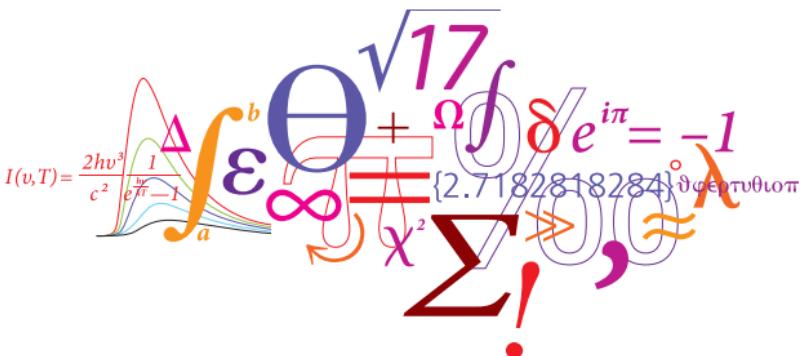


# Recent secular variation and core motions: Complementary constraints from ground observatories and the Swarm satellite constellation

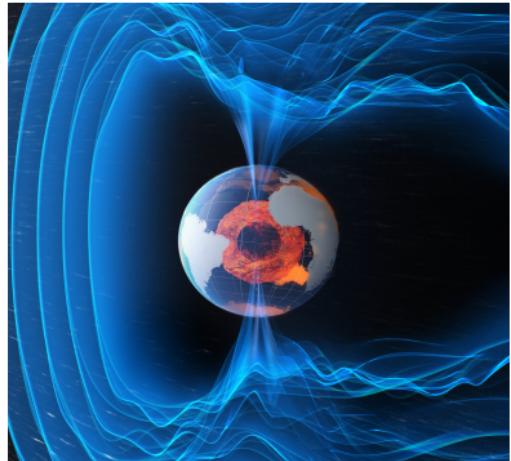
Chris Finlay

*DTU Space, Technical University of Denmark*


$$I(v,T) = \frac{2hv^3}{c^2} \frac{1}{e^{\frac{hv}{kT}} - 1}$$
$$\int_a^b \Sigma \Theta + \Omega \delta e^{i\pi} = -1$$
$$\zeta(s) = \sum_{n=1}^{\infty} \frac{1}{n^s}$$
$$\theta = \sqrt{17}$$
$$\delta = \{2.7182818284\}^{\circ}$$
$$\lambda = \text{θφερτυθιοπ}$$

# Exploring core motions using geomagnetic secular variation

- > 98% Earth's **B** field originates in the core
- Provides protection from the solar wind
- Generated by **dynamo action** in the core
- Not steady; continuously changing  
-> Secular Variation (SV)



[Image credit: ESA]

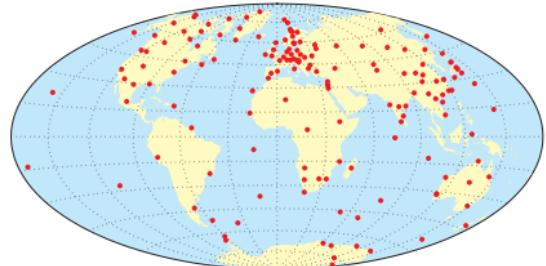
## Outstanding scientific questions

- Structure of flows responsible for generating, and driving the evolution, of the field?
- Origin of core field changes on timescales of decades and less?

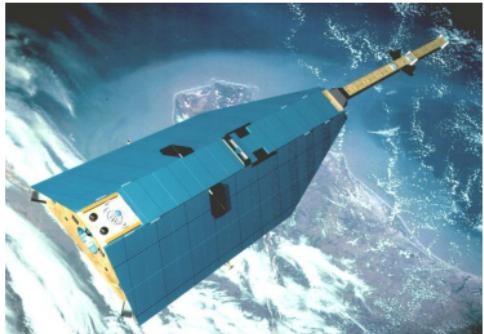
This talk: recent findings using latest ground observatory and *Swarm* data

# Geomagnetic field observations

- Ground observatories:



- Low Earth Orbit Satellites (*Swarm*, CHAMP, Ørsted, SAC-C)



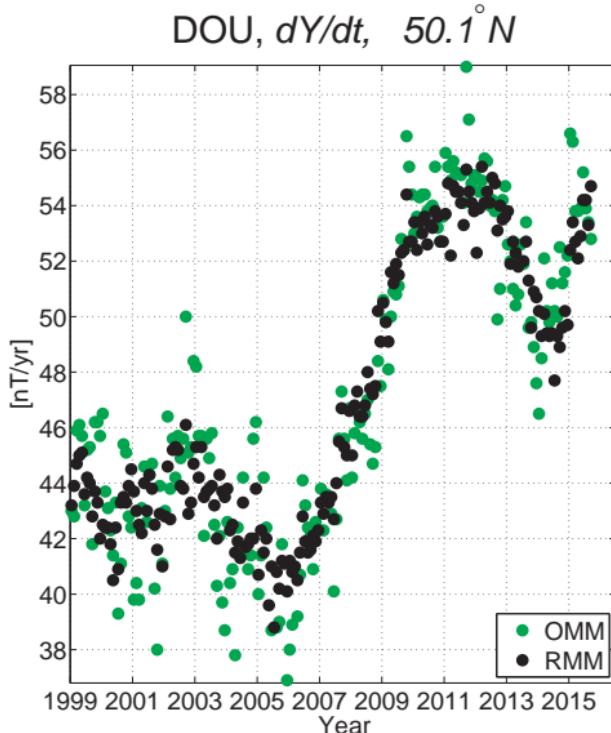
## Talk Outline

1. Field modelling with observatory and satellite data
2. Recent secular variation 1999-2016.5
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## Talk Outline

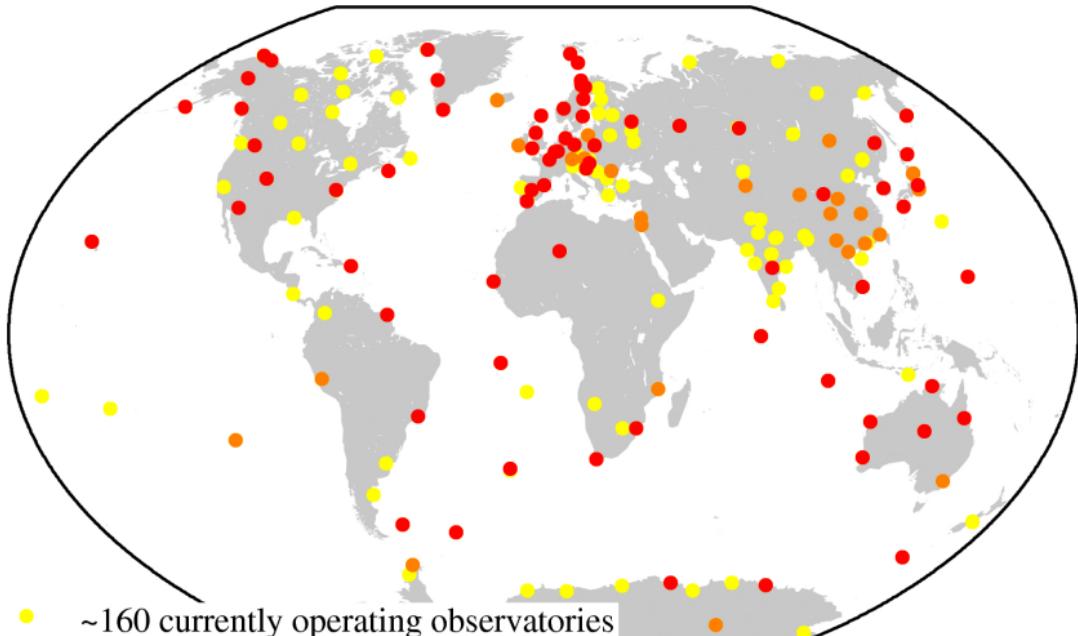
1. Field modelling with observatory and satellite data
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# Observatory data: Revised Monthly Means (RMM)



- AUX\_OBS\_2 data product, derived from WDC hourly means ( $\sim 160$  active observ.)
- Manually checked and corrected for known baseline changes (Macmillan and Olsen 2013)
- Estimates of large-scale magnetospheric (Olsen et al., 2014) and Sq (Sabaka et al., 2004) fields removed
- Compute Huber-weighted monthly mean, considering all local times

## Availability of close to definitive (or QD) data



- ~160 currently operating observatories
- 93 with acceptable definitive or close-to-definitive data in 2015
- 70 with acceptable definitive or close-to-definitive data in 2016

[Courtesy S. Macmillan, BGS]

## Selection of satellite data: vector and scalar

- Night side: data from dark regions, sun 10 deg below horizon
- Vector data below 55 deg geomagnetic latitude
- Quiet-time, based on observatory-data derived indices:
  - $K_p \leq 2$
  - $|dRC/dt| \leq 2\text{nT/hr}$
- Quiet-time, based on IMF and solar wind parameters (for scalar data in polar regions)
  - IMF  $B_z > 0$ , averaged over preceding 1 hr
  - $E_m = \leq 0.8\text{mV/m}$ , averaged over preceding 1hr

## The Swarm satellite constellation and field gradients

- A pair of satellites (*Alpha*, *Charlie*), flying close together at altitude approx. 460 km
- A third satellite (*Bravo*) higher ~ 500 km, and separated in LT (now by 3hrs)



- Use field differences (approx. gradients) btw satellites and along-track
- Relax selection criteria  $Kp \leq 30$ ,  $|dRC/dt| \leq 3nT/hr$
- Consider scalar gradient also in sunlit polar region (-> more uniform data coverage)

# Parameterization of Internal Field

- **Potential field approach:**  $\mathbf{B} = -\nabla V$  where  $V = V^{\text{int}} + V^{\text{ext}}$ .

- The internal part of the potential takes the form

$$V^{\text{int}} = a \sum_{n=1}^{N_{\text{int}}} \sum_{m=0}^n (g_n^m \cos m\phi + h_n^m \sin m\phi) \left(\frac{a}{r}\right)^{n+1} P_n^m (\cos \theta)$$

- For  $n \leq 20$ , expand in 6th order B-splines

$$g_n^m(t) = \sum_{k=1}^K {}^k g_n^m B_k(t). \quad (1)$$

# Parameterization of External Field

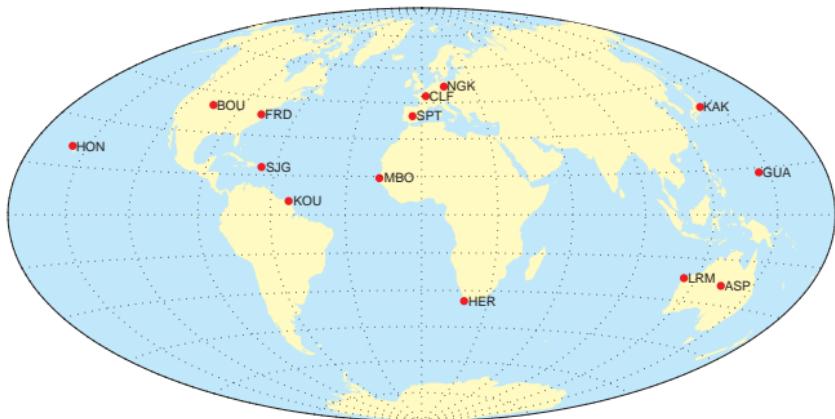
- For the external potential, expand in SM and GSM co-ordinate systems, with  $\theta_d$  and  $T_d$  being dipole co-lat. and dipole local time

$$\begin{aligned} V^{\text{ext}} &= a \sum_{n=1}^2 \sum_{m=0}^n (q_n^m \cos mT_d + s_n^m \sin mT_d) \left(\frac{r}{a}\right)^n P_n^m(\cos \theta_d) \\ &+ a \sum_{n=1}^2 q_n^{0,\text{GSM}} R_n^0(r, \theta, \phi). \end{aligned}$$

- Degree-1 coefficients in SM coords dependent on the RC disturbance index

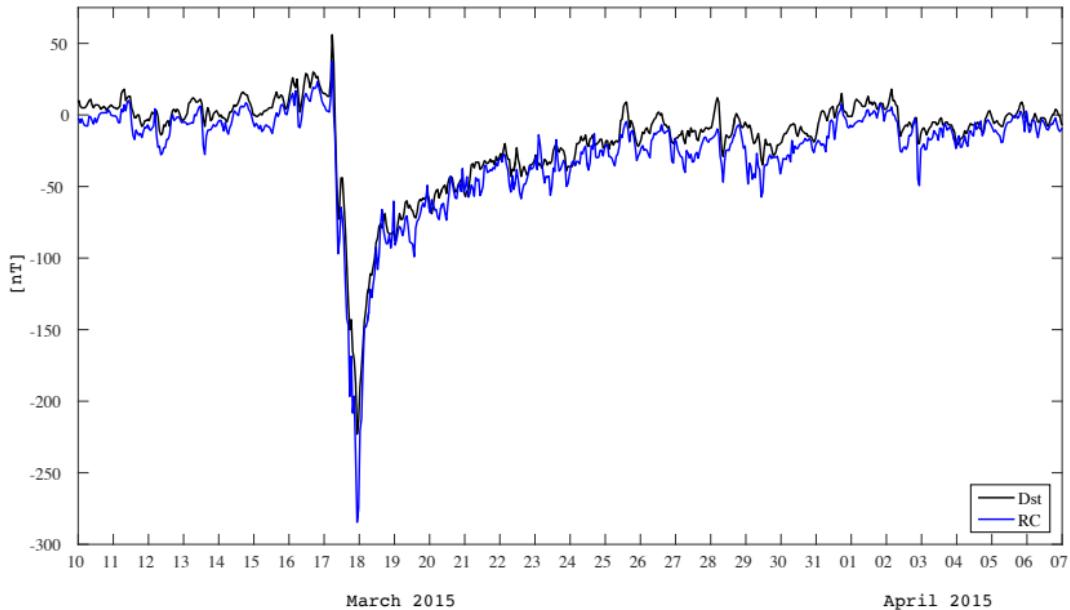
## The RC Index

- Similar to  $Dst$  but stable on months to year time-scale
- Based on hourly means from 14 mid/low latitude obs reporting up-to-date QD data



- Baseline: core field from latest CHAOS field model
- Only night-side data, no explicit  $Sq$  correction
- Hour-by-hour spherical harmonic analysis of horizontal components
- Separated into internal and external components using a 1D mantle conductivity model
- An 'experimental' index, mostly for field modelling purposes. Under development....

## Example: RC Index during the St. Patrick's day storm



- Small offset compared to Dst (due to different definition of baseline)
- Amplitude slightly different, especially during storms, due to different selection of contributing observatories

## Global field modelling: Estimation

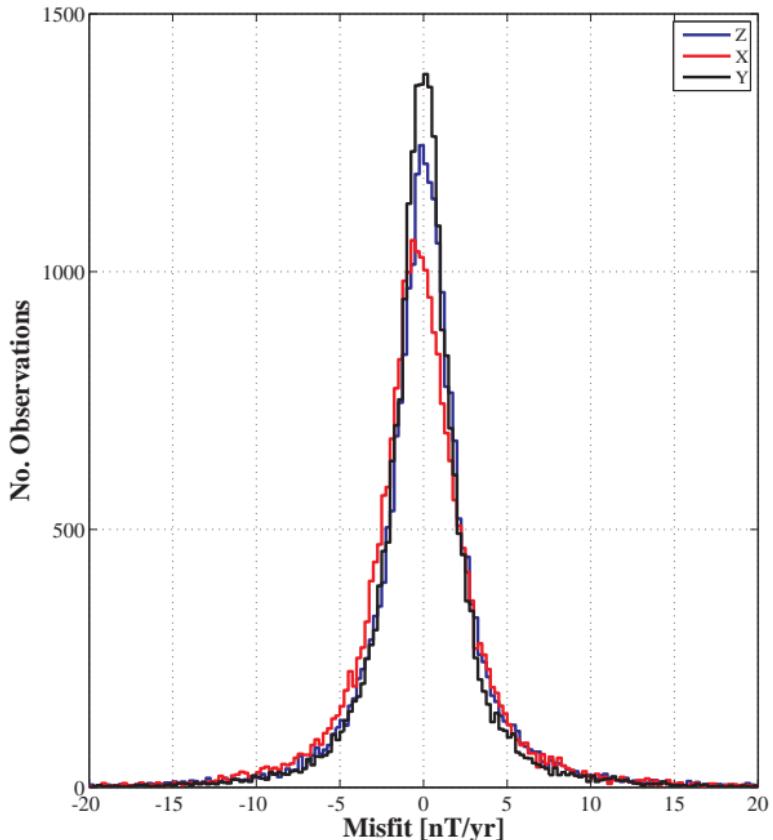
- Work with satellite vector data in **magnetometer frame**, co-estimate Euler angles
- 7,873,156 data in all ( $3 \times 24583$  from Observatory Revised Monthly Means)
- **Robust non-linear least squares including regularization**, iteratively minimizing

$$[\mathbf{d} - F(\mathbf{m})]^T \underline{\mathbf{W}}^{-1} [\mathbf{d} - F(\mathbf{m})] + \lambda_2 \mathbf{m}^T \underline{\underline{\Lambda}}_2 \mathbf{m} + \lambda_3 \mathbf{m}^T \underline{\underline{\Lambda}}_3 \mathbf{m}$$

$\underline{\mathbf{W}}$  is a Huber weighting matrix,  $\underline{\underline{\Lambda}}_2$  and  $\underline{\underline{\Lambda}}_3$  are regularization matrices

- Latest model, **CHAOS-6** ([Finlay et al., 2016](#)), now updated to Aug 2016  
<http://www.spacecenter.dk/files/magnetic-models/CHAOS-6/>
- Weighted rms misfit to non-polar, dark *Swarm* scalar data is **2.14 nT**,  
For scalar field differences, **0.26 nT** along-track and **0.45 nT** cross-track,  
For obs RMM, **3.66 nT/yr, 3.08 nT/yr, 3.80nT/yr** for  $dX/dt, dY/dt, dZ/dt$

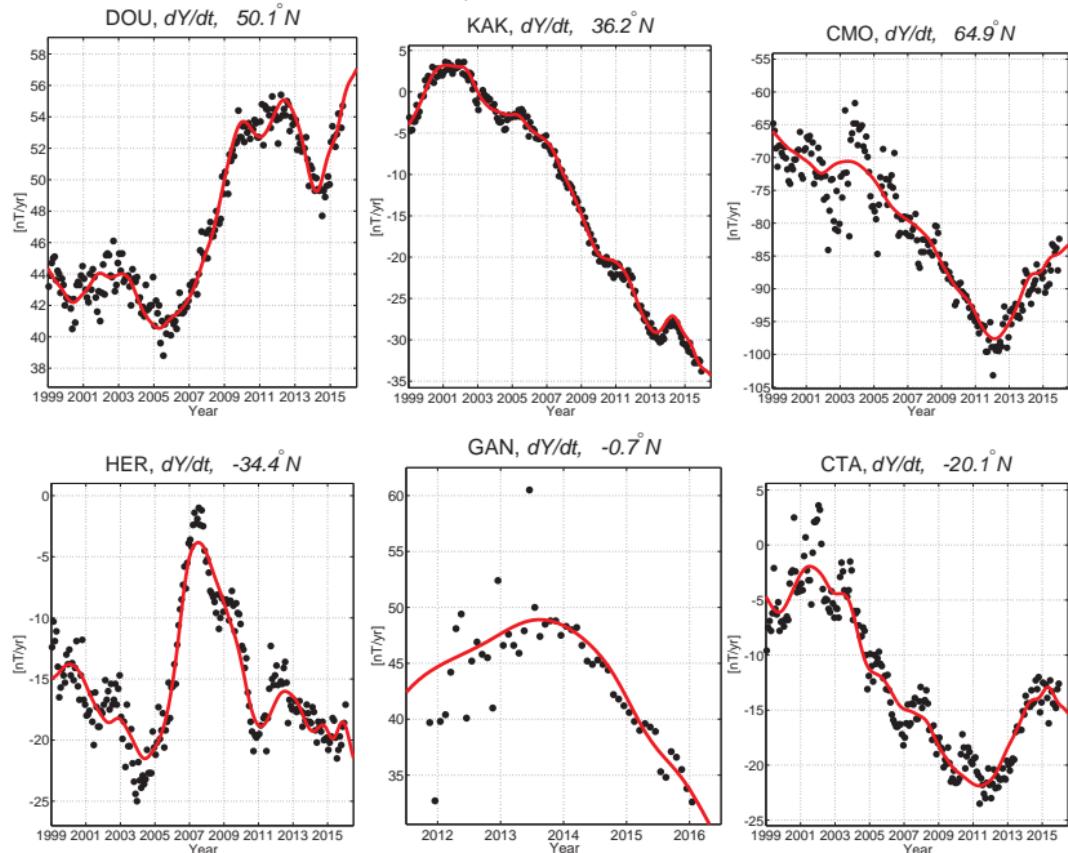
## Histograms of residuals to observatory RMM



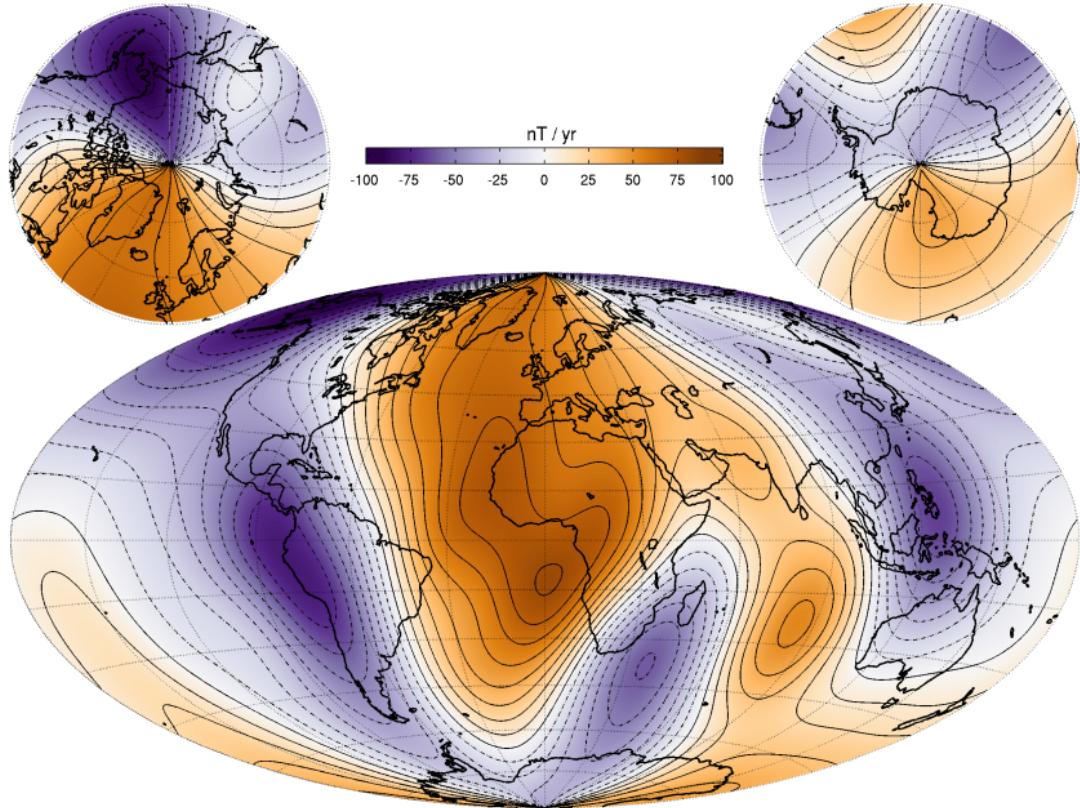
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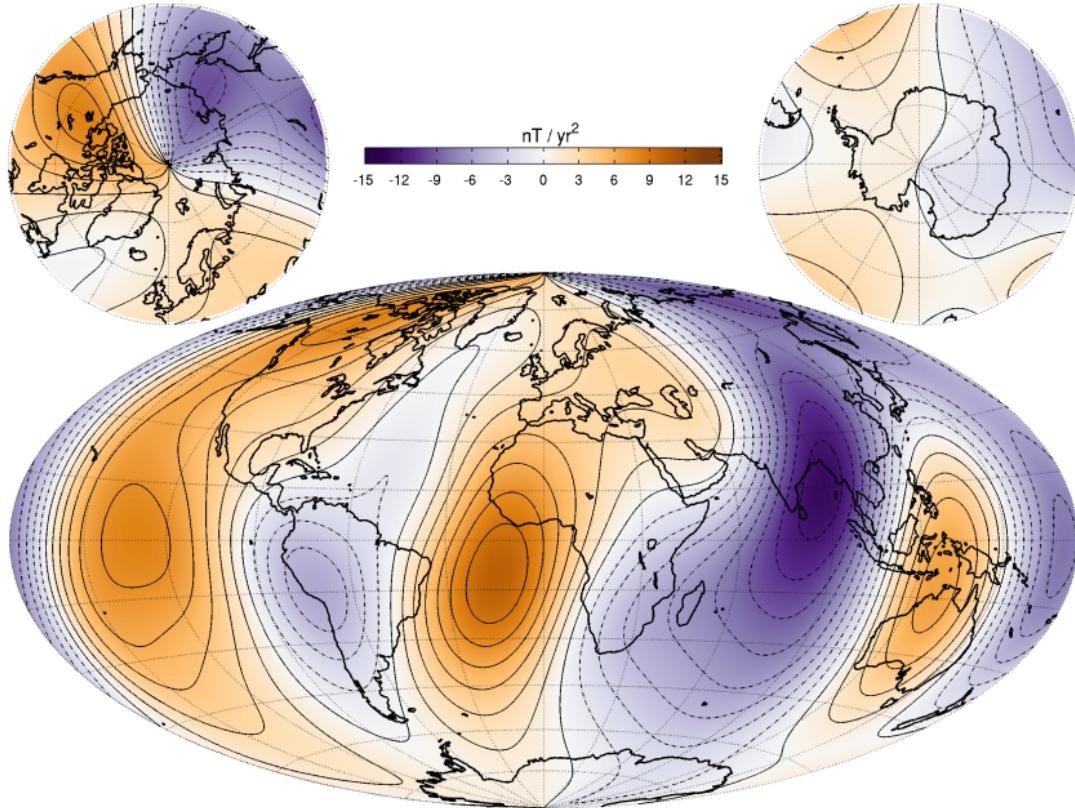
## Fit to observatory data, $dY/dt$



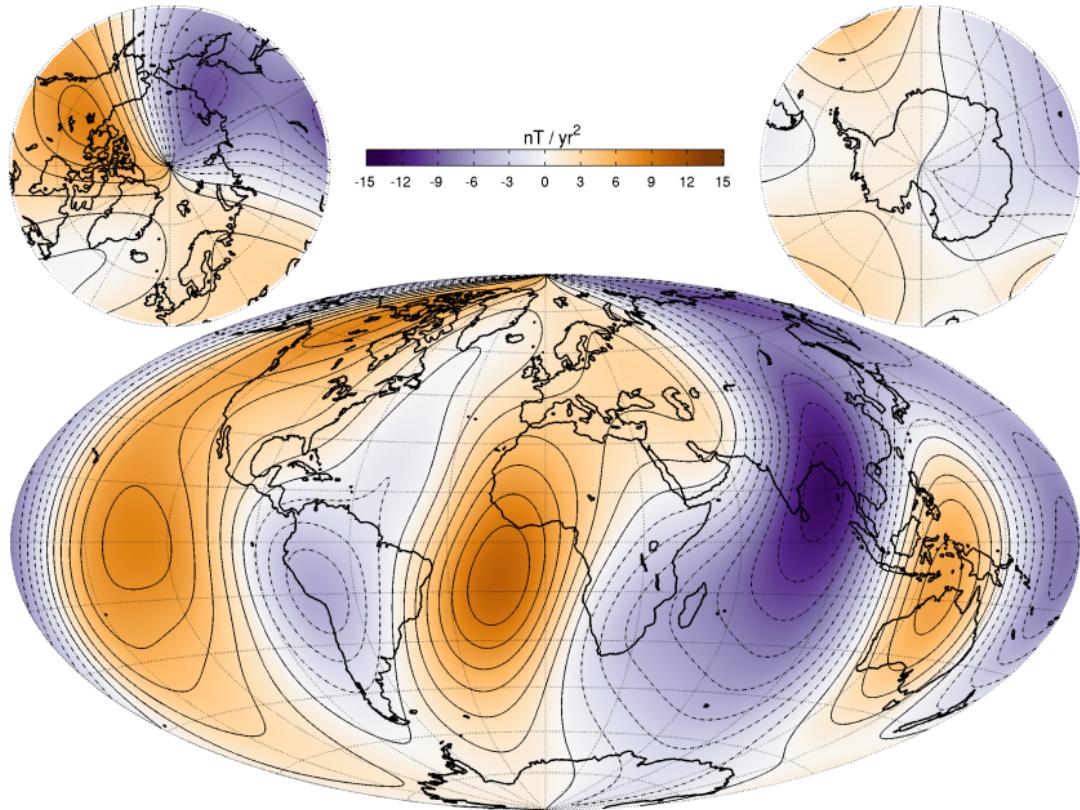
# Rate of change of Eastward field $dY/dt$ in 2016.5



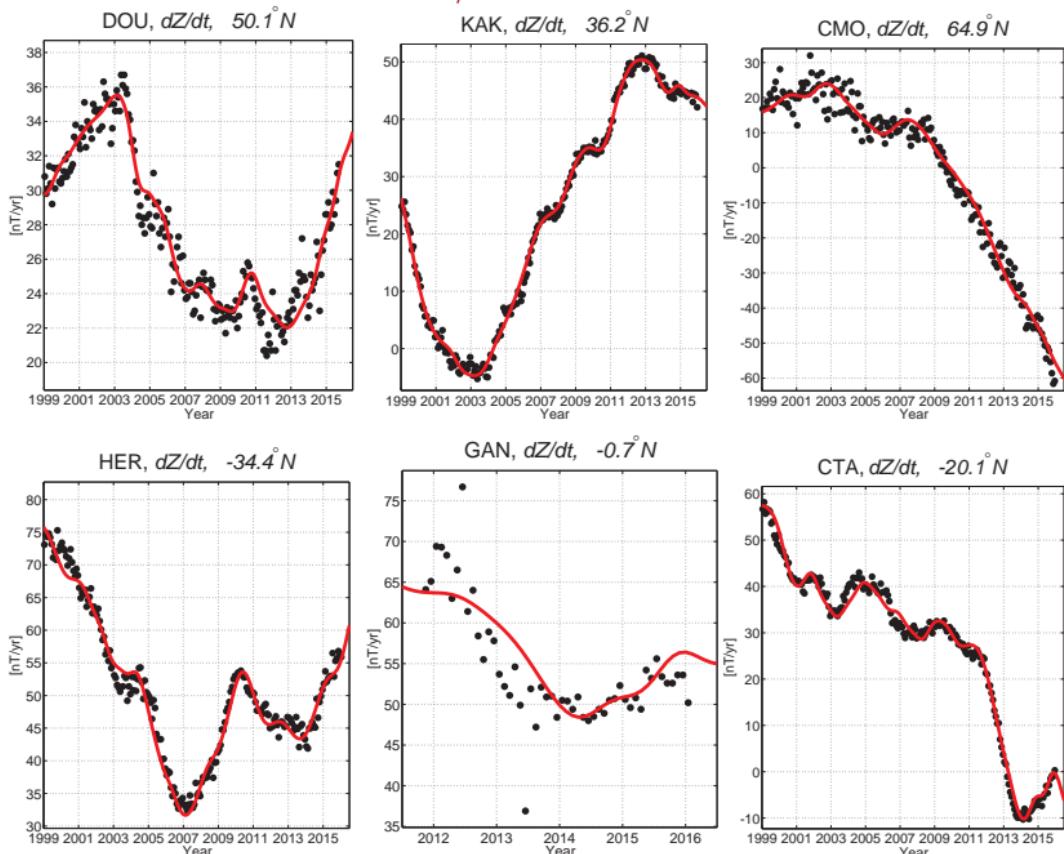
# Acceleration of Eastward field $d^2Y/dt^2$ in 2015



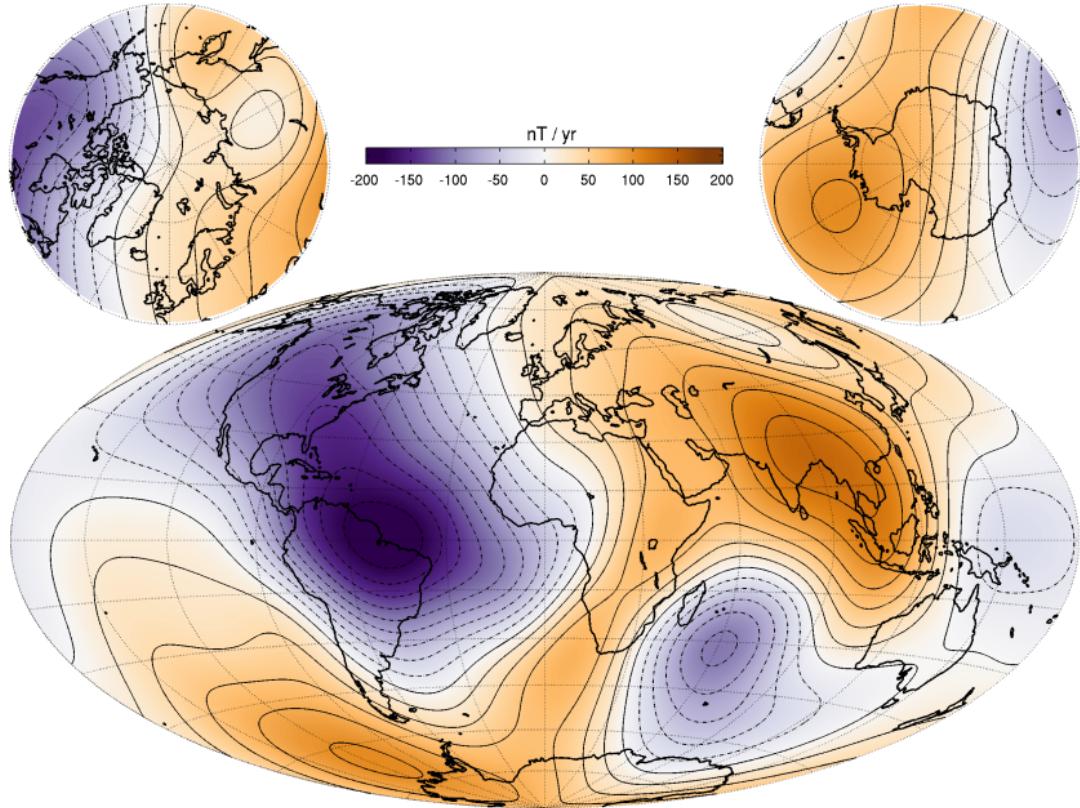
# Acceleration of Eastward field $d^2Y/dt^2$



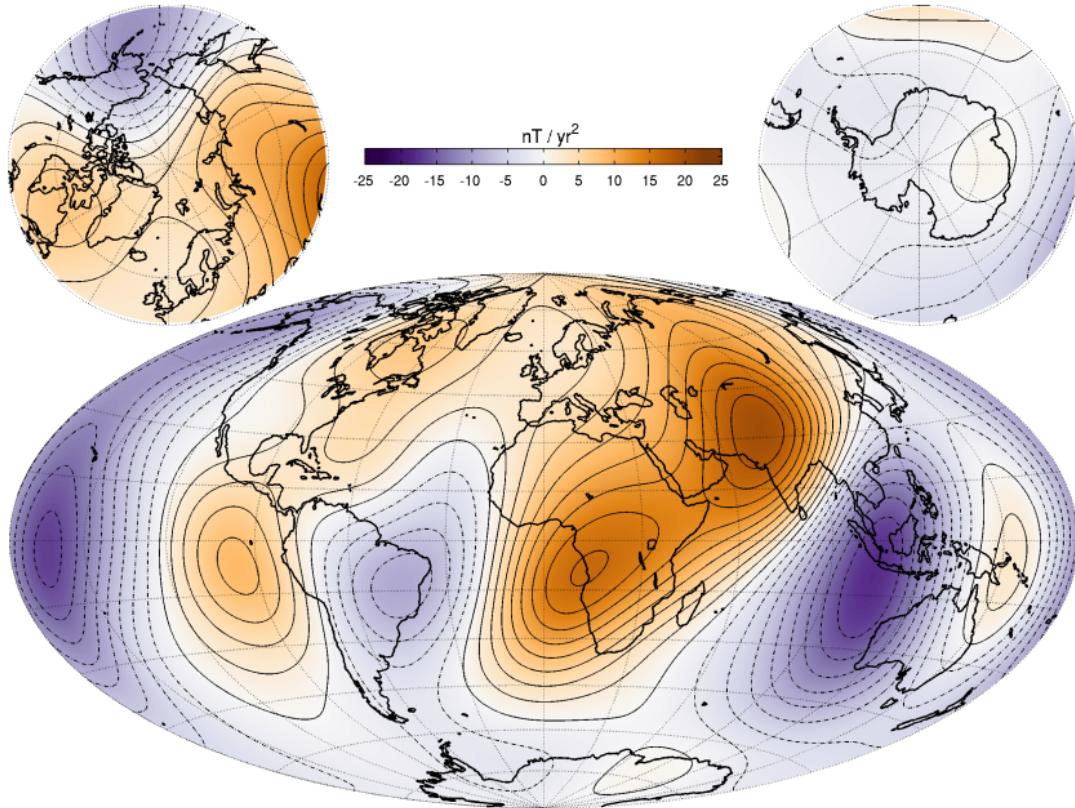
## Fit to observatory data, $dZ/dt$



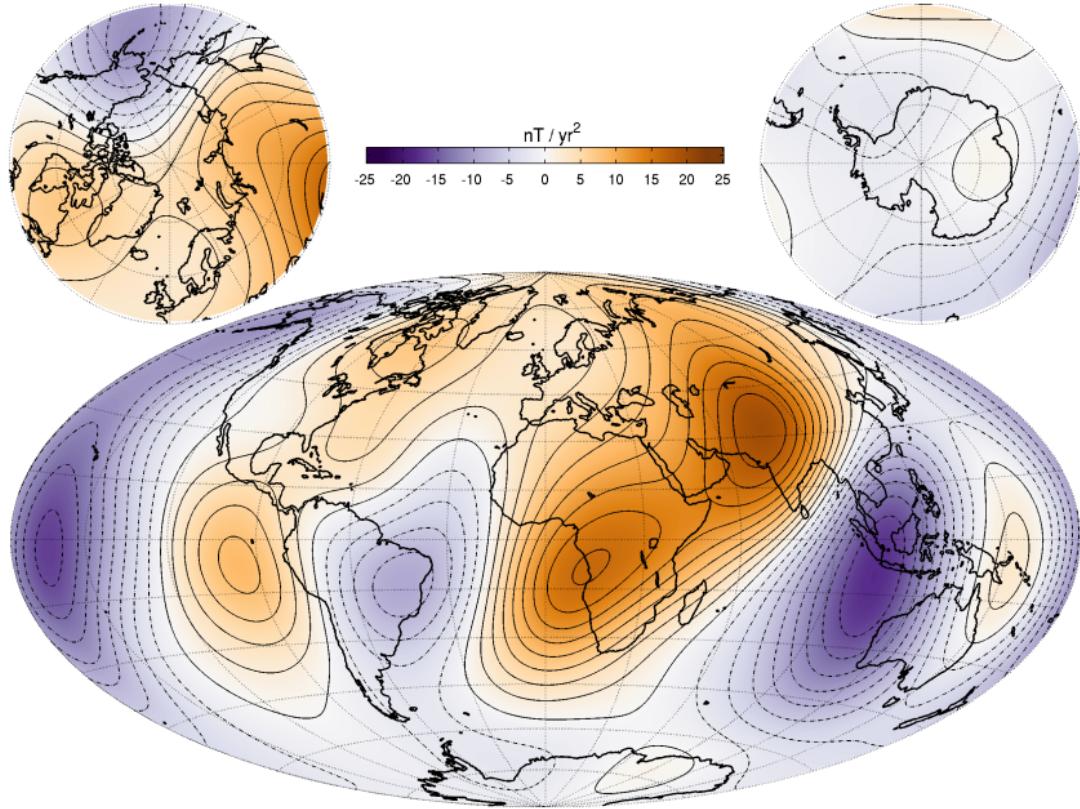
## Rate of change of vertical field $dZ/dt$ in 2016.5



# Acceleration of Eastward field $d^2 Z/dt^2$ in 2015



# Acceleration of Eastward field $d^2 Z/dt^2$

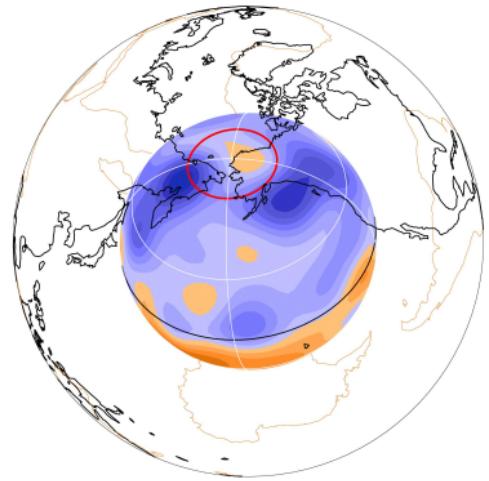


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# Downward continuation to the core-mantle boundary

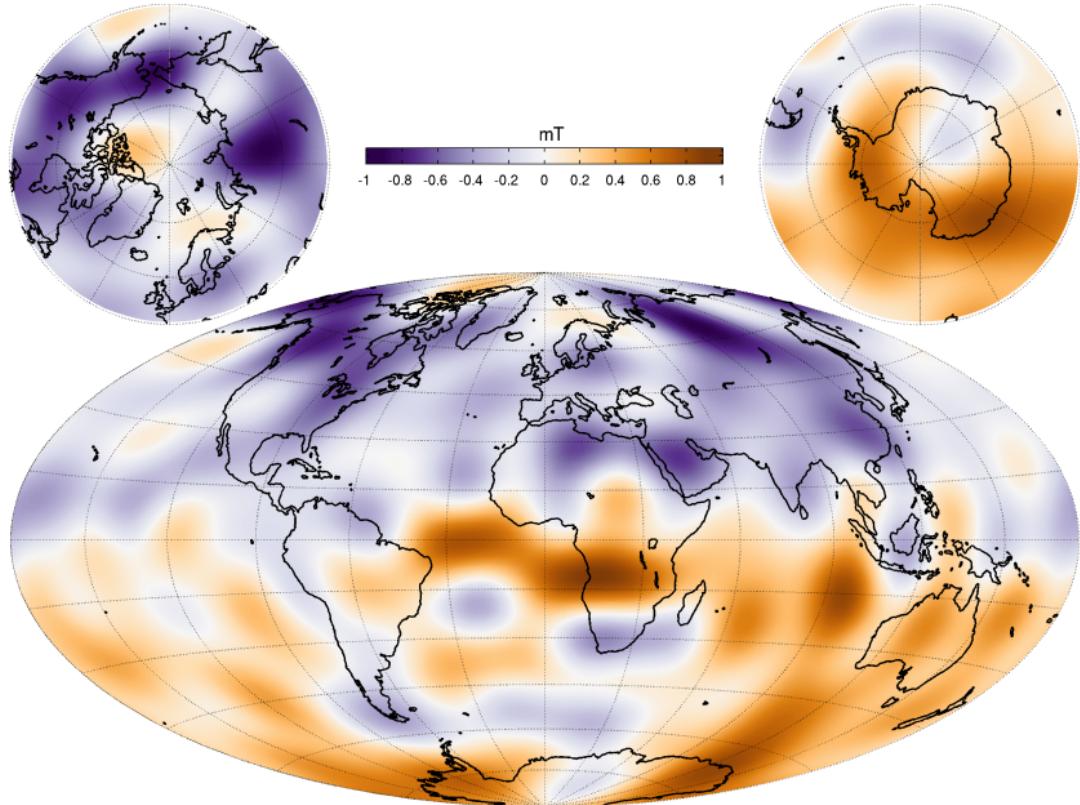
- Wish to understand origin of changes  
-> need to descend to core
- Possible to downward continue through mantle  
(Neglecting currents there on timescales > 1 yr)
- Small scales amplified as approach source
- Field at core surface stable to degree 13  
(above this crust dominate)
- Field change (SV) stable to degree 18



[Image credit: A. Jackson]

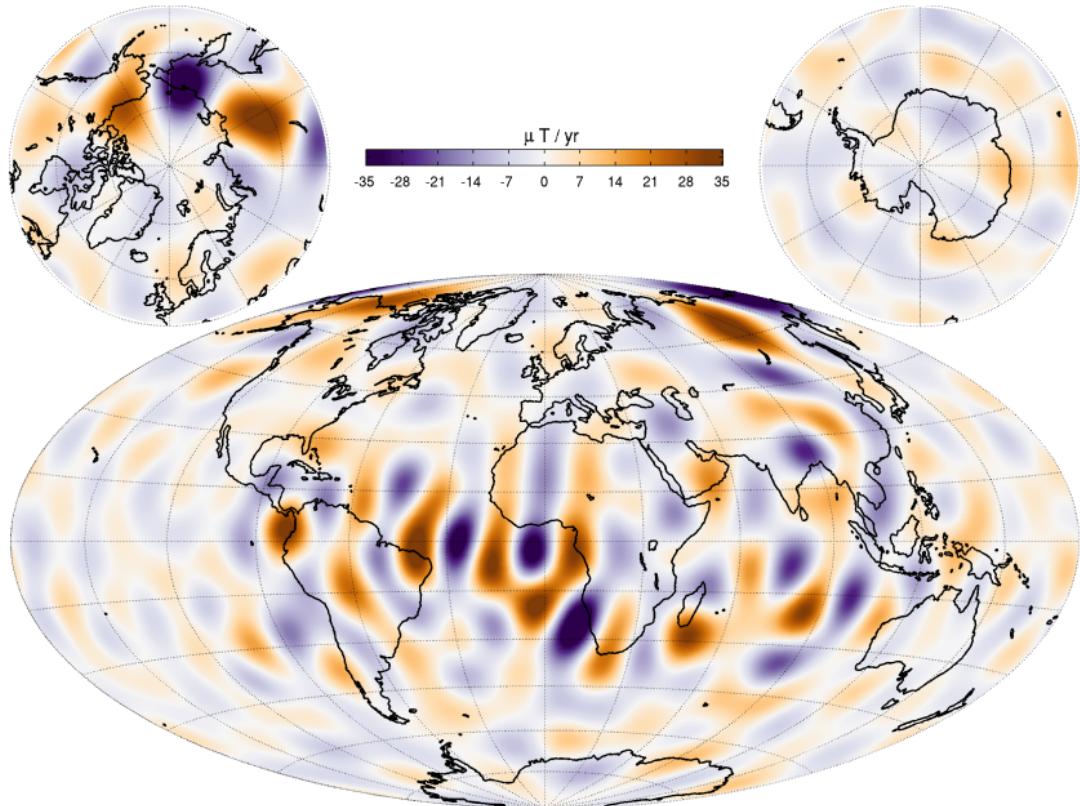
$$B_r = \sum_{n=1}^N \sum_{m=0}^n (n+1) (g_n^m \cos m\phi + h_n^m \sin m\phi) \left(\frac{a}{r}\right)^{n+2} P_n^m (\cos \theta)$$

## Radial field $B_r$ at core surface in 2015



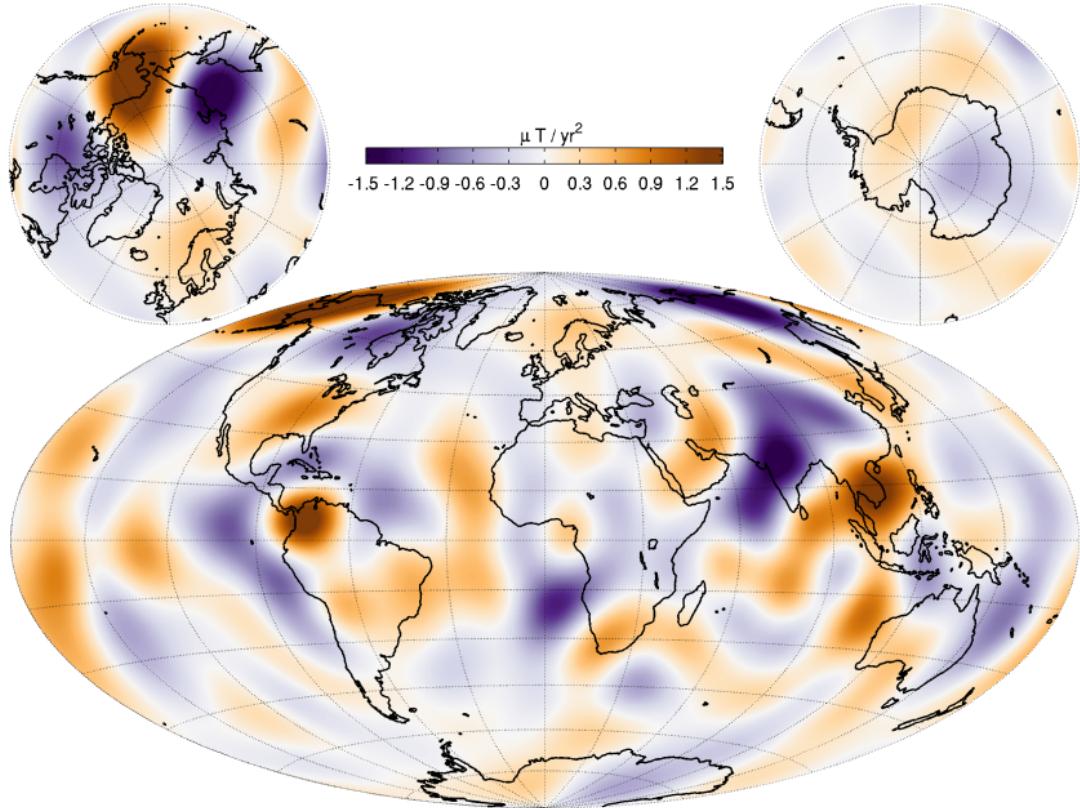
[CHAOS-6, truncated degree 13]

## Radial field SV $dB_r/dt$ at core surface in 2015

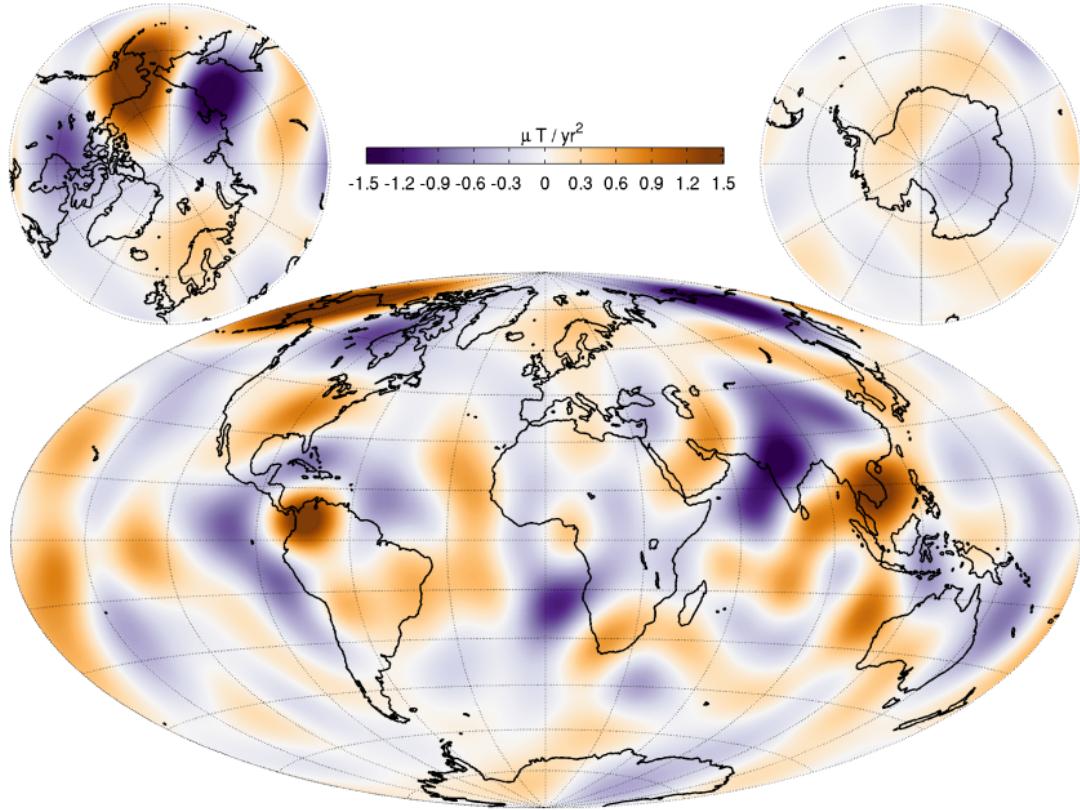


[CHAOS-6, truncated degree 18]

## Radial field SA $d^2B_r/dt^2$ at core surface in 2015



## Radial field SA $d^2 B_r / dt^2$ at core surface



## Talk Outline

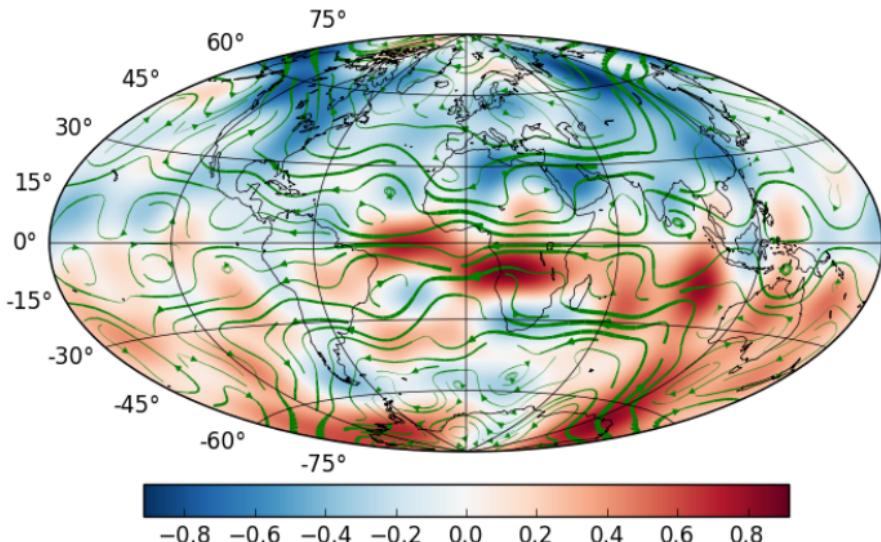
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## Inferred quasi-geostrophic core flow in 2015

- Assume rotation dominates the core flow (quasi-geostrophy)
- Invert for flow producing observed field changes, using the frozen flux induction eqn:

$$\frac{\partial B_r}{\partial t} = -\nabla_H \cdot (\mathbf{u} B_r)$$

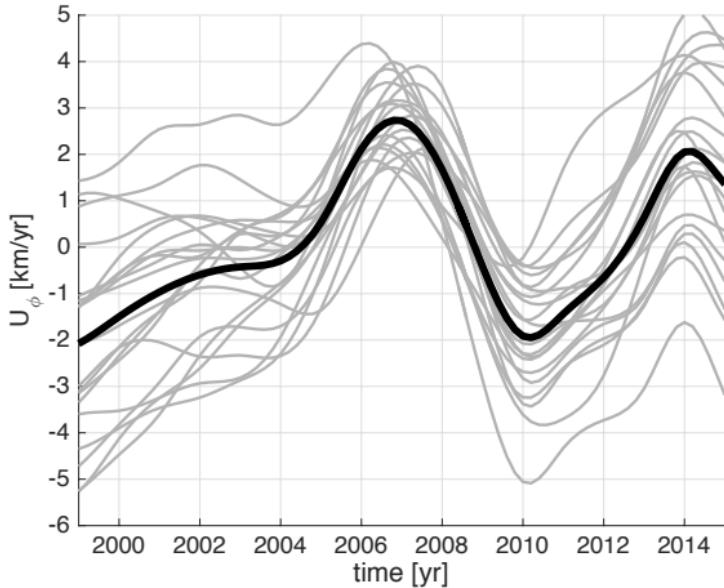
- Ensemble approach: random realizations of unknown small scale field



- Planetary scale anticyclonic gyre, westward at mid/low latitudes under Atlantic

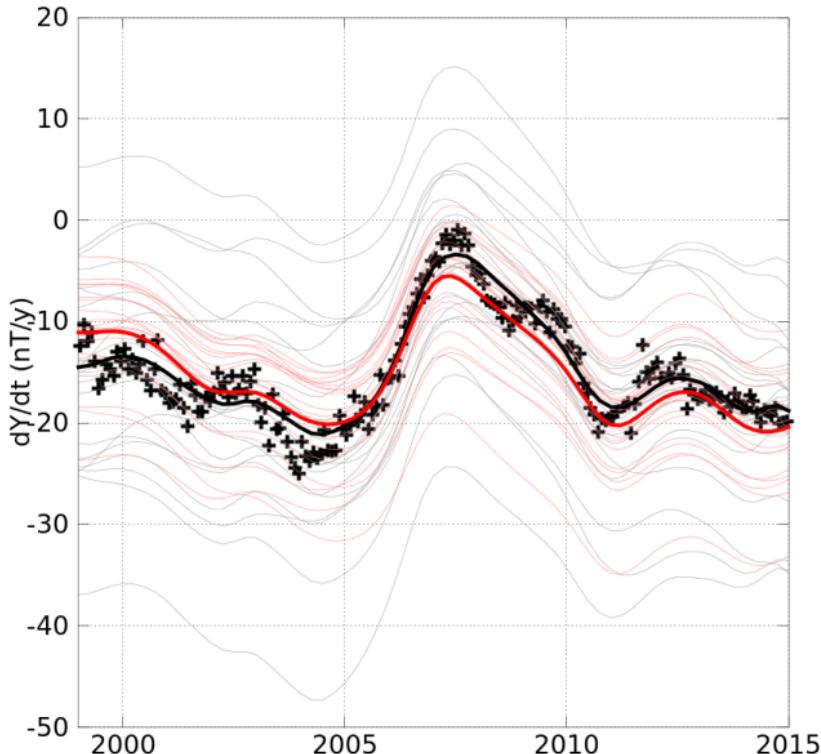
## Time-dependent (oscillating) core flow

- Find non-axisymmetric flow **oscillations** at low latitudes e.g.  $-15^{\circ}\text{N}$ ,  $0^{\circ}\text{E}$

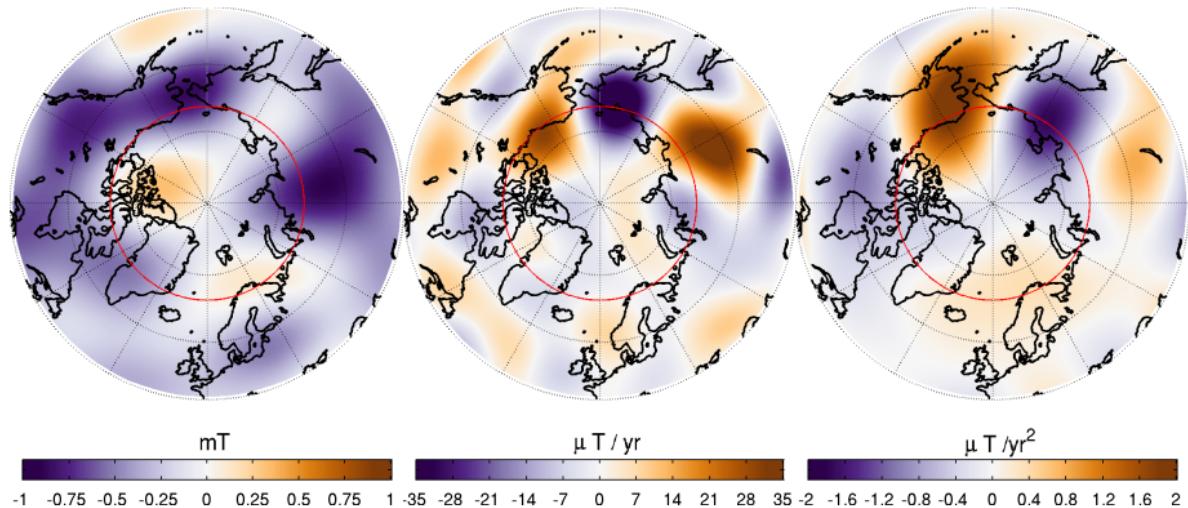


- Times of azimuthal flow acceleration, correspond to times of rapid field change
- Dynamical origin of oscillations presently unknown

## Predictions from time-dependent core flow: HER

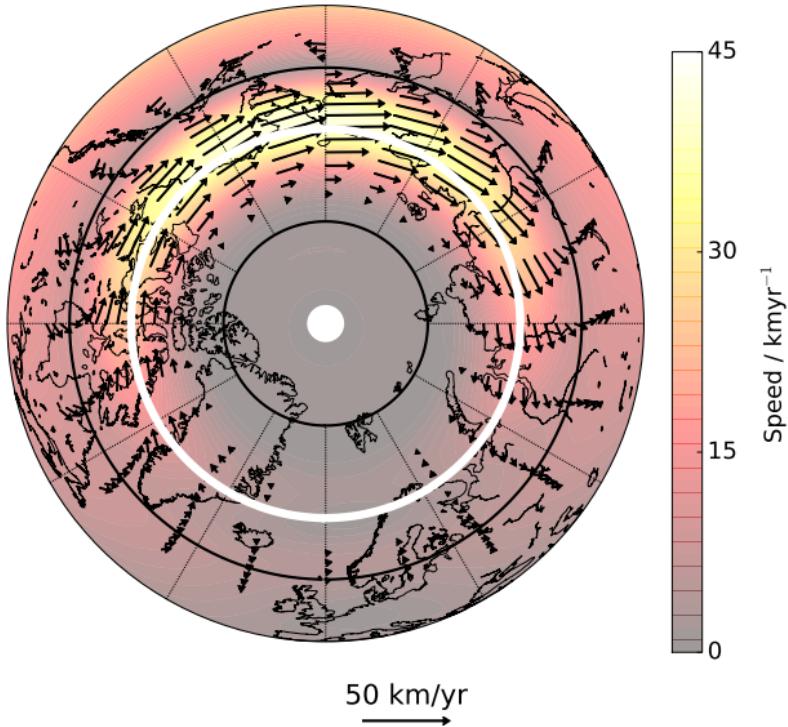


# Evolution of $B_r$ close to the tangent cylinder in 2015



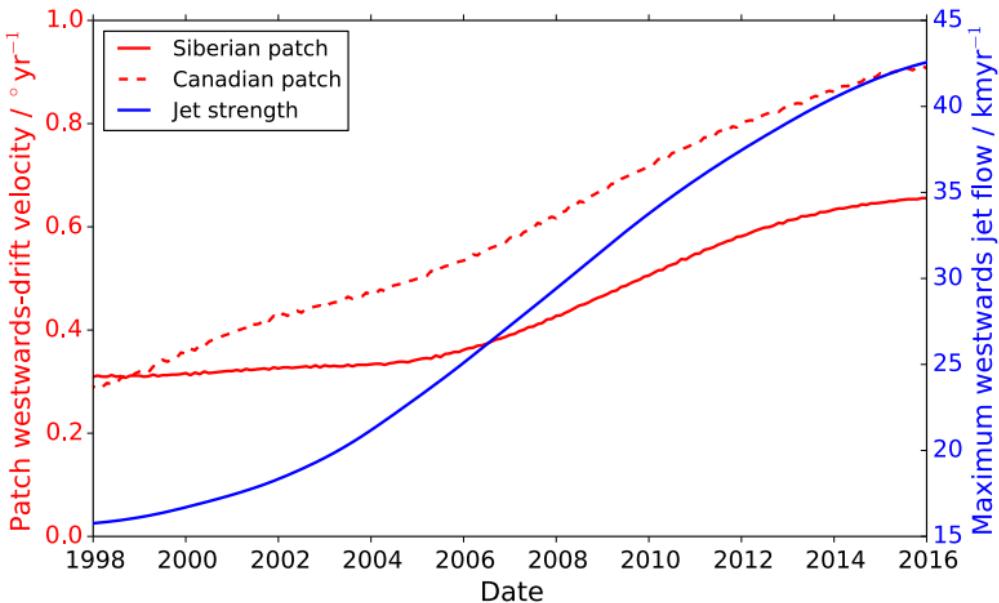
[CHAOS-6 model at CMB]

# A localized jet at the tangent cylinder



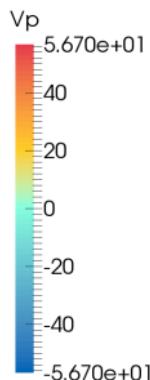
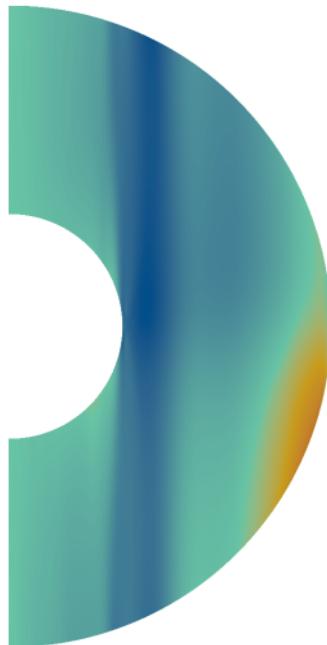
[Livermore et al. (submitted)]

# Accelerating of tangent cylinder jet



[Livermore et al. (submitted)]

# Role of shear at tangent cylinder in geodynamo process



- Shear at tangent cylinder is important for dynamos in rapidly-rotating regime
- Fundamental for building toroidal field within core
- Underlies dynamo oscillations and reversals

## Talk Outline

- 1.** Field modelling with observatory and satellite data
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# Summary



**(1) Close-to-definitive (QD) observatory AND *Swarm* data provide the basis for monitoring today's geodynamo**

## Summary

- (1) Close-to-definitive (QD) observatory AND *Swarm* data provide the basis for monitoring today's geodynamo**
- (2) Dynamic and localized secular variation observed on sub-decadal time scales**

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- (1) Close-to-definitive (QD) observatory AND *Swarm* data provide the basis for monitoring today's geodynamo
- (2) Dynamic and localized secular variation observed on sub-decadal time scales
- (3) Underlying core flow : Planetary-scale gyres, oscillations and localized jets

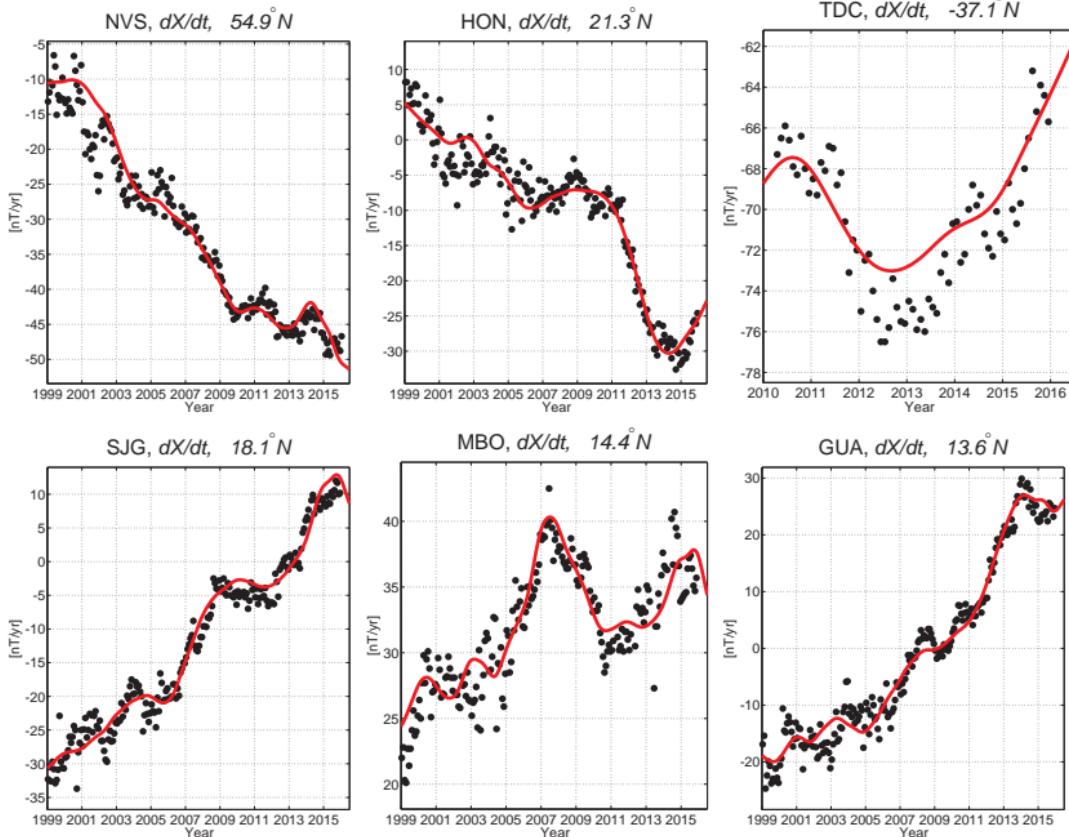
## Summary

- (1) Close-to-definitive (QD) observatory AND *Swarm* data provide the basis for monitoring today's geodynamo
- (2) Dynamic and localized secular variation observed on sub-decadal time scales
- (3) Underlying core flow : Planetary-scale gyres, oscillations and localized jets
- (4) Up-to-date and long-term stable observatory data is essential to improve our understand of the geodynamo and for real-time reference model applications

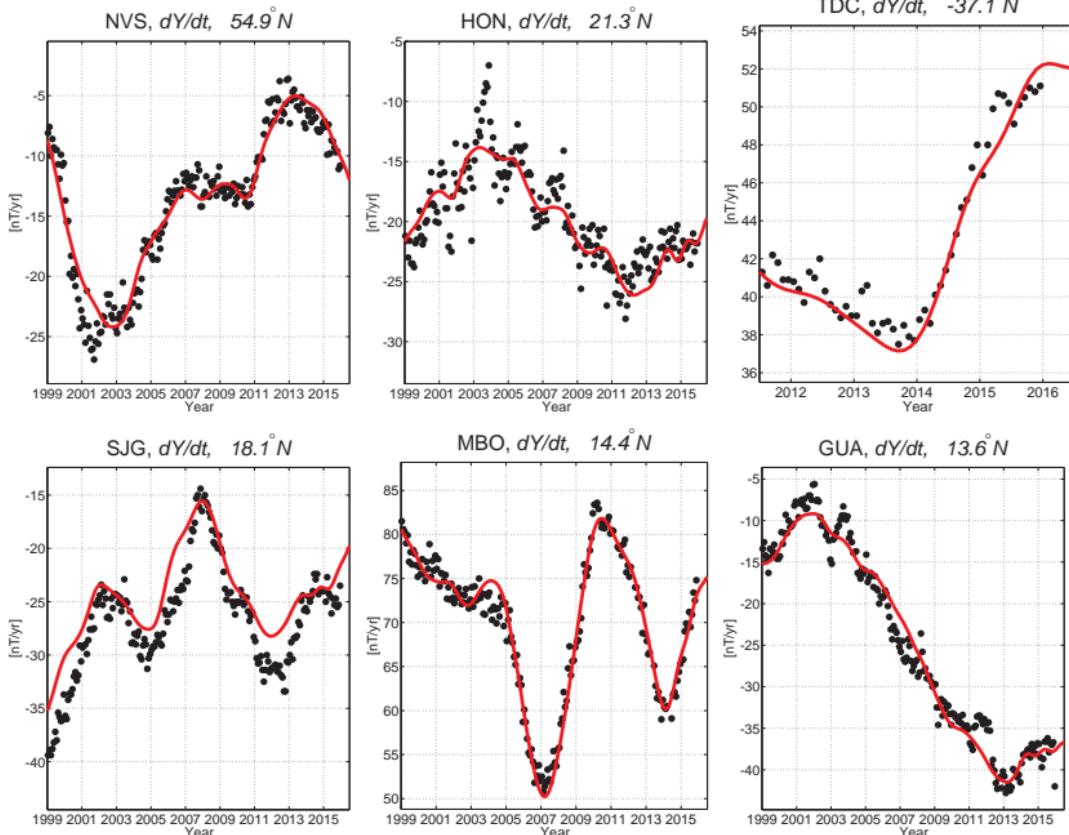




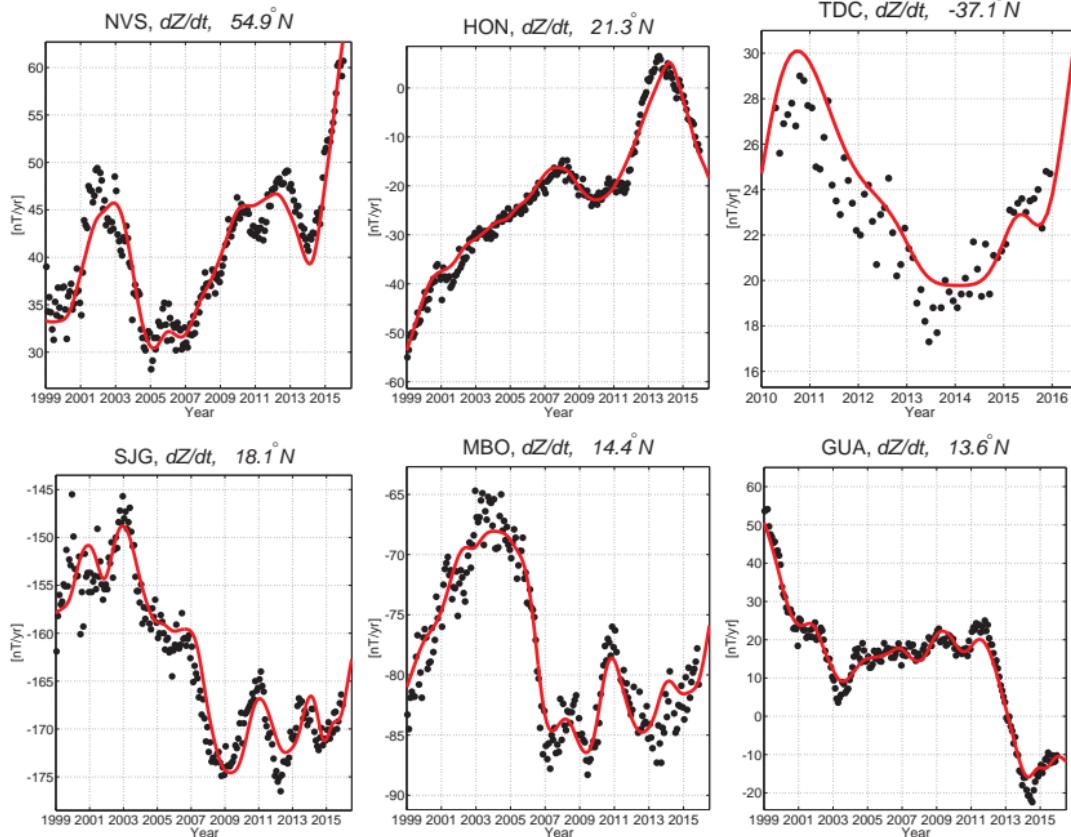
# Fit to observatory data, $X$



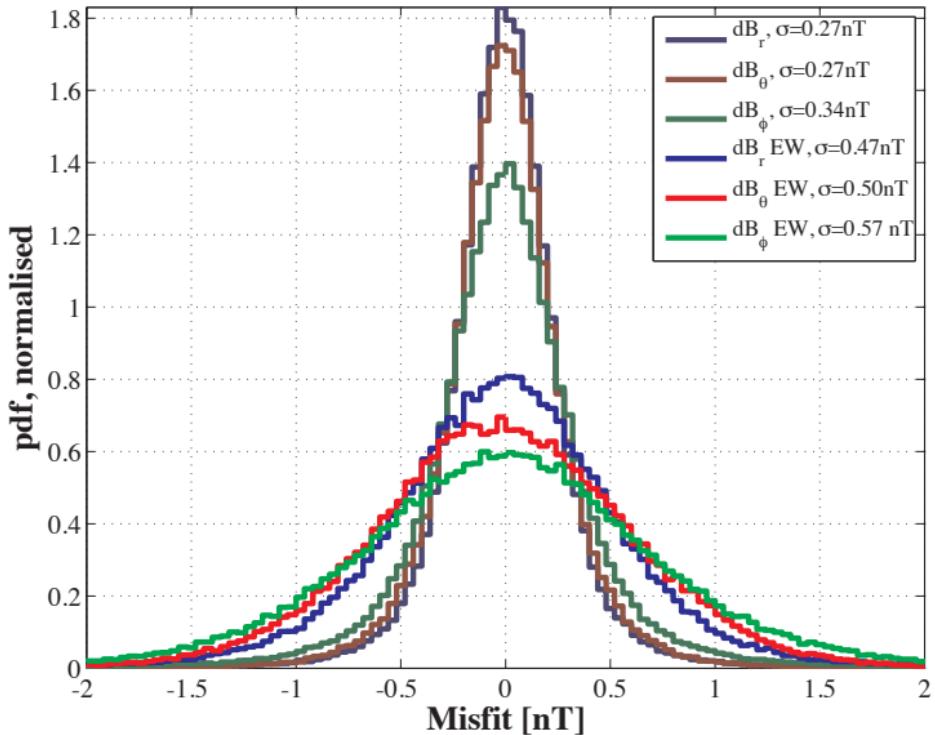
# Fit to observatory data, $Y$



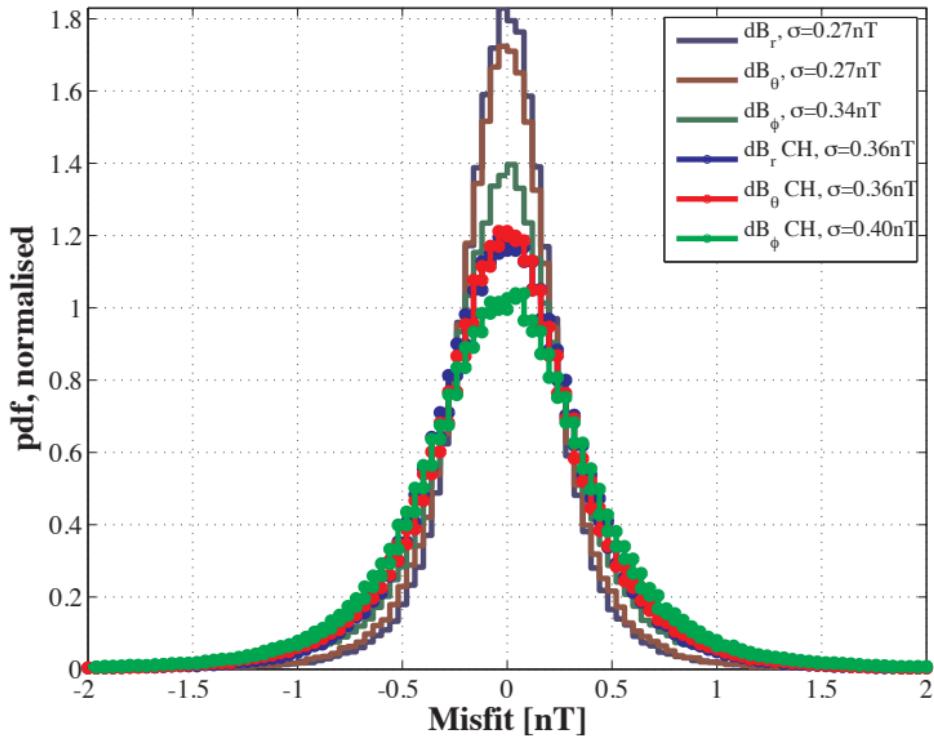
# Fit to observatory data, $Z$



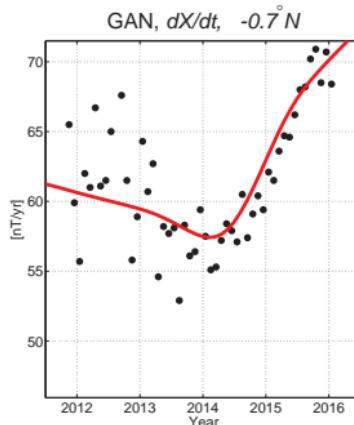
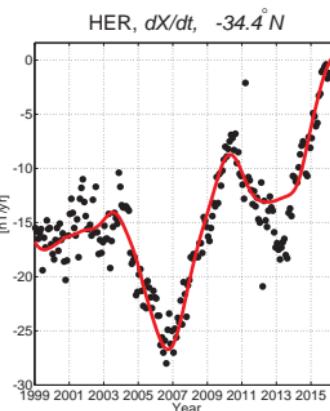
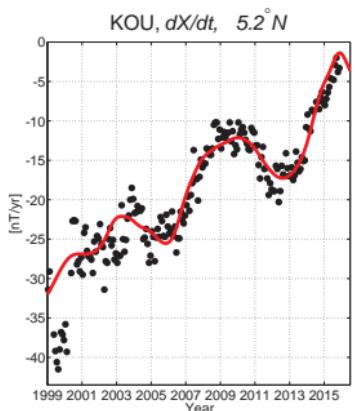
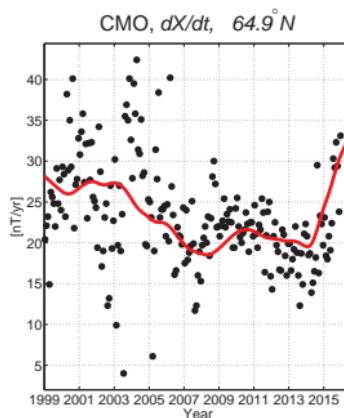
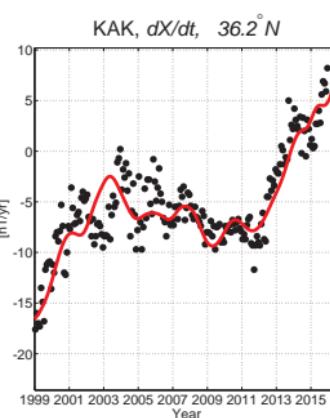
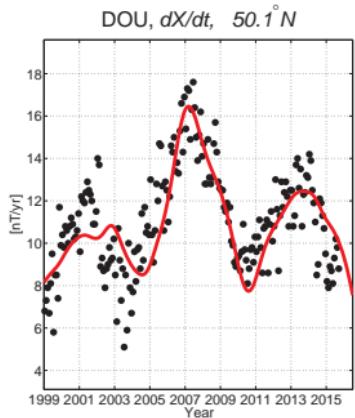
# Swarm vector difference residuals, Along vs Cross track



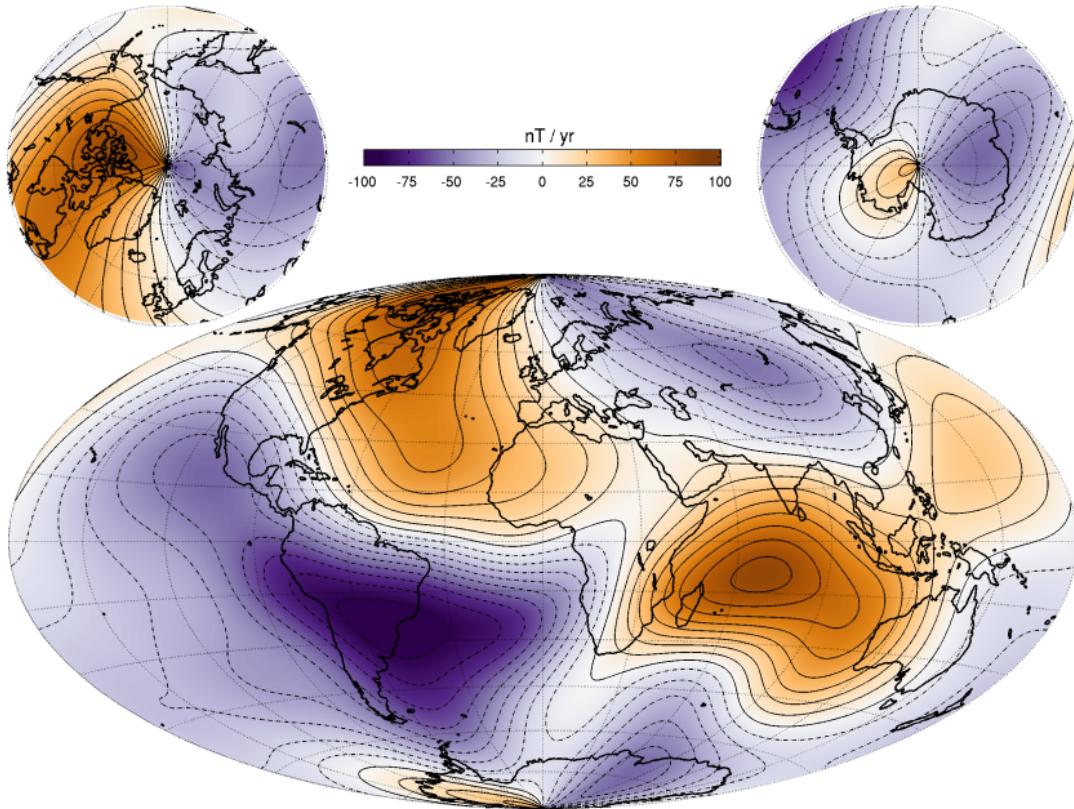
# Vector difference residuals, Swarm vs CHAMP



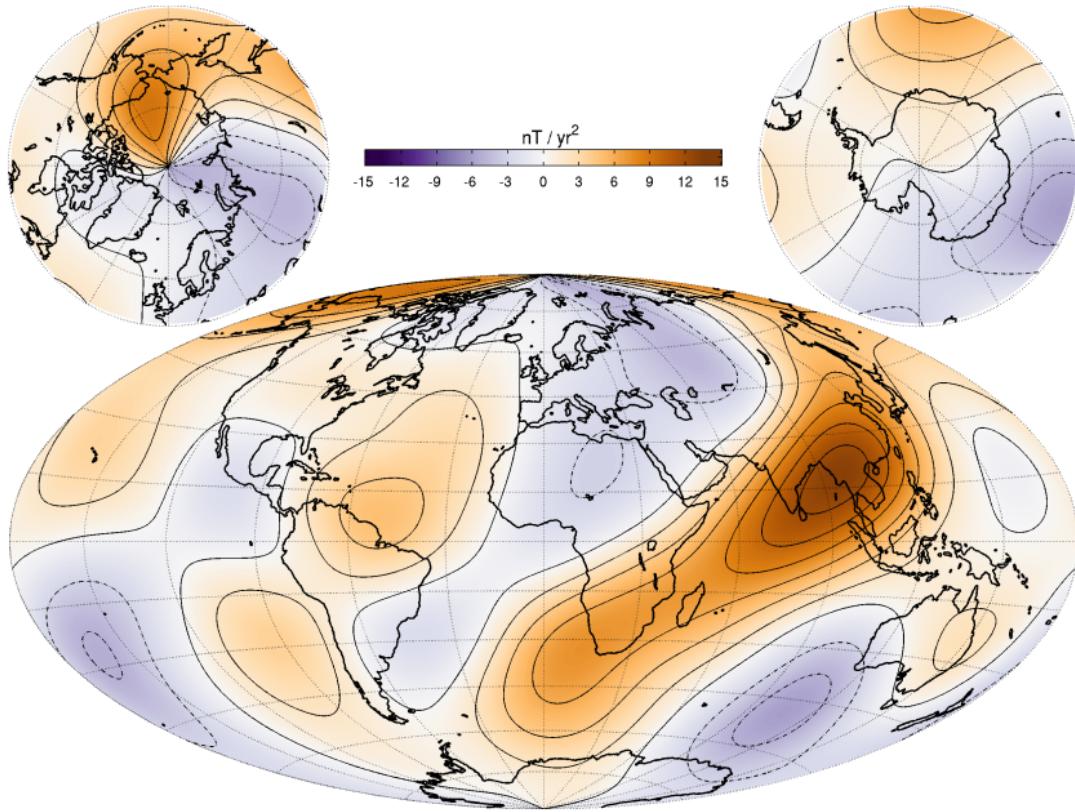
# Fit to observatory data, $dX/dt$



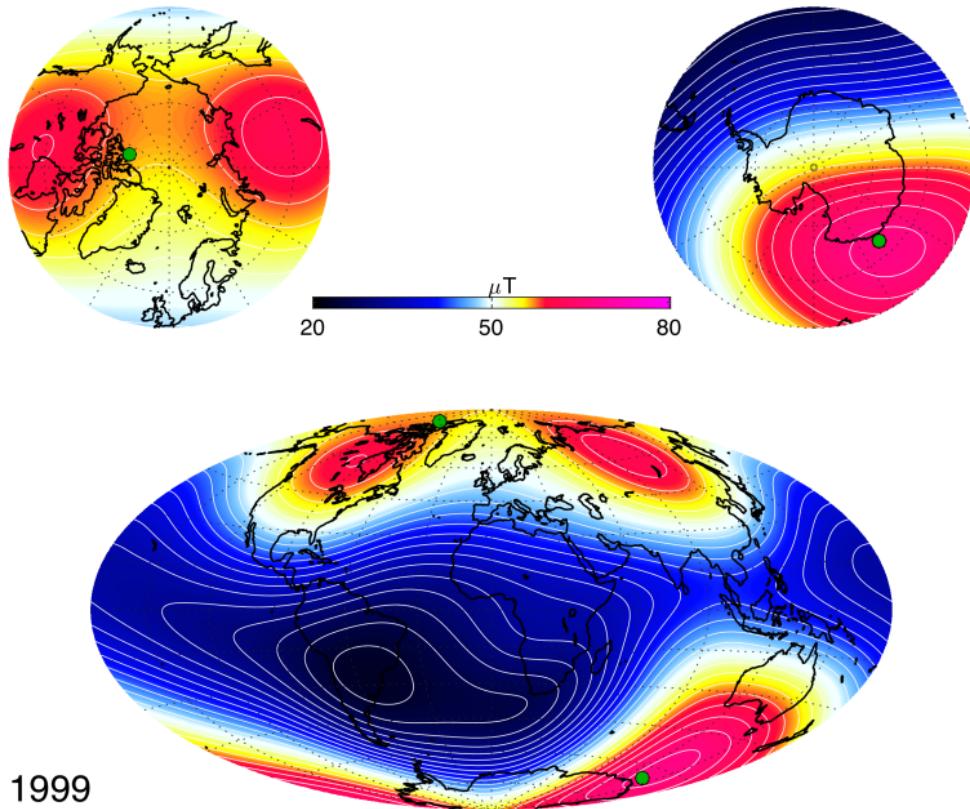
# Rate of change of Northward field $dX/dt$ in 2016.5



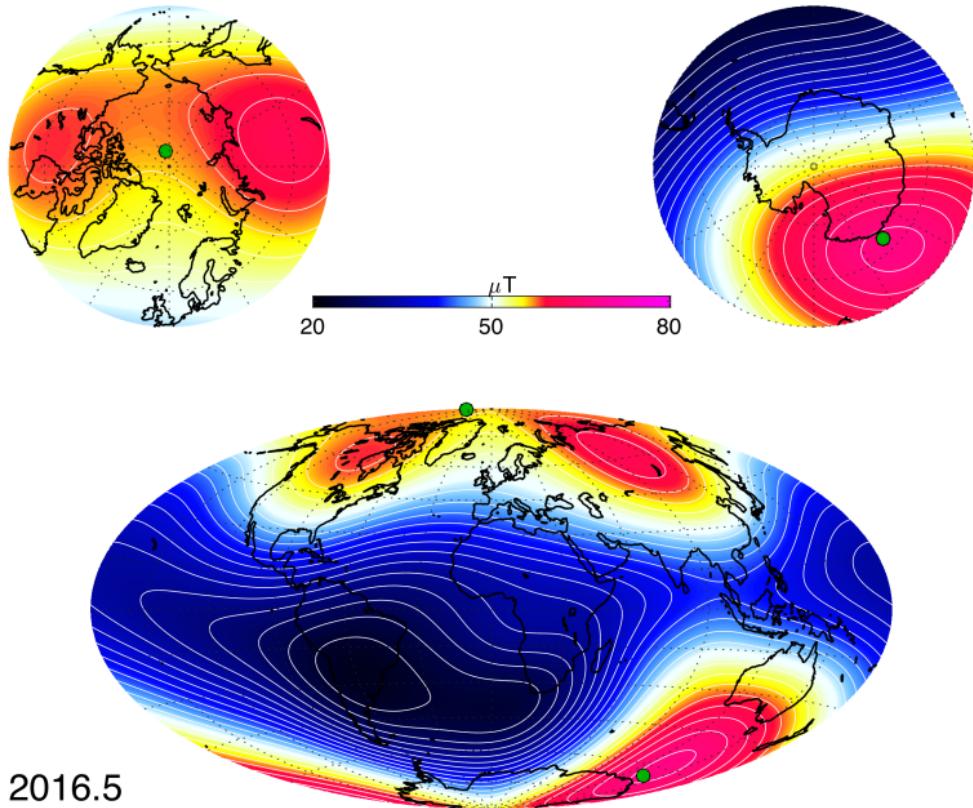
# Acceleration of Northward field $d^2 X/dt^2$ in 2015



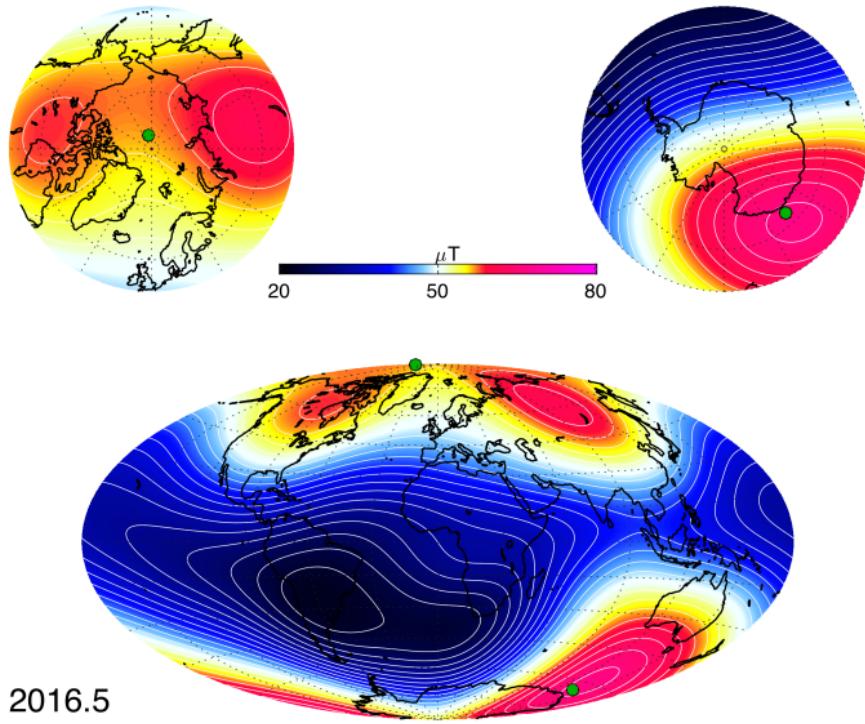
# Field strength and magnetic pole position in 1999



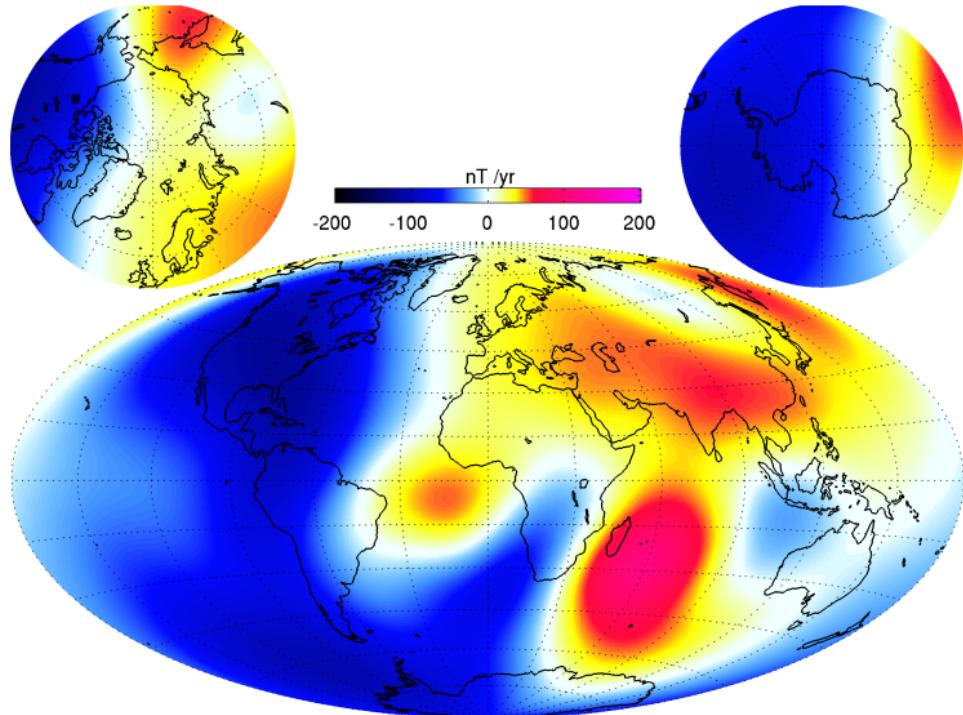
# Field strength and magnetic pole position in 2016.5



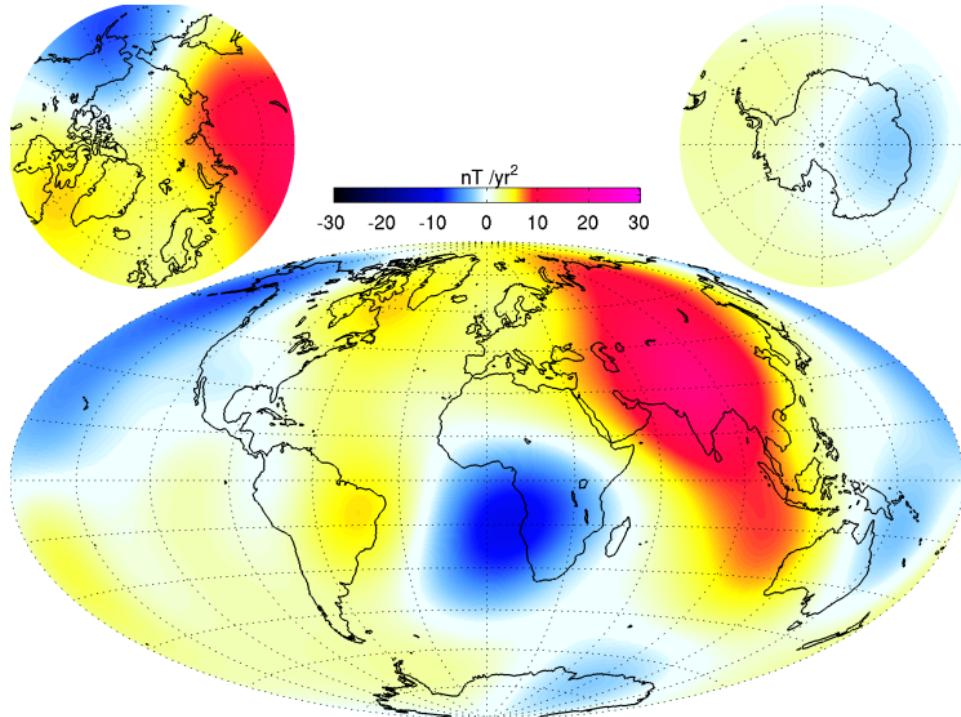
# Evolution of field intensity



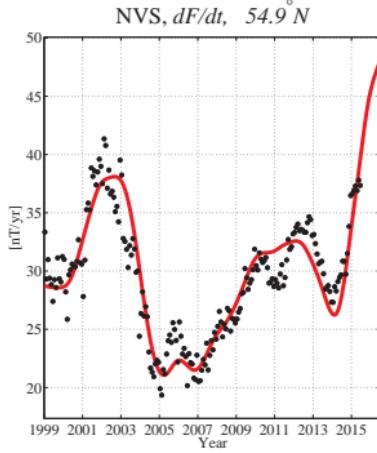
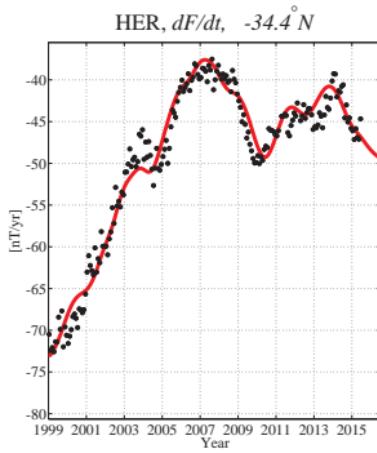
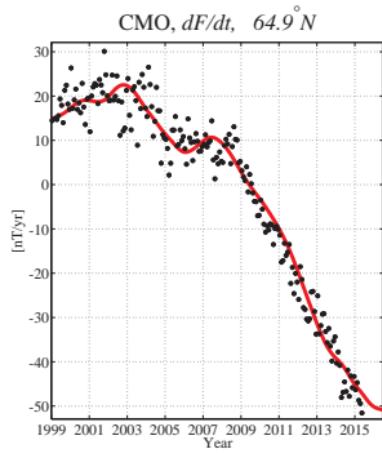
# Field strength strengthening and weakening in 2015



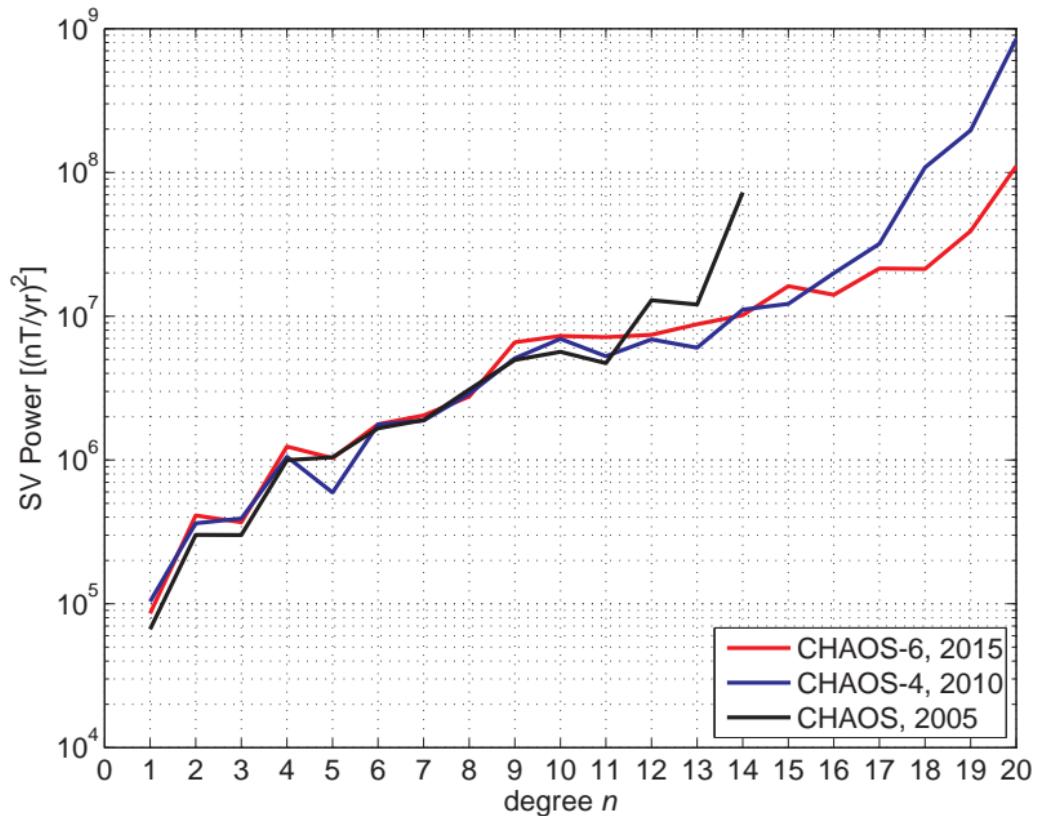
# Rate of change of field strengthening/weakening 2015



# Ground observatory series of field strength change

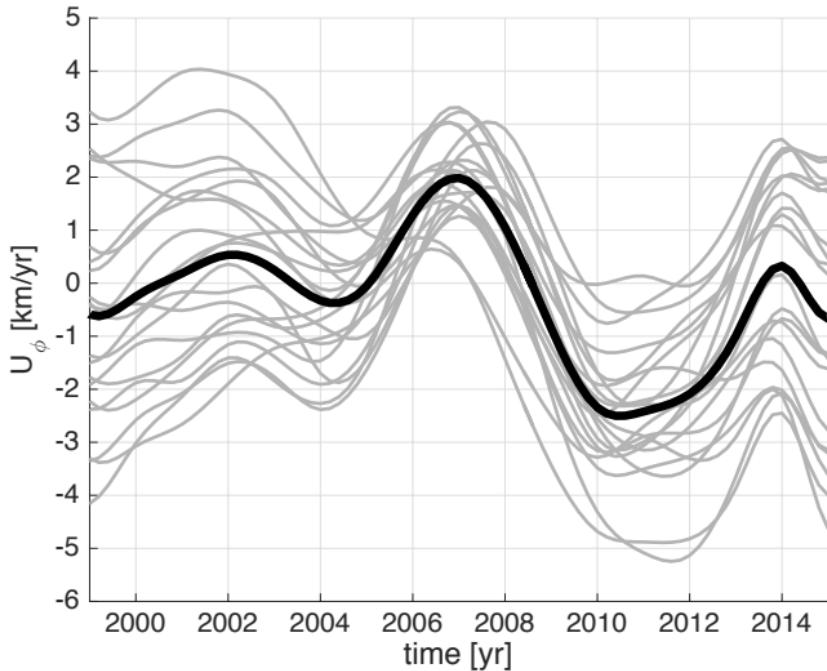


# Power spectrum of SV at core surface



## Time-dependence of core flow (another example)

- Also find non-axisymmetric flow **oscillations** at low latitudes e.g.  $0^{\circ}\text{N}$ ,  $40^{\circ}\text{W}$



# Predictions from time-dependence of core flow: KOU

