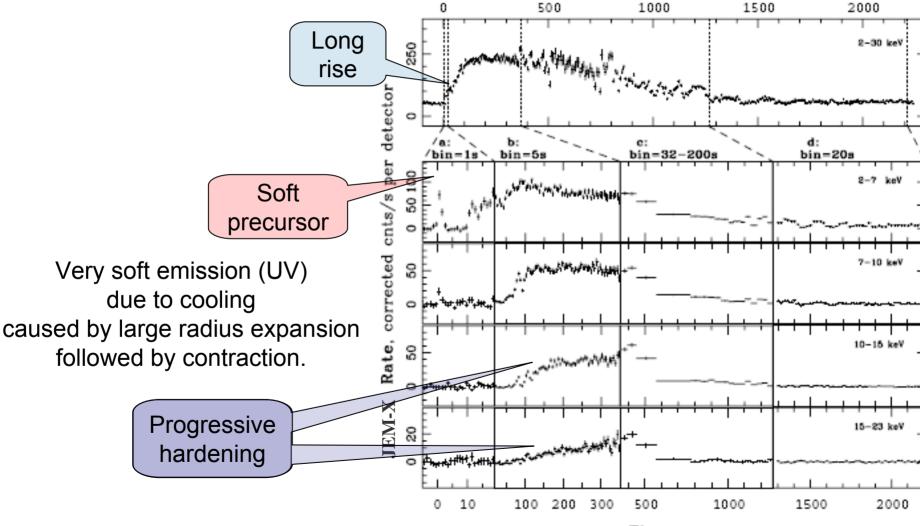
Exponential decay (e-folding time: τ) due to thermal conduction (Newton's law) \Rightarrow Cooling

Fluence:
$$E_b = \int_0^T F_{bol}(t) dt$$

 $\Rightarrow E_b = F_p \times \tau \left(1 - e^{-T/\tau}\right)$ (bolometric)

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S. Molkov et al.: INTEGRAL detection of a long powerful burst from SLX 1735-269 (2005)







Investigation method

Time resolved spectral analysis

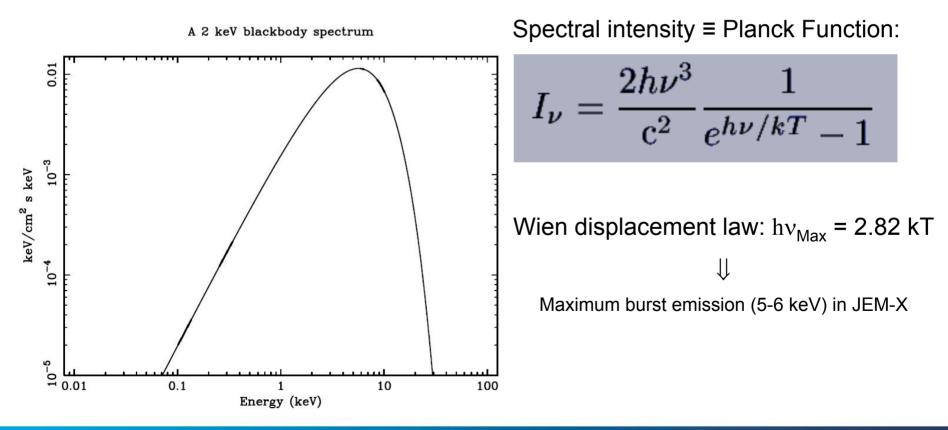
- Standard method: modelling of the net burst emission by blackbody (BB)
- 2-component method: modelling of the total burst emission by BB+PL (PL is fixed by pre-burst persistent emission)





Blackbody radiation

Type I X-ray bursts are characterized by a ≈ 2 keV (T $\approx 25 \cdot 10^6$ K) blackbody emission and exponential decay with cooling.



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Stefan-Boltzmann law

The total brightness of a black body is obtained from

$$\boldsymbol{B}(T) = \int_0^\infty B_\nu(T) \,\mathrm{d}\nu \tag{3.42}$$

... substituting $x = h\nu/kT$

$$=\frac{2h}{c^2}\left(\frac{kT}{h}\right)^4 \int_0^\infty \frac{x^3 \,\mathrm{d}x}{\exp(x) - 1} \tag{3.43}$$

... the integral has the value $\pi^4/15$

$$=\frac{2\pi^4 k^4}{15c^2 h^3}T^4 = \frac{ac}{4\pi}T^4 = \frac{\sigma_{\rm SB}T^4}{\pi}$$
(3.44)

Convert the brightness to the flux ($F = \pi B$), to obtain:

$$F = \sigma_{\rm SB} T^4 \tag{3.45}$$

the Stefan-Boltzmann law.

IAAT

And, yes, Boltzmann's first name is Ludwig, while Stefan's first name is Josef.

a is the radiation density constant,

$$a := \frac{8\pi^5 k^4}{15c^3 h^3} = 7.566 \times 10^{-15} \,\mathrm{erg} \,\mathrm{cm}^{-3} \,\mathrm{K}^{-4}$$
 (3.46)

also written as the Stefan-Boltzmann constant

$$\sigma_{\rm SB} := \frac{2\pi^5 k^4}{15c^2 h^3} = 5.671 \times 10^{-5} \, \rm erg \, cm^{-2} \, K^{-4} \, s \qquad (3.47)$$

Blackbody Radiation: Properties

3 - 13





Blackbody emission from a neutron star

Flux conservation: $L = \Phi$ $\Leftrightarrow 4\pi R_{BB}^2 \sigma T_{eff}^4 = 4\pi d^2 F_{BB}$ $\Leftrightarrow R_{BB} = \frac{d}{T_{eff}^2} \sqrt{\frac{F_{BB}}{\sigma}}$

(Stefan's law)

Caveats:

Burst emission is assumed isotropic (ξ =1)

Gravitational redshift effects $\begin{cases} L = L_{\infty}(1+z)^2 \\ T = T_{\infty}(1+z) \end{cases}$

$$\begin{bmatrix} I &= I_{\infty}(1+z) \\ R &= R_{\infty}(1+z)^{-1} \end{bmatrix}$$

What is actually observed is a "colour temperature"...





Deviations from blackbody emission of hot neutron stars ($kT > kT_{Edd} \approx 2.4$ keV)

- Nakamura et al., 1989: High energy tail due to comptonization of photons in a hot plasma around NS
- Lewin et al., Space Sci. Rev. 62 (1993):

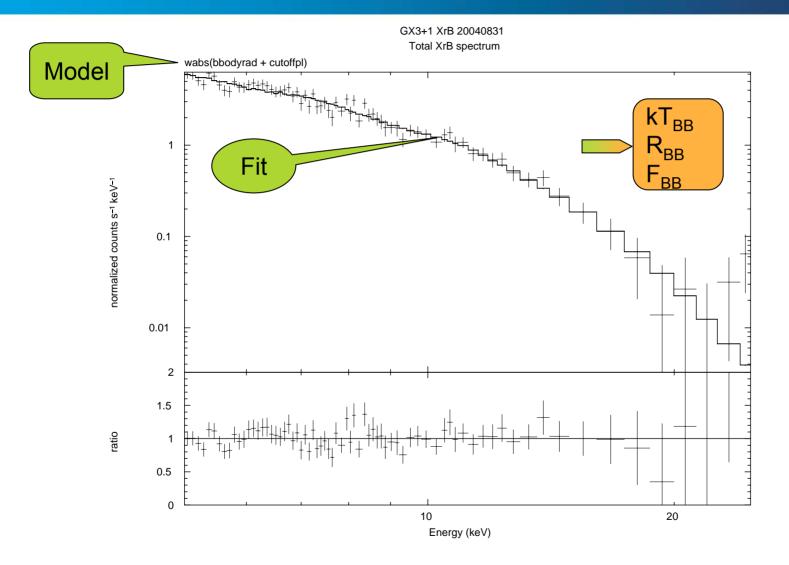
Modification of BB emission by electron scattering in the atmosphere of NS

► $T_{col} \approx 1.5 T_{eff} \Rightarrow R$ understimated by factor ≈ 2

• Strohmayer & Brown, ApJ 566 (2002): Reflection from accretion disk of 4U 1820-30 [suggested by Day & Dove, MNRAS 253 (1991)]



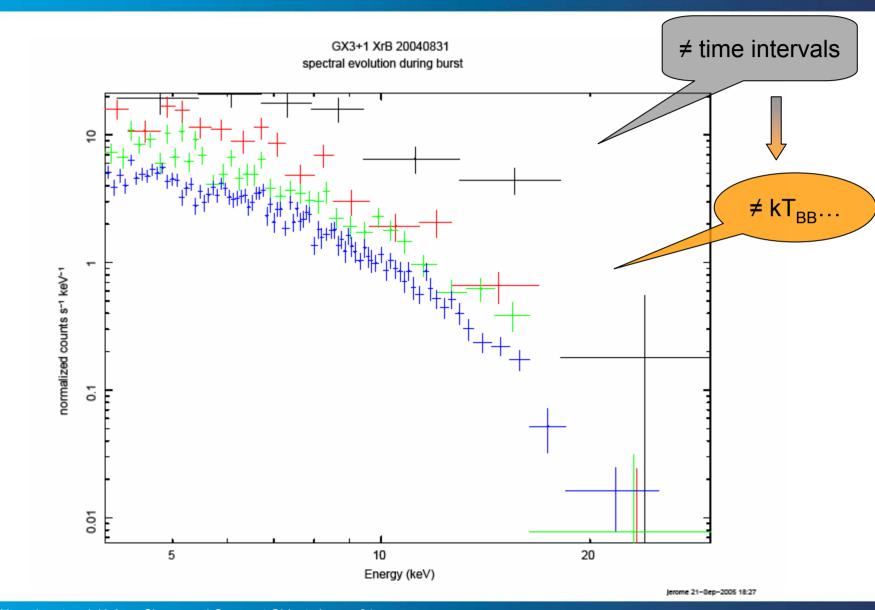




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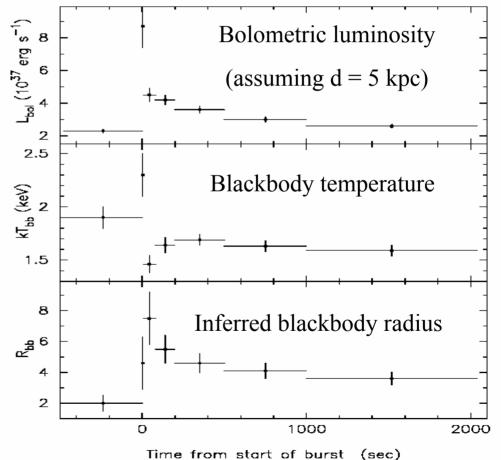






Results (Example 1)

The time resolved spectral analysis of GX 3+1 long X-ray burst reveals variations in the temperature and inferred blackbody radius which indicate expansion and contraction of the emission region.







Example 2: IGR J17254-3257 X-ray burst spectral analysis

Dataset	Burst 1		Burst 2			
Parameters	average	$_{\rm peak}$	decay	average		
$kT_{\rm bb}~({\rm keV})$	$1.4^{+0.5}_{-0.4}$	$1.6^{+0.3}_{-0.2}$	$1.2^{+0.3}_{-0.2}$	$1.3^{+0.2}_{-0.2}$		
$R_{\rm bb, d_{\rm Skpc}}$ (km)	12_{-6}^{+13}	6.4^{+3}_{-4}	$1.2^{+0.3}_{-0.2}$ 5.6^{+4}_{-2}	$5.1^{+2.2}_{-2}$		
χ^2/dof	12/10	48/49	48/42	59/47		
F_{bol} ^a	8.9	4.9	1.0	1.1		
Burst parameters						
F_{peak}	$\simeq 20$		$\simeq 12$			
fb ^b	2.6×10^{-7}		2.6×10^{-6}			
τ^{c}	13		216			
γ^{d}	0.006		0.009			

^{*a*} Unabsorbed flux (0.1–100 keV) in units of 10^{-9} erg cm⁻² s⁻¹. ^{*b*} Fluence (erg cm⁻²). ^{*c*} $\tau(sec) \equiv f_{\rm b}/F_{\rm peak}$. ^{*d*} $\gamma \equiv F_{\rm pers}/F_{\rm peak}$; $F_{\rm pers} = 1.1 \times 10^{-10}$ erg cm⁻² s⁻¹ (0.1–100 keV).



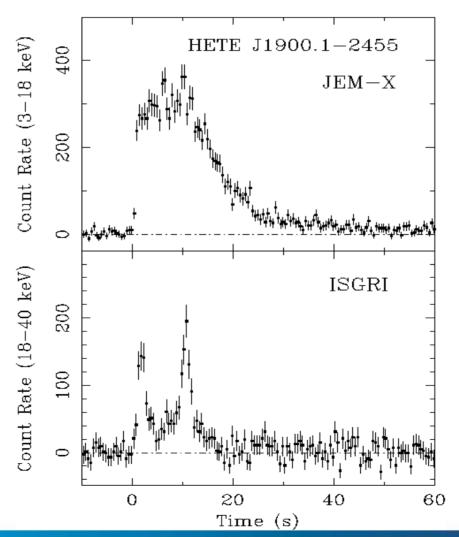


Photospheric Radius Expansion





Radius expansion burst from GX 354-0 observed by INTEGRAL (Falanga et al., 2006)







Radius expansion burst from GX 3+1 (Kuulkers & van der Klis, 2000)

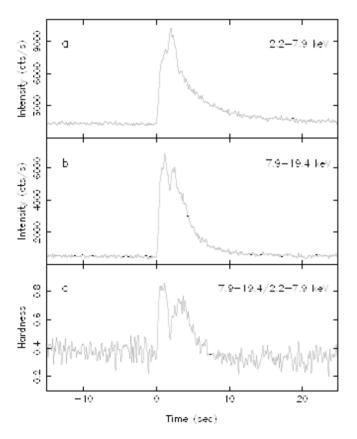


Fig. 2. The X-ray burst light curve at low (a.) and high (b.) energies and the corresponding hardness curve (c.), all at a time resolution of 0.125 sec. T=0 s corresponds to 1999 August 10, 18:35:53.5 UTC.

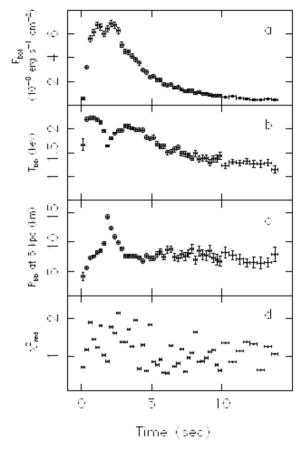
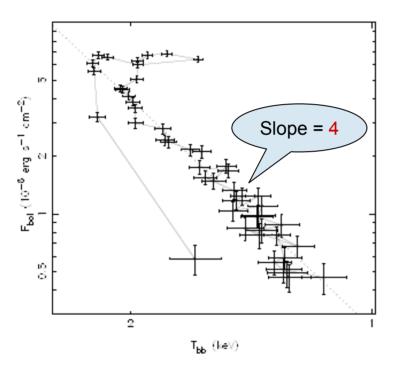


Fig. 3. Spectral fit results during the burst: (a) bolometric blackbody flux, $F_{\rm bol}$, (b) black-body temperature, $T_{\rm bb}$, (c) effective black-body radius, $R_{\rm bb}$, at 5 kpc, and (d) goodness of fit expressed in reduced χ^2 .





Blackbody cooling track and Stefan's law: $F \sim S \times T^4$



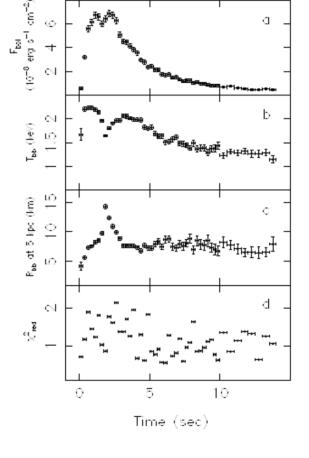
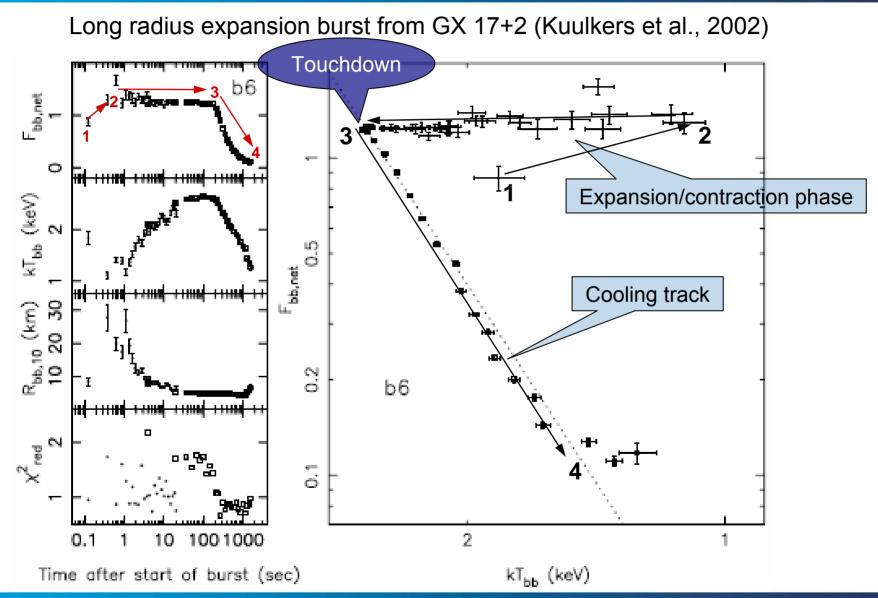


Fig. 4. Bolometric black-body flux ($F_{\rm bol}$) versus black-body temperature ($T_{\rm bb}$) for the first 14 s of the burst. Data points are connected for clarity. The dotted line represents the fit to the cooling track of the burst, see text. Note that $T_{\rm bb}$ runs from right to left.











Eddington Limit

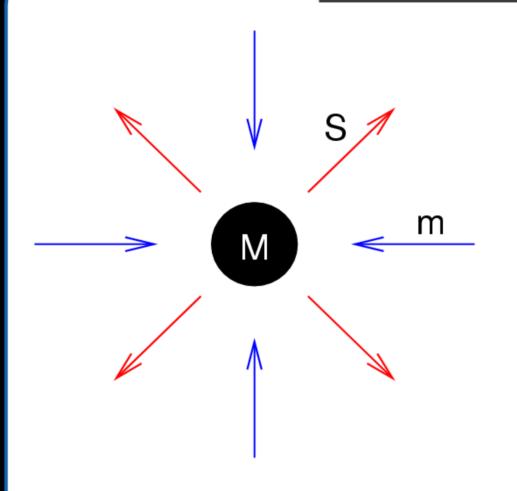
For any luminous object, there is a maximum luminosity beyond which radiation pressure will overcome gravity, and material outside the object will be forced away from it rather than falling inwards.

For canonical NS parameters (R_{NS} = 10 km, M_{NS} = 1.4 M_{\odot})

- Eddington luminosity
- Eddington temperature
- Eddington accretion rate



Eddington luminosity, IV



Assume mass M spherically symmetrically accreting ionized hydrogen gas.

At radius r, accretion produces energy flux S.

Important: Interaction between accreted material and radiation!

Accretion Luminosity



Eddington luminosity, VIII



Force balance on accreted electrons and protons: Inward force: gravitation:

$$F_{g} = \frac{GMm_{p}}{r^{2}} \tag{4.5}$$

Outward force: radiation force:

$$F_{\rm rad} = \frac{\sigma_{\rm T}S}{c} \tag{4.6}$$

where energy flux S is given by

$$S = \frac{L}{4\pi r^2} \tag{4.7}$$

where *L*: luminosity. *Note:* $\sigma_T \propto (m_e/m_p)^2$, so negligable for protons. *But:* strong Coulomb coupling between electrons and protons $\implies F_{rad}$ also has effect on protons!

Accretion Luminosity



Eddington luminosity, IX

Accretion is only possible if gravitation dominates: $\frac{GMm_{\rm p}}{r^2} > \frac{\sigma_{\rm T}S}{c} = \frac{\sigma_{\rm T}}{c} \cdot \frac{L}{4\pi r^2}$ (4.8)and therefore $L < L_{\mathsf{Edd}} = \frac{4\pi G M m_{\mathsf{p}} c}{\sigma_{\mathsf{T}}}$ (4.9)or, in astronomically meaningful units $L < 1.3 imes 10^{38} \, \mathrm{erg} \, \mathrm{s}^{-1} \cdot rac{M}{M_{\odot}}$ (4.10)where L_{Edd} is called the Eddington luminosity. But remember the assumptions entering the derivation: spherically symmetric accretion of fully ionized pure hydrogen gas. For pure He: L_{Edd} =2.9x10³⁸ erg s⁻¹

Accretion Luminosity



(for η

Eddington luminosity, X

Characterize accretion process through the accretion efficiency, $\eta = \frac{GM}{Rc^2}$: $L = \frac{GM}{R} \frac{dM}{dt} \Rightarrow L = \eta \cdot \dot{M}c^2$ (4.11) where \dot{M} : mass accretion rate (e.g., g s⁻¹ or M_{\odot} yr⁻¹).

Therefore maximum accretion rate ("Eddington rate"):

$$\dot{M}_{Edd} = \frac{L_{Edd}}{\eta c^2} \sim 2 \times 10^{-8} \qquad M_{\odot} \text{ yr}^{-1}$$
(4.12)
= 0.2)
Per unit area: $\dot{m}_{Edd} = \frac{\dot{M}_{Edd}}{4\pi R^2} = 10^5 \text{ g cm}^{-2} \text{ s}^{-1}$

Peak Temperature (at "touchdown"):
$$T_{Edd} = \left(\frac{L_{Edd}}{4\pi R_{NS}^2 \sigma}\right)^{\frac{1}{4}}$$

Accretion Luminosity

4–7





Applications

Relativistic formula for $\mathrm{L}_{\mathrm{Edd}}$:

$$L_{Edd} = 1.9 \cdot 10^{38} \times \frac{M}{M_{\odot}} \times \frac{1 + (\alpha T)^{0.86}}{1 + X} \times \frac{1.31}{1 + z(R)} \text{ erg/s}$$
$$z(R) = \left(1 - \frac{2 G M_{NS}}{R c^2}\right)^{-\frac{1}{2}} - 1 = 0.31 \text{ (a) } R = R_{NS}$$

X : H fraction, $\alpha \approx 2.2 \times 10^{-9}$ K⁻¹ : e⁻ scattering opacity coefficient of the atmosphere

Observationally (globular clusters): $L_{Edd} \approx 3.8 \times 10^{38} \text{ erg/s}$ (Kuulkers et al., 2003)

- > Determination of the redshift $z \Rightarrow M_{NS}$
- \succ X-ray bursts as standard candles: if L= $\rm L_{Edd} \,{\Rightarrow}\, d$

$$L \leq L_{Edd} \iff 4 \pi d^2 F \leq L_{Edd}$$
$$\iff d \leq \sqrt{\frac{L_{Edd}}{4\pi F}}$$

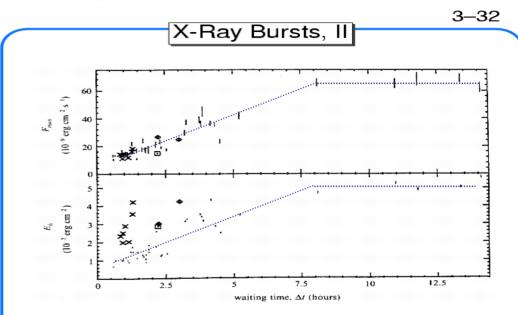
: upper limit to distance





Burst intervals and burst energy

The released energy is limited by PRE and indicates limited nuclear fuel due to steady nuclear burning between bursts.



(Lewin et al., 1995, Fig. 4.10)

Peak flux and total fluence of bursts are correlated with distance to the next burst. *Explanation*: Accretion of hydrogen onto surface \implies hydrogen burns quietly into helium (thickness of layer $\sim 1 \text{ m}$) \implies thermonuclear flash when critical mass reached

Low Mass X-ray Binaries

IAA





Recurrence time

1. Bursts are fuelled by accreted material at rate $\frac{dM}{dt} = \dot{M}$ Energy 2. Mass burned during a burst is given by: $M_b = \frac{E_b}{\varepsilon}(1+z)$; ε : burning efficiency [erg \cdot g⁻¹] 3. Recurrence time between bursts is then: $\Delta t = \frac{M_b}{\dot{M}} = \frac{E_b}{L_{pers}} \times \frac{\eta c^2}{\varepsilon} \times (1+z)$

 $\Delta t \propto (L_{pers})^{-1}$ should reflect the time needed to accumulate the nuclear burning fuel

But things are not that simple...





Burst parameters

 $\alpha = \frac{F_{pers}}{E_{b}} \Delta t \quad 10 < \alpha < 10^{3} : \text{a measure of burst energetics}$ $\gamma = \frac{F_{pers}}{F_{peak}} : \text{burst strength relative to persistent emission}$

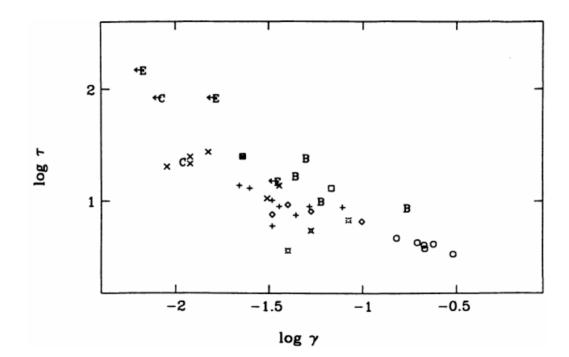
Effective burst duration: $\tau = \frac{E_b}{F_{peak}}$ ~ e-folding decay time

Note:
$$\frac{\alpha \tau}{\gamma} = \Delta t$$





Burst parameter relationships: τ vs. γ

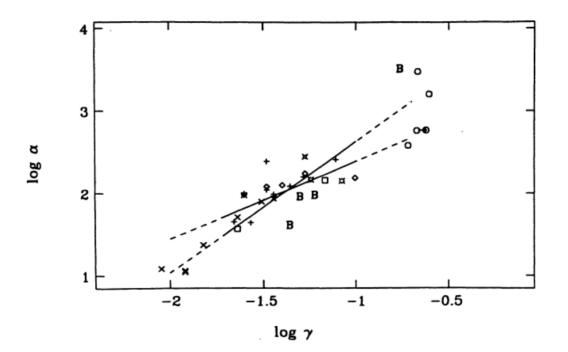


The decrease of burst duration with persistent luminosity indicates that hydrogen becomes less important in the energetics of the burst as the mass accretion rate increases (Van Paradijs et al, 1988).





Burst parameter relationships: α vs. γ



The correlation of α with γ is consistent with previous conclusion and seems to indicate that steady nuclear burning limiting the burst energy release does increase with accretion rate (Van Paradijs et al, 1988).





Preliminary interpretation

- The previous records seem to indicate a transition between two nuclear burning regimes.
- Evidences of increasing time between bursts as persistent emission increases may indicate an increase of the accretion area implying that the local accretion rate per unit area, m, actually decreases with the accretion rate M.
- The influence of the accretion rate per unit area is an indication that only a fraction of the NS is covered by freshly accreted fuel.





X-ray burst oscillations

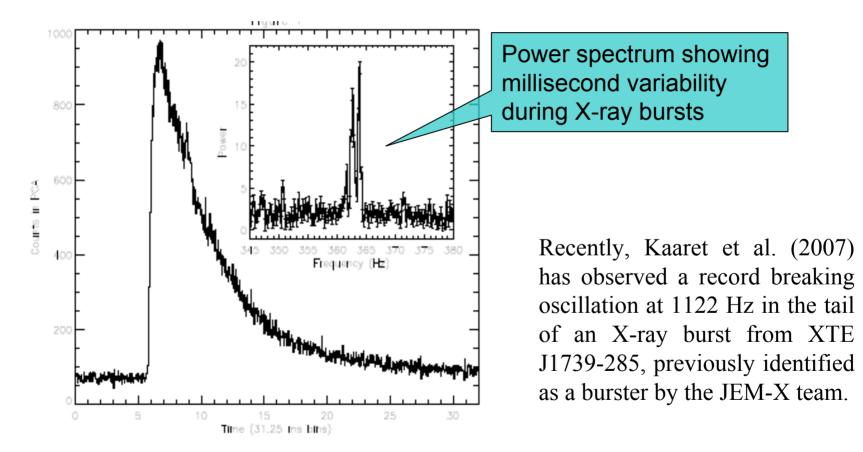


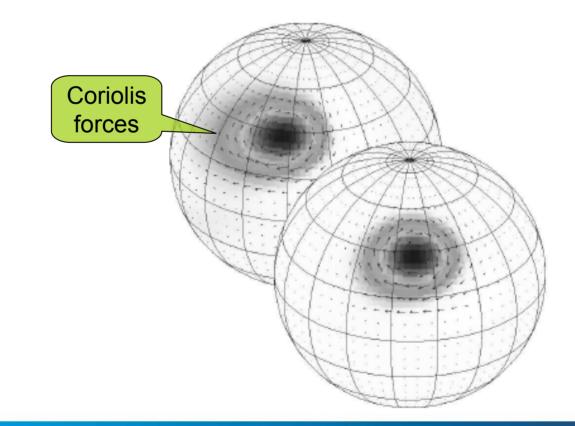
Fig. 3.6. An X-ray burst from 4U 1728–34 observed with the PCA onboard RXTE. The main panel shows the X-ray counts observed by the PCA in (1/32) s bins. The inset panel shows the power spectrum in the vicinity of 363 Hz (after Strohmayer et al. 1996).





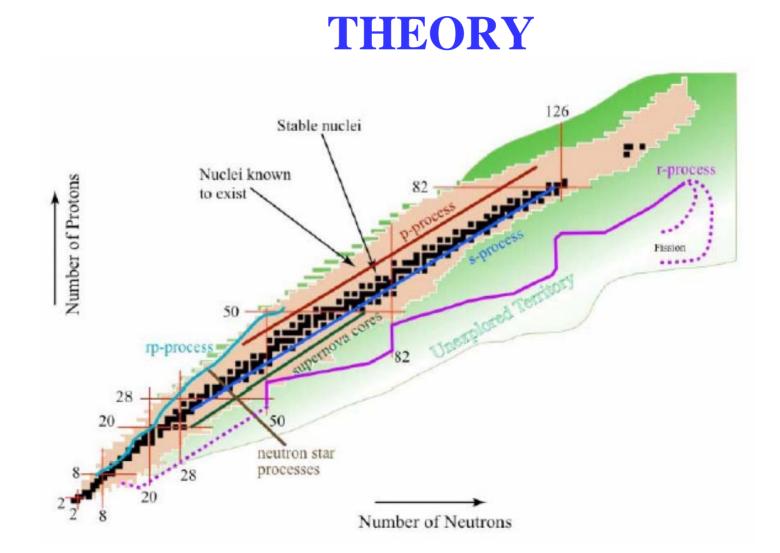
Spin modulation

Oscillations are associated with a hot spot expanding on the NS surface like a deflagration flame and modulated by the NS rotation.













More or less long bursts

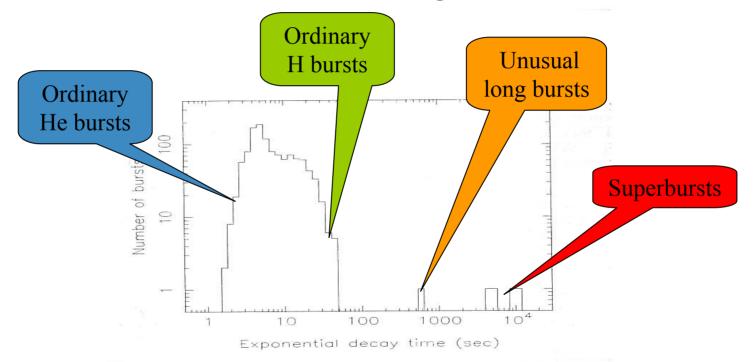
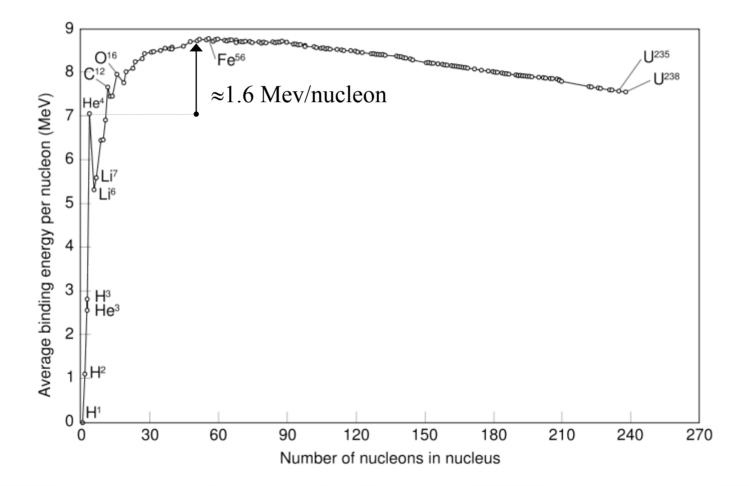


Figure 1. The distribution of the decay times of 1158 X-ray bursts seen by the BeppoSAX/WFCs. The decay times are determined from exponential fits to the burst decay profiles. Courtesy: the BeppoSAX/WFC team at SRON/Utrecht and CNR/Rome.





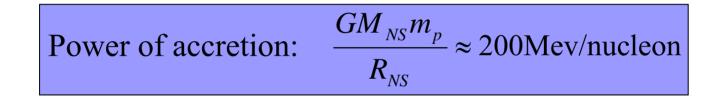
Burst Energetics







Nuclear vs. gravitation



Energy release of nuclear burning to heavy elements is ≈1.6 Mev/nucleon for pure He and ≈5 Mev/nucleon for solar composition material

 \Rightarrow Ineffective process compensated by accumulation





Nuclear burning regimes

 $m < 900 \text{ g/cm}^2/\text{s}$: Mixed H/He burning triggered by thermally unstable H ignition.

Long burst duration (> 100s - 1000s) due to rp- process. $\alpha \approx 150$ cm²/s : H stable burning (hot CNO cycle) to He \Rightarrow Pure He flash (3- α). Frequent PRE. $\alpha \approx 200$. stability 006 • $\geq 2000 \text{ g/cm}^2/\text{s}$: H stable burning (hot CNO cycle) to He \Rightarrow Pure He flash (3- α). Frequent PRE. $\alpha \approx 200$.

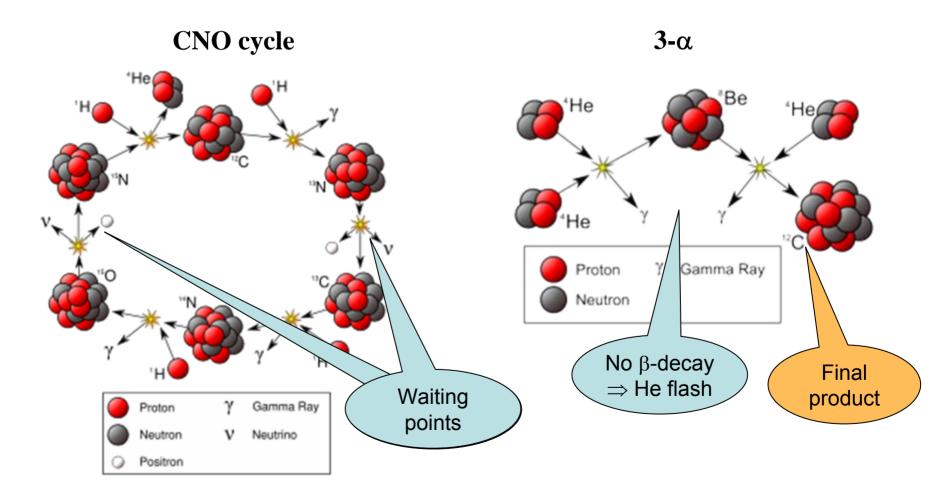
•2000 $\frac{1}{2}$ /cm²/s < \dot{m} < \dot{m}_{Edd} : Mixed H/He burning triggered by thermally unstable He ignition. Burst duration > 10s due to rp- process. α ~20-100.

- $m \ge m_{Edd}$: No bursts (e.g. pulsars).
- Pure He accretion (e.g. from white dwarf) \Rightarrow powerful pure He bursts.
- Deep Carbon burning in superbursts.





Nucleosynthesis







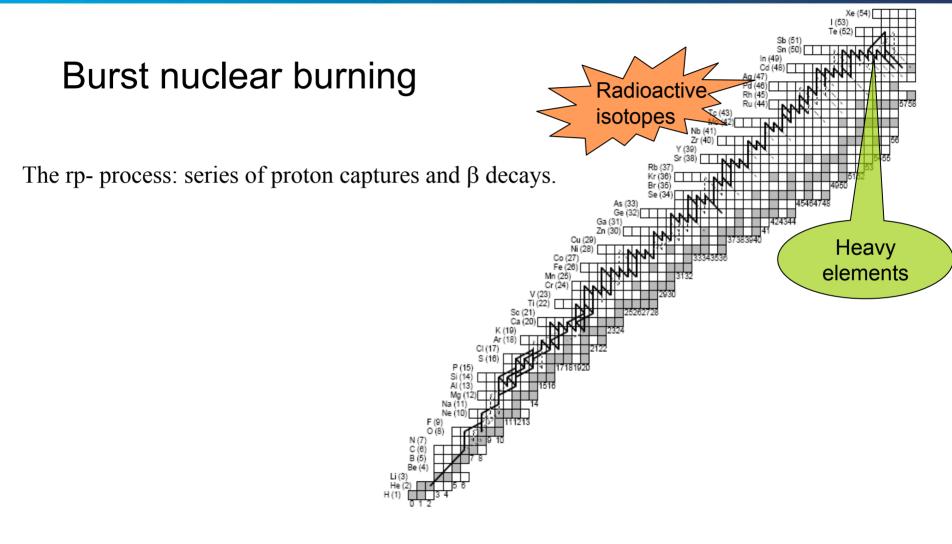


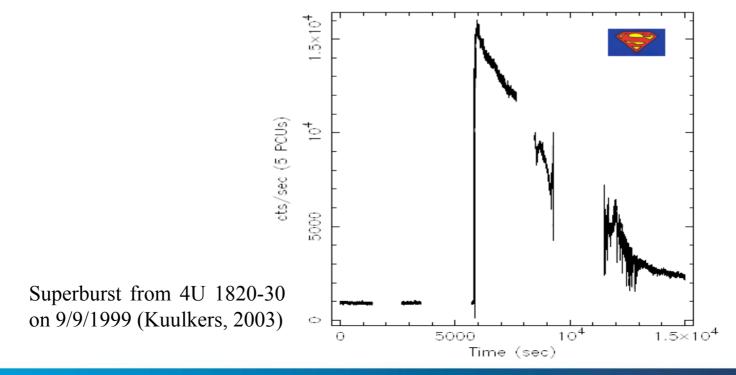
Fig. 3.1. Schematic showing the dominant pathways of the nuclear reaction flows during the rp process. Elements far beyond ⁵⁶Fe can easily be reached. Filled squares denote stable nuclides (after Schatz et al. 2001).





Superbursts

Compared to normal type I X-ray bursts, superbursts are ~1000 times more energetic ($E_b \approx 10^{42}$ ergs), ~1000 times longer (from hours to half a day), and have recurrence times of the order of years. They are very rare, only 13 such events having been found from 8 sources.



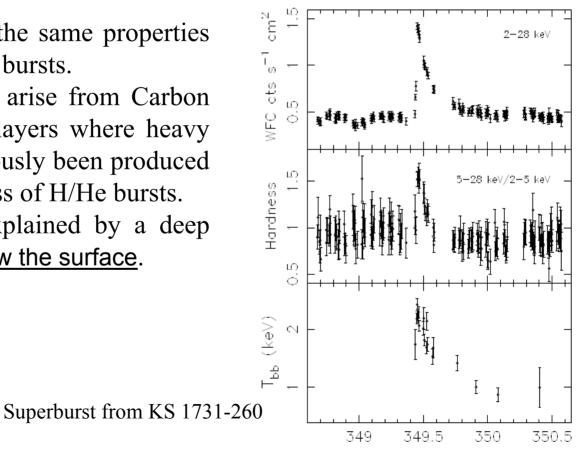




Superbursts II

Superbursts display the same properties as usual type I X-ray bursts.

They are thought to arise from Carbon shell flashes in the layers where heavy elements have previously been produced through the rp-process of H/He bursts. Their duration is explained by a deep ignition column <u>below the surface</u>.



Days (MJD-50000)





Unusually long bursts

Only 8 known bursts have shown a duration of a few tens of minutes

Unusually long bursts seem generally to be associated with mixed H/He burning at low accretion rate.

Depending on the actual accretion rate, either the burning of a large amount of H is triggered by an He flash, or a large column of He is triggered by H ignition.

Long pure He bursts involving an even larger column depth are also possible, especially if no H is accreted.

An aborted superburst due to the premature ignition of a carbon layer triggered by an He detonation may also be considered.





Burst triggering Mechanisms



 10^{9}

 10^{8}

1000

100

10

1.00

0.10

0.01

⁴He

 ^{1}H

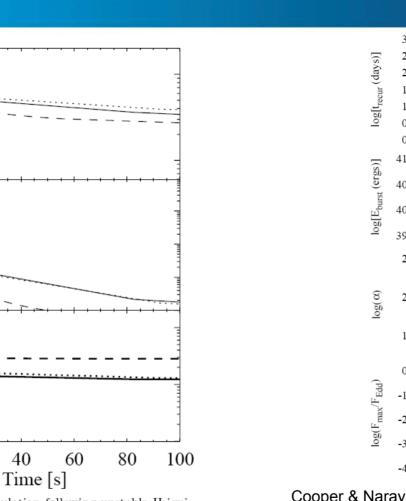
20

0

T[K]

 $F_{\rm cool}$ $/F_{\rm acc}$

 $X(^{1}\mathrm{H}), X(^{4}\mathrm{He})$





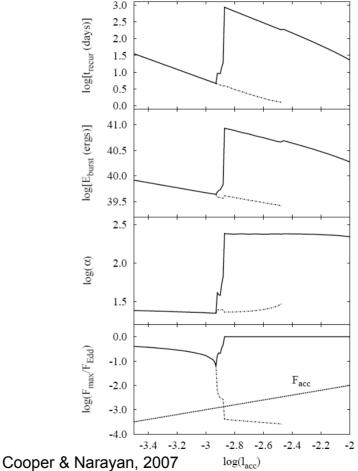
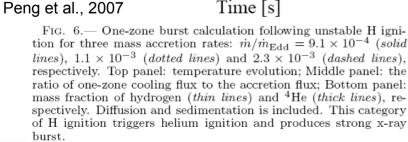


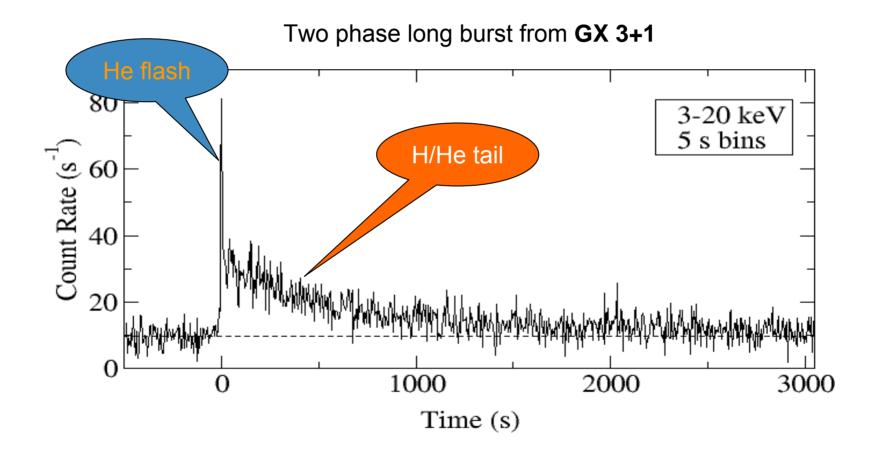
FIG. 7.— Recurrence time, burst energy, ratio of accretion to burst energy α , and peak flux of type I X-ray bursts as a function of $l_{\rm acc}$, from top to bottom. For $-2.9 \lesssim \log(l_{\rm acc}) \lesssim -2.5$, both energetic pure helium flashes and weak hydrogen flashes occur. In this case, the solid line denotes the burst properties of the helium flashes. The chaotic behavior discussed in §4 and Fig. 5 causes the sudden jumps in the panels that occur in the range $-2.93 < \log(l_{\rm acc}) < -2.87$. The dashed line in the bottom panel denotes the luminosity due to accretion. Note that the peak flux during most weak hydrogen flashes is much less than excretion luminosity.







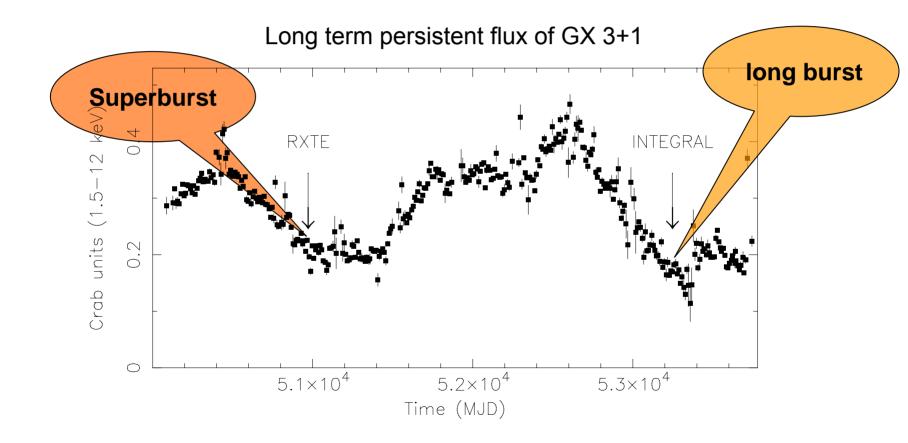
Back to observations







Relation with accretion rate

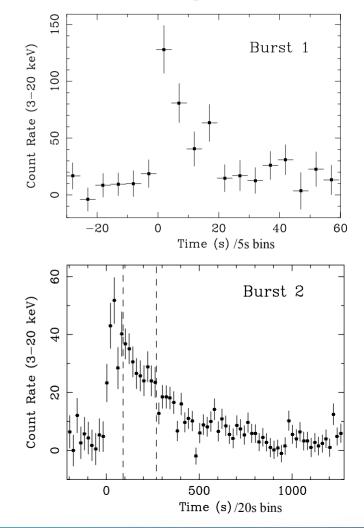






IGR J17254-3257 short and long bursts

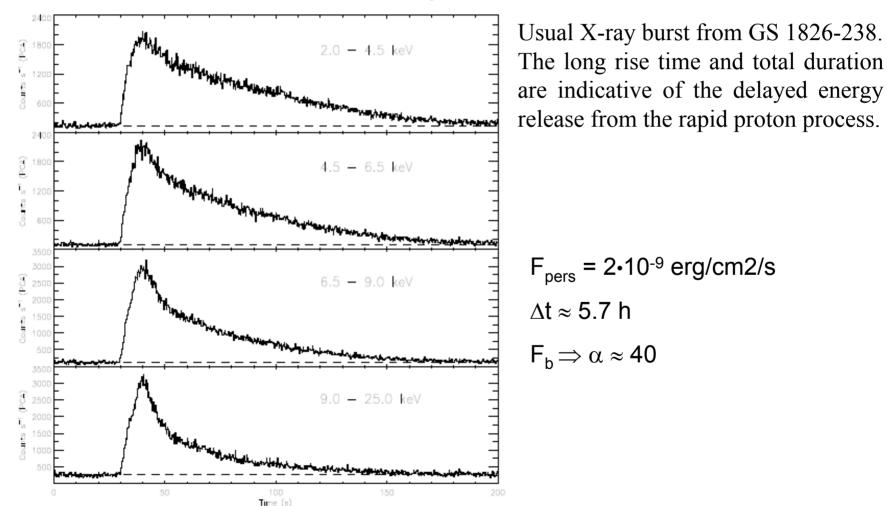
Different lasting bursts from IGR J17254-3257 can be explained by a transition between two slightly different accretion rates. Burst 1 is a mixed H/He burst triggered by a weak H flash, while burst 2 is the result of the burning of a large He pile at a slightly higher accretion rate.







Practical example: GS 1826-24







Some calculations (1/3)

$$\dot{m} = \frac{M}{4\pi R_{NS}^2} \qquad \dot{M} = \frac{L_{pers}}{\eta c^2} \qquad L_{pers} = 4\pi d^2 \xi_p F_{pers} \qquad \xi_p \approx 1 : \text{ anisotropy}$$
$$\dot{m} = \left(\frac{d}{R_{NS}}\right)^2 \frac{F_{pers}}{\eta c^2} = \frac{10^4 \text{ g cm}^{-2} \text{ s}^{-1}}{0.1 \text{ m}_{Edd}}: \text{ Mixed H/He burning triggered by He ignition}$$

Ignition column depth: $y = m \Delta t$ $y = 2 \times 10^8 \text{ g cm}^{-2}$





Some calculations (2/3)

$$\alpha = \frac{F_{\text{pers}}}{F_{\text{b}}} \Delta t$$

$$\Delta t = \frac{E_{\text{b}}}{L_{\text{pers}}} \frac{\eta c^{2}}{\varepsilon} (1+z) = \frac{\xi_{\text{b}}}{\xi_{p}} \frac{F_{\text{b}}}{F_{\text{pers}}} \frac{\eta c^{2}}{\varepsilon} (1+z)$$

$$\alpha = \frac{\xi_{\text{b}}}{\xi_{p}} \frac{\eta c^{2}}{\varepsilon} (1+z) \Leftrightarrow \varepsilon = \frac{\xi_{\text{b}}}{\xi_{p}} \frac{\eta c^{2}}{\alpha} (1+z)$$

$$\varepsilon \approx 5 \times 10^{18} \text{ erg g}^{-1} \quad \text{for } : \frac{\xi_{\text{b}}}{\xi_{p}} \approx 0.85$$

Energy efficiency: $\varepsilon = Q_{nuc} \times 10^{18} \text{ erg g}^{-1}$

$$Q_{nuc} \approx 1.6 + 4X \text{ Mev/nucleon}$$

$$\Rightarrow Q_{nuc} \approx 5 \text{ Mev/nucleon} \Leftrightarrow X \approx 0.8 : \text{H-rich burst}$$





Some calculations (3/3)

Mass burned:
$$m = 4\pi R_{_{NS}}^2 y = 2.5 \times 10^{21} g$$

Burst energy release:

$$E_{\rm b} = \frac{m}{1+z} \varepsilon$$
$$E_{\rm b} \approx 10^{40} \, ergs$$

m





OUTLOOK

X-ray bursts as probes of:

- Compact object as neutron star
- Neutron stars properties (M_{NS}, R_{NS}, T_{NS}, spin)
- Accretion rate
- Evolutionary state (H/He) of the companion

Future prospect: • Nuclear lines





THE END